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(12) United States Patent Ludwig

(54) ADVANCED LENSLESS LIGHT-FIELD IMAGING SYSTEMS FOR ENABLING A WIDE RANGE OF ENTIRELY NEW APPLICATIONS

(71) Applicant: NRI R&D PATENT LICENSING,

LLC, San Antonio, TX (US)

(72) Inventor: Lester F. Ludwig, San Antonio, TX

(US)

(73) Assignee: NRI R&D Patent Licensing, LLC,

San Antonio, TX (US)

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patent is extended or adjusted under 35

U.S.C. 154(b) by 0 days.

This patent is subject to a terminal dis-

claimer.

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(65) Prior Publication Data

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(Continued)

(51) Int. Cl. G06T 7/557 H01L 27/30

(2017.01) (2006.01)

(Continued)

(52) U.S. Cl.

(Continued)

(10) Patent No.: US 10,546,382 B2

(45) **Date of Patent:**

*Jan. 28, 2020

(58) Field of Classification Search

CPC G06T 7/557; G06T 2207/10052; G06T 2207/10024; H01L 27/288; H01L 27/307; H04N 9/045; H04N 5/3745; H04N 5/378 See application file for complete search history.

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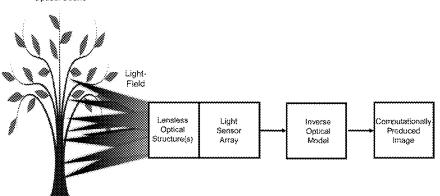
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Primary Examiner — Christopher K Peterson

(57) ABSTRACT

Continuing a sequence of lensless light-field imaging camera patents beginning 1999, the present invention adds light-use efficiency, predictive-model design, distance-parameterized interpolation, computational efficiency, arbitrary shaped surface-of-focus, angular diversity/redundancy, distributed image sensing, plasmon surface propagation, and other fundamentally enabling features. Embodiments can be fabricated entirely by printing, transparent/semi-transparent, layered, of arbitrary size/curvature, flexible/bendable, emit light, focus and self-illuminate at zero-separation distance between (planar or curved) sensing and observed surfaces, robust against damage/occultation, implement color sensing without use of filters or diffraction, overlay on provided surfaces, provided color and enhanced multi-wavelength color sensing, wavelength-selective imaging of near-infrared/near-ultraviolet, and comprise many other fundamentally enabling features. Embodiments can be thinner, larger/ smaller, more light-use efficient, and higher-performance (Continued)

Optical Scene



than recently-popularized coded aperture imaging cameras. Vast ranges of diverse previously-impossible applications are enabled: credit-card cameras/phones, in-body monitoring of healing/disease, advanced biomarker analysis systems, perfect eye-contact video conferencing, seeing fabrics/skin/housings, and manufacturing-monitoring, wearmonitoring, and machine vision capabilities.

22 Claims, 97 Drawing Sheets

Related U.S. Application Data

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- (51) Int. Cl.

 H01L 27/28 (2006.01)

 H04N 5/225 (2006.01)

 H04N 9/04 (2006.01)

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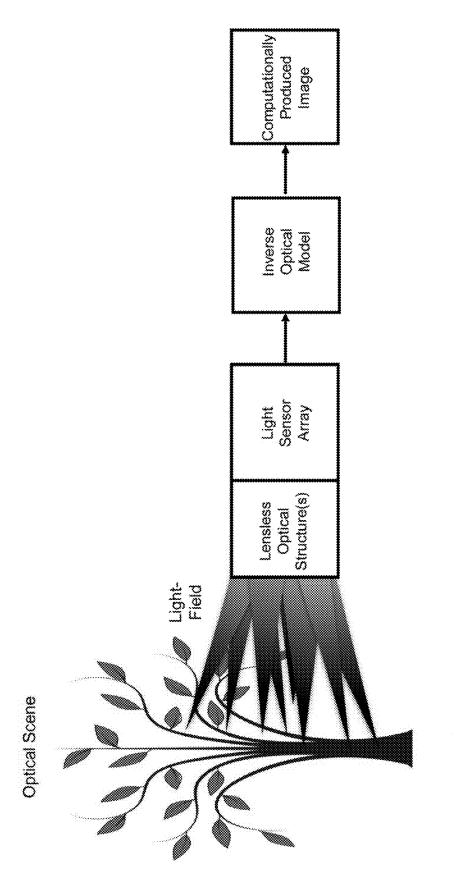
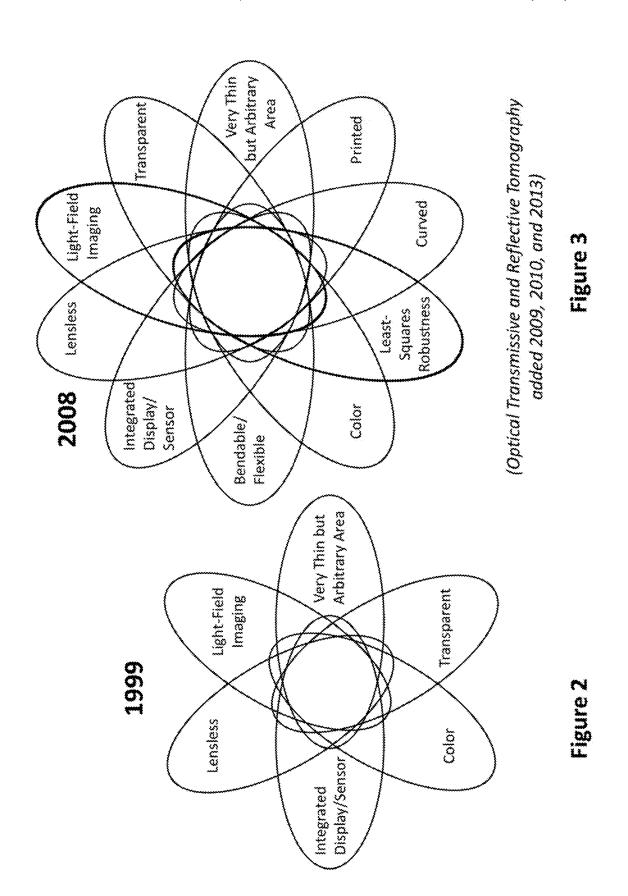
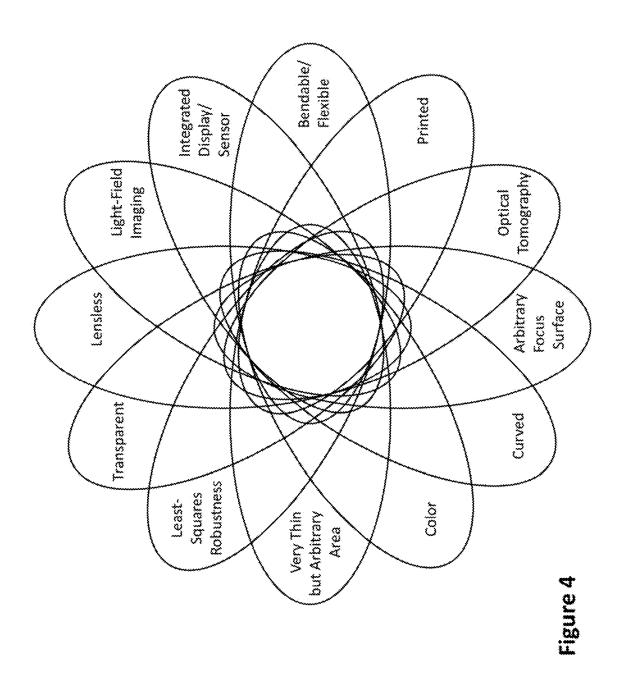
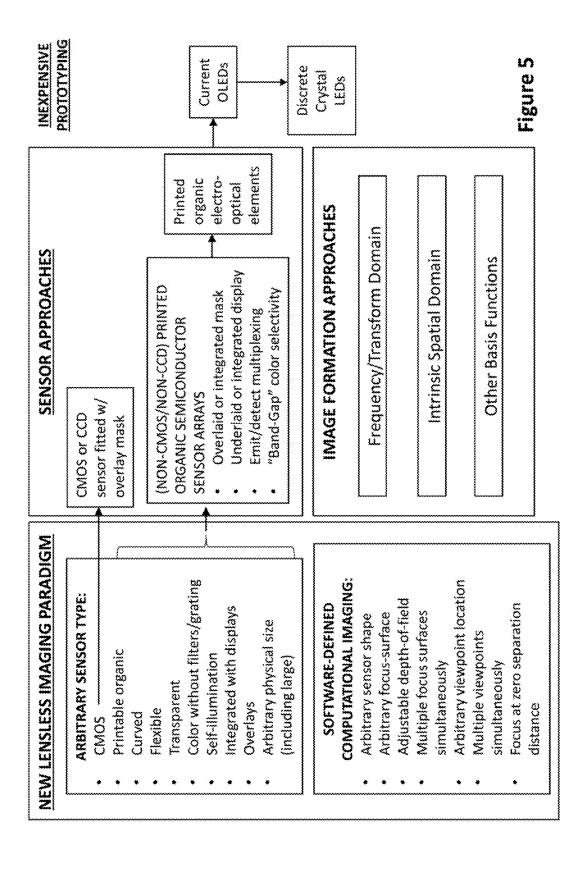
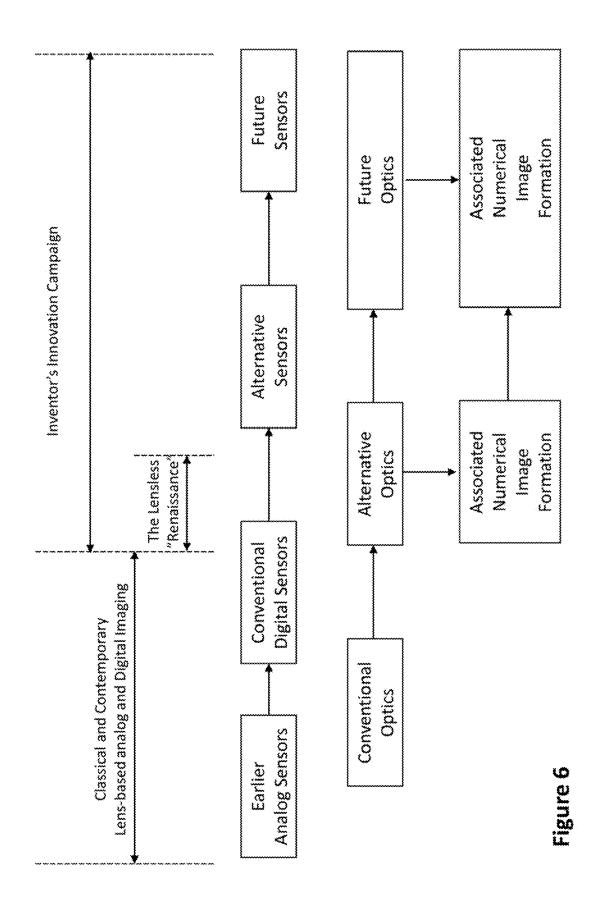


Figure 1



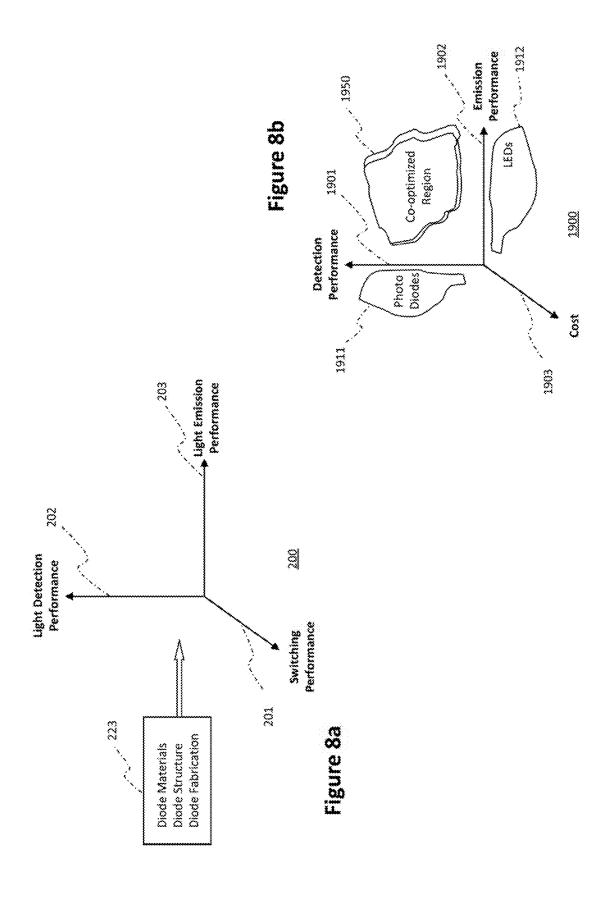


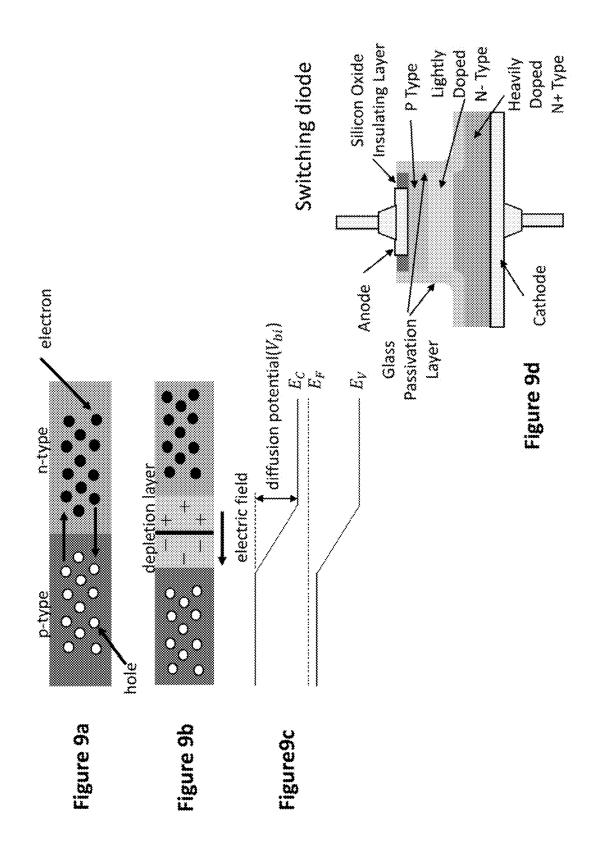




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Figure 7





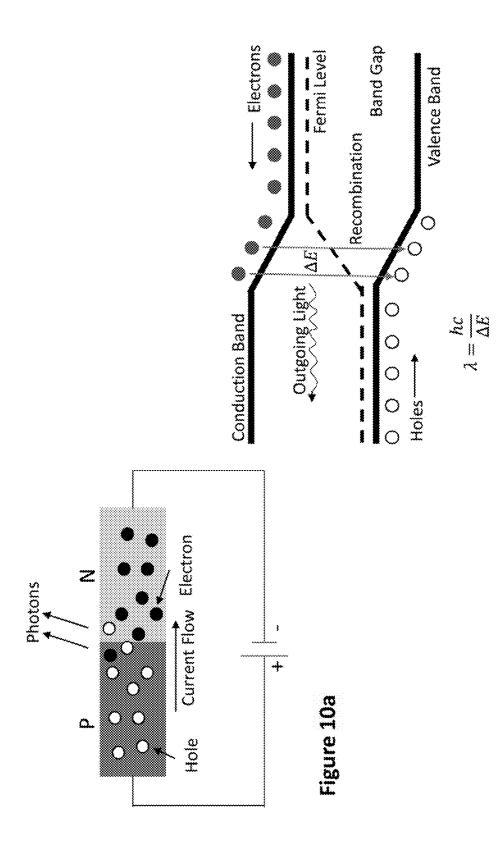


Figure 10b Band diagram of a simple LED

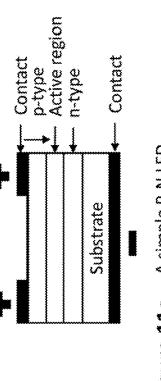


Figure 11a A simple P-N LED

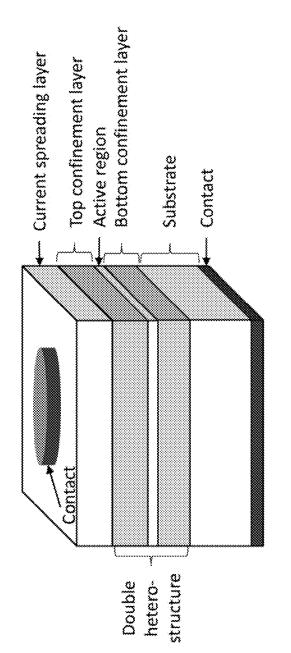
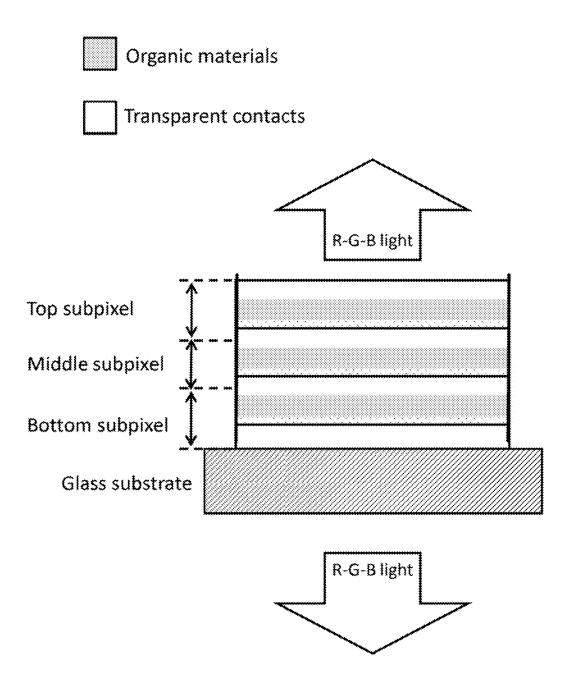
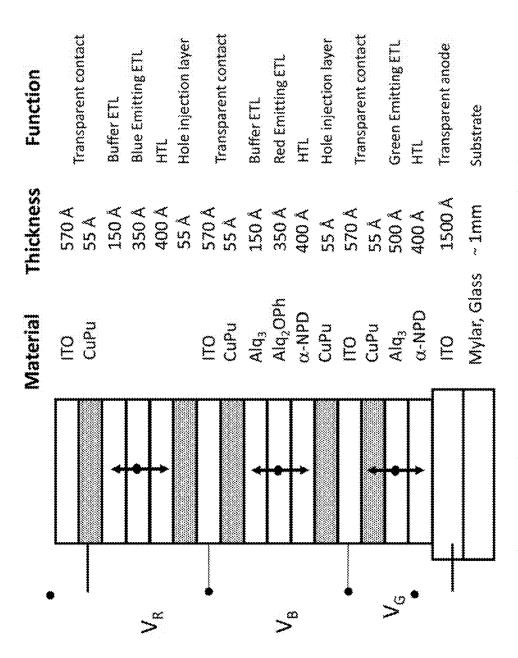


Figure 11b P-N LED with double hetero-structure



Adapted from G. Gu, G. Parthasarathy, P. Burrows, T. Tian, I. Hill, A. Kahn, S. Forrest, "Transparent stacked organic light emitting devices. I. Design principles and transparent compound electrodes," *Journal of Applied Physics*, October 1999, vol. 86 no. 8, pp.4067-4075.

Figure 12a



compound electrodes," Journal of Applied Physics, October 1999, vol. 86 no. 8, pp.4087-4075. Adapted from G. Gu, G. Parthasarathy, P. Burrows, T. Tian, I. Hill, A. Kahn, S. Forrest, "Transparent stacked organic light emitting devices. I. Design principles and transparent

Figure 12b

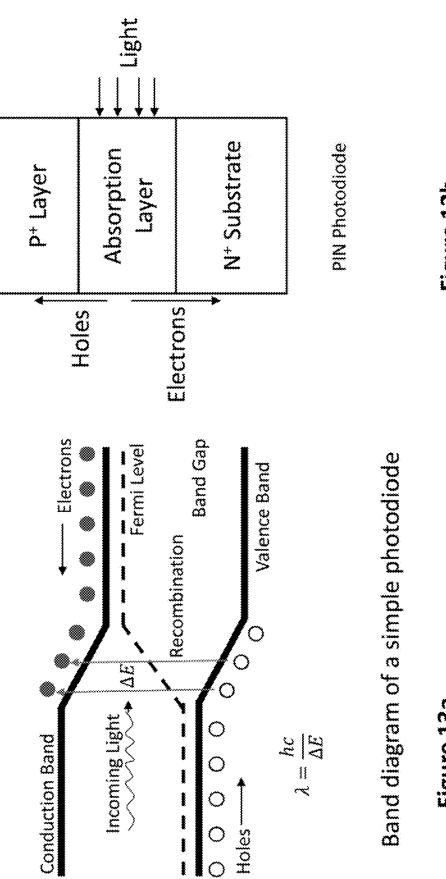
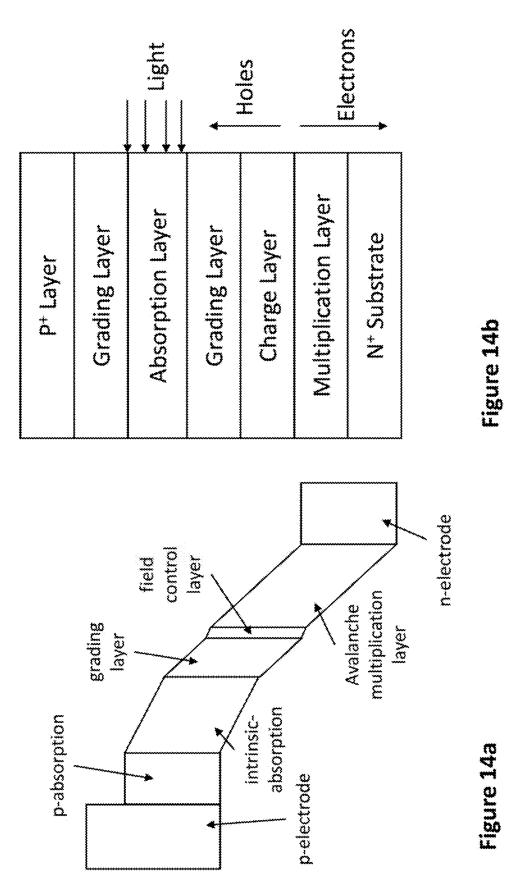


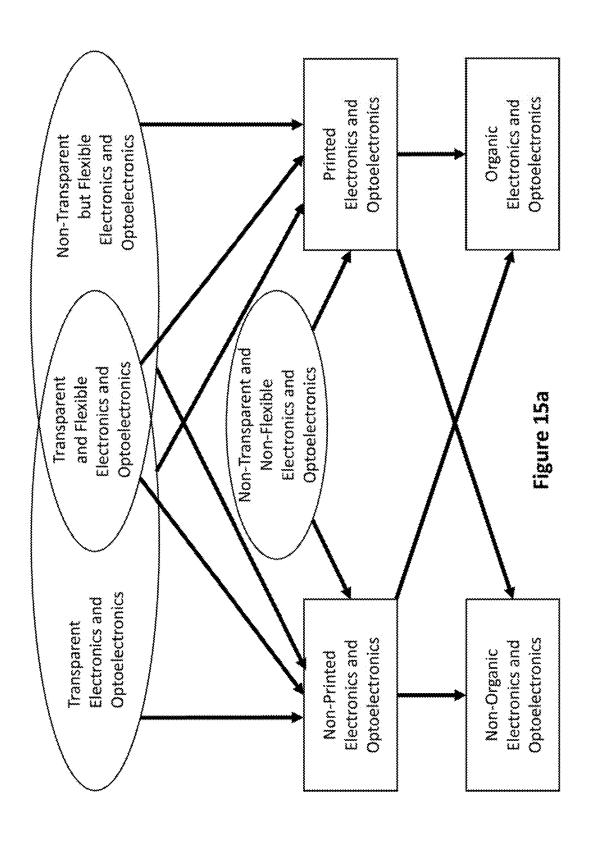
Figure 13b

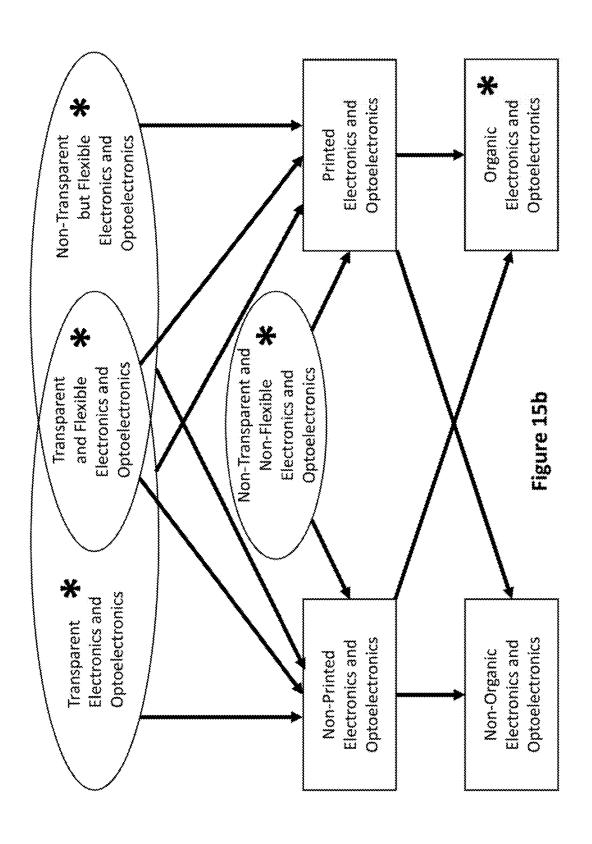
Figure 13a

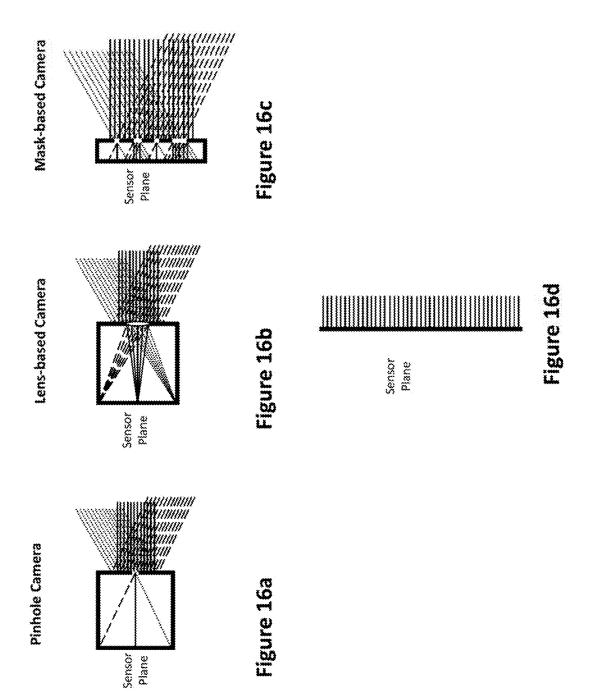


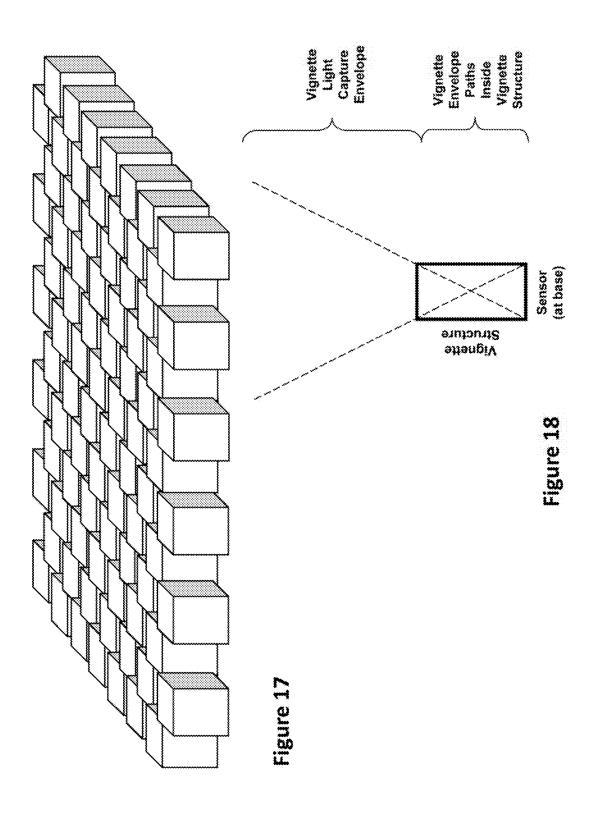
Avalanche photodiode (APD)

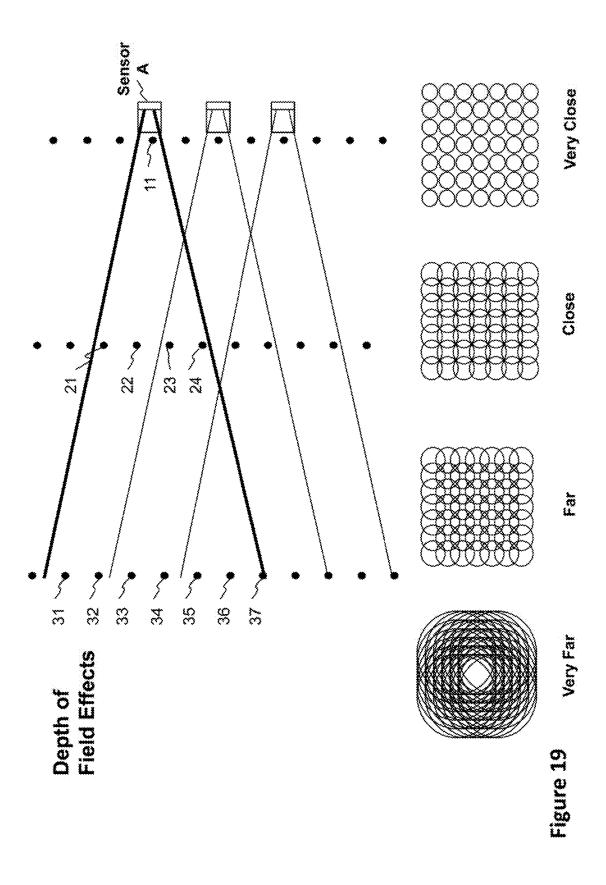
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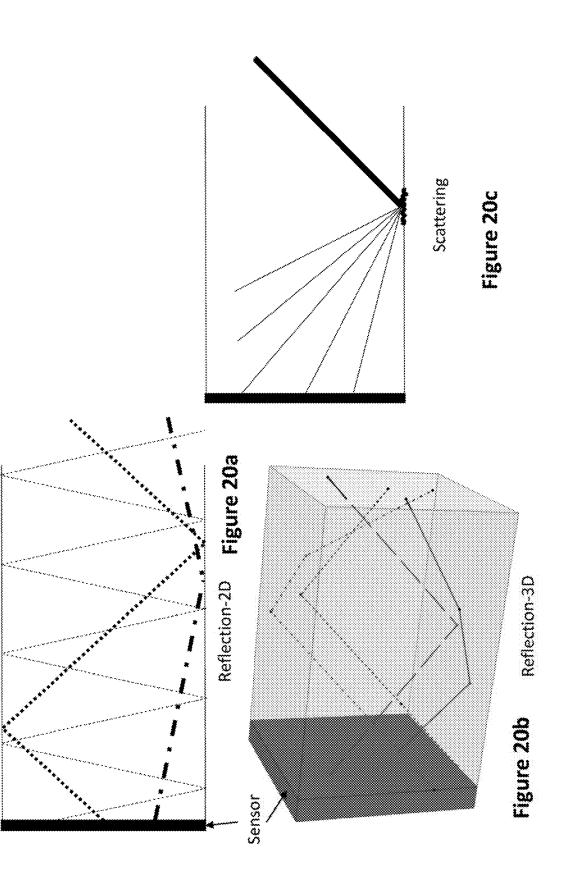


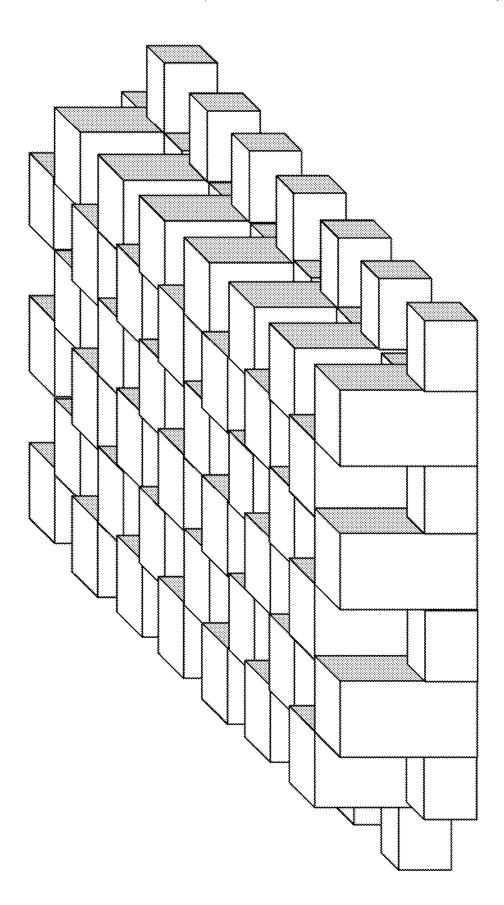


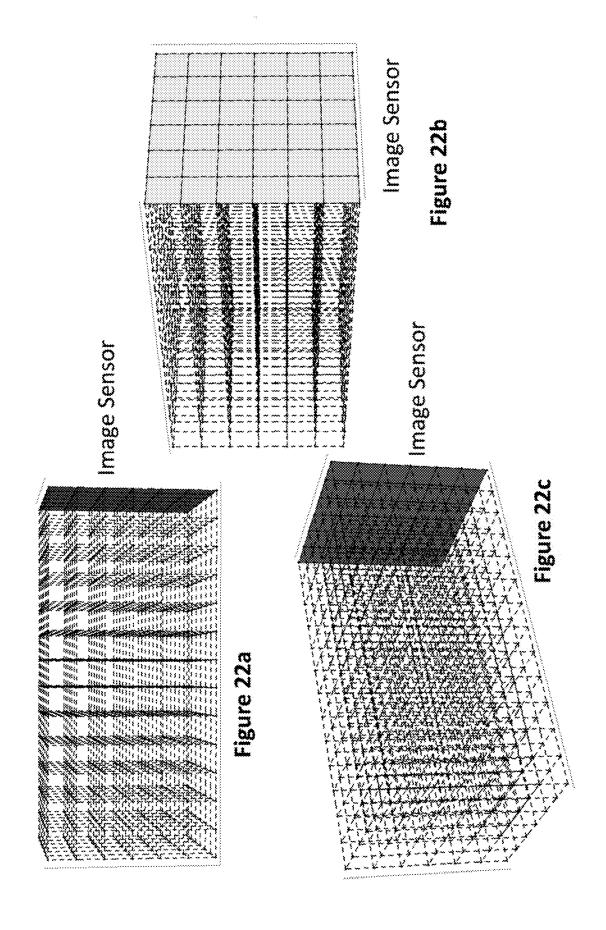


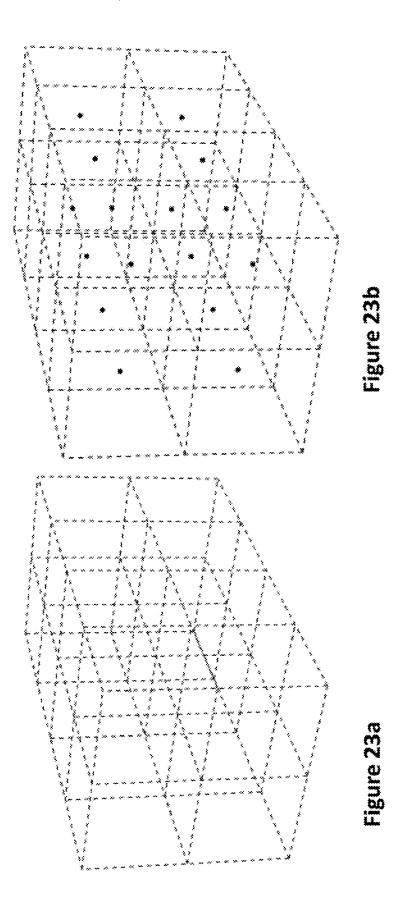


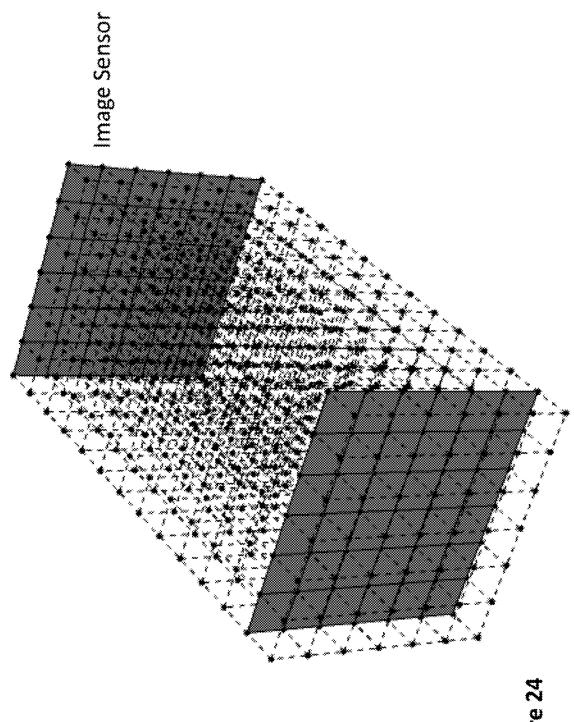


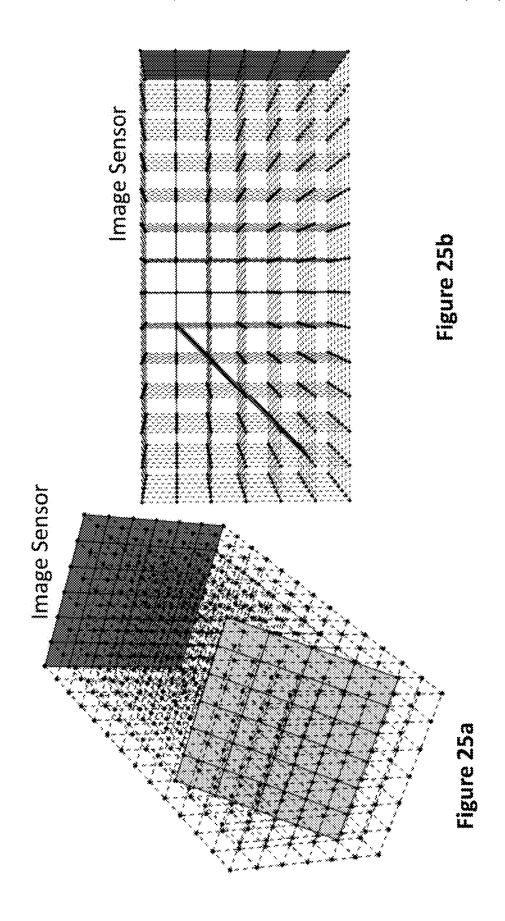


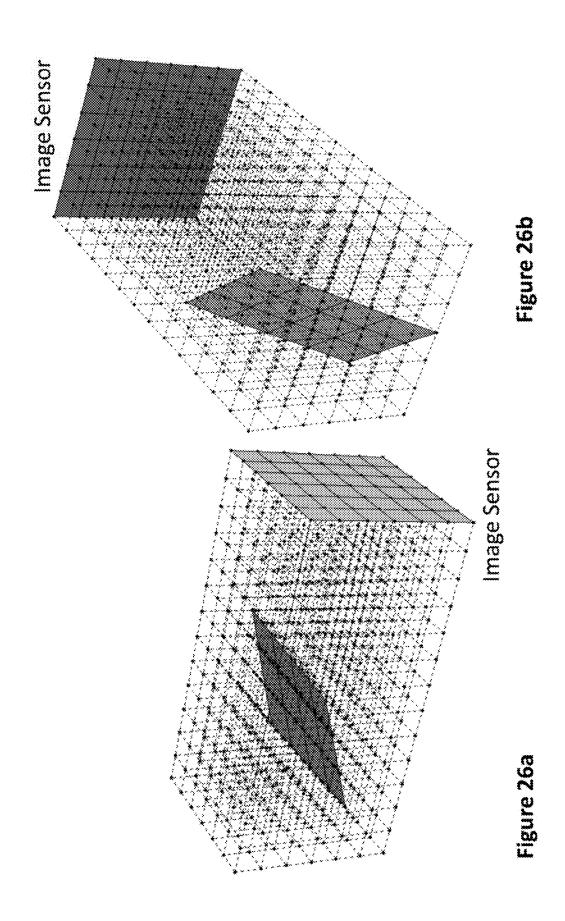


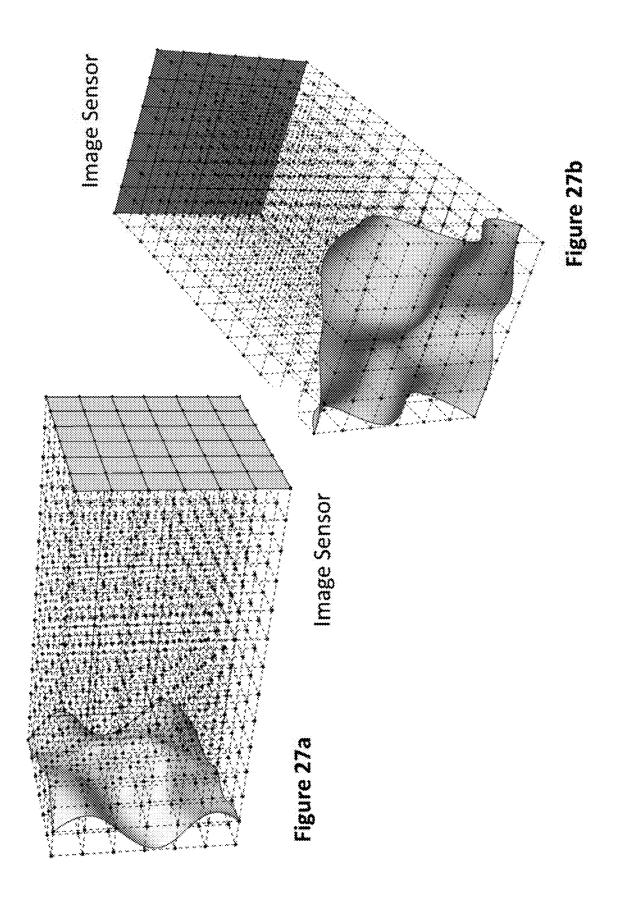


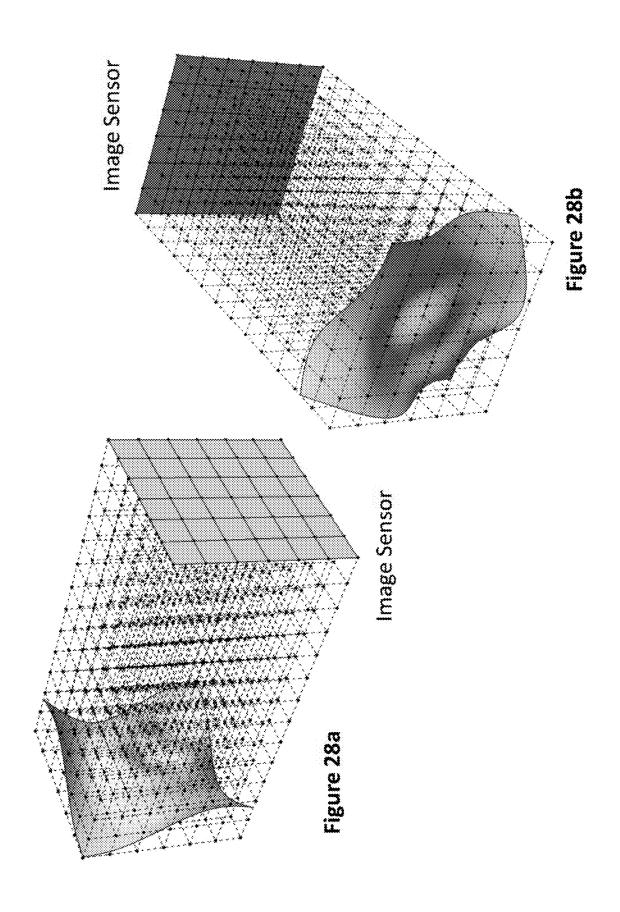


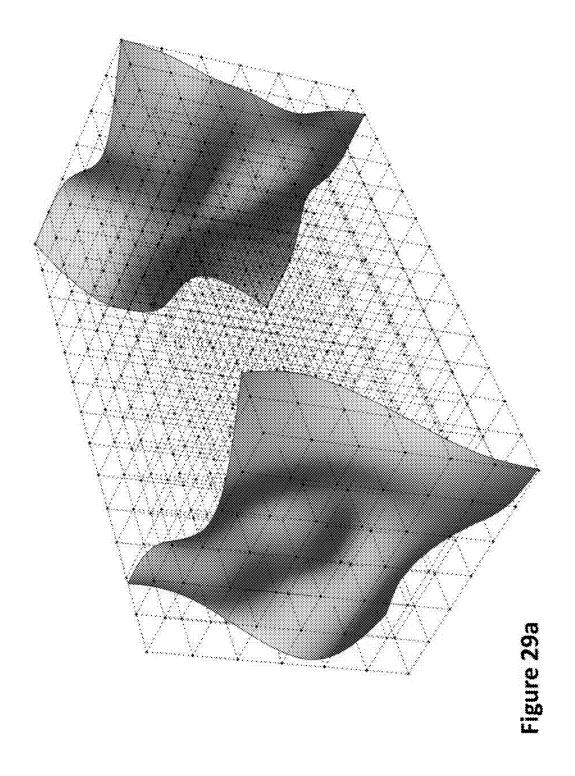




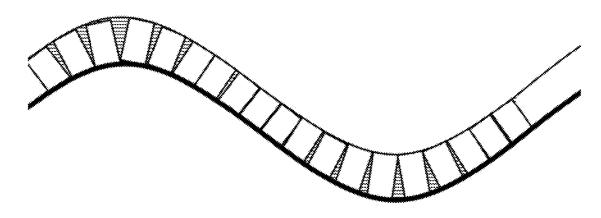




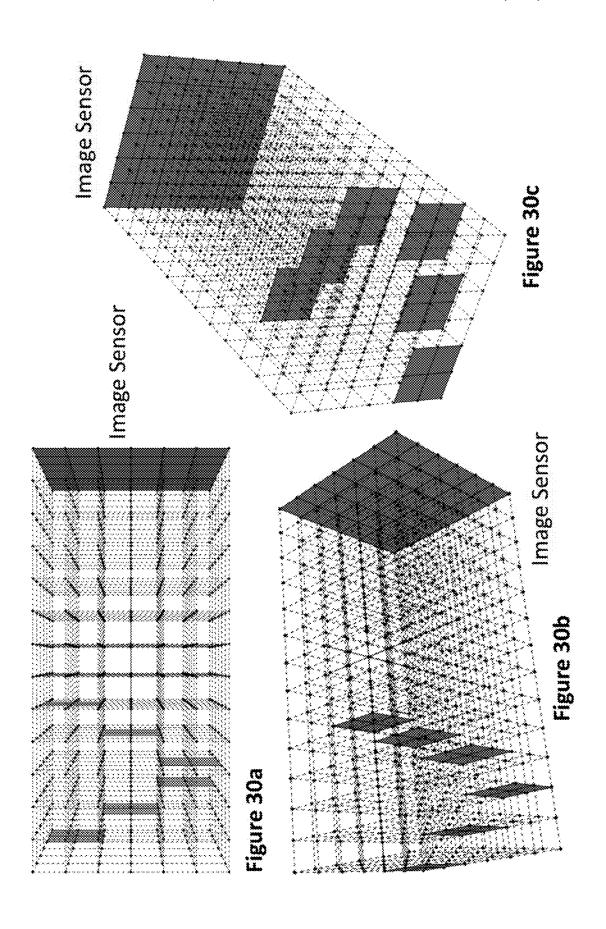


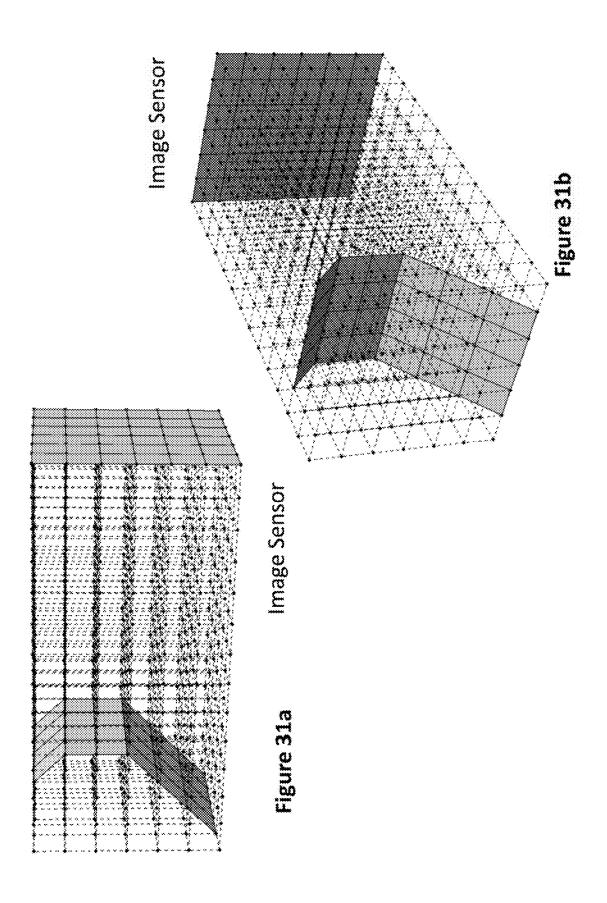


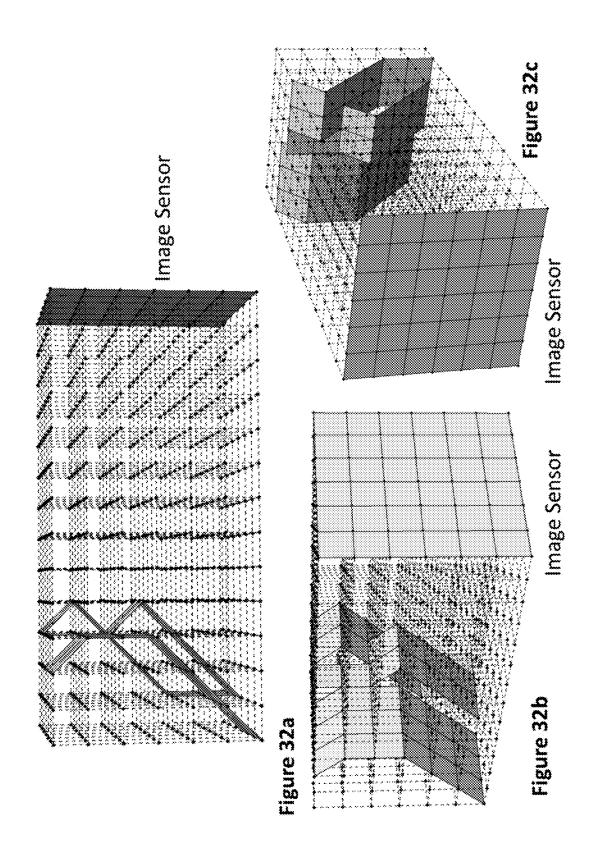


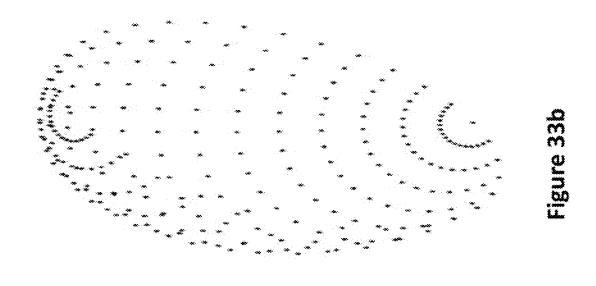


Sensor Side









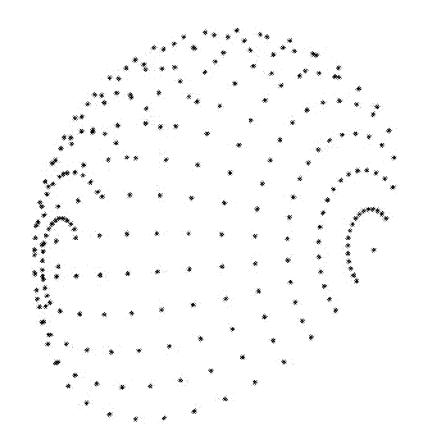
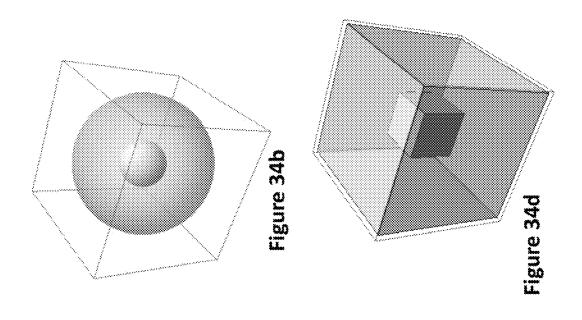
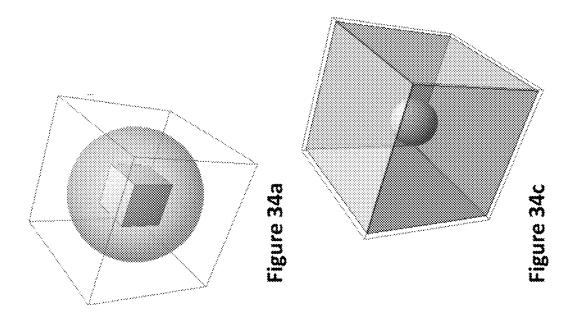
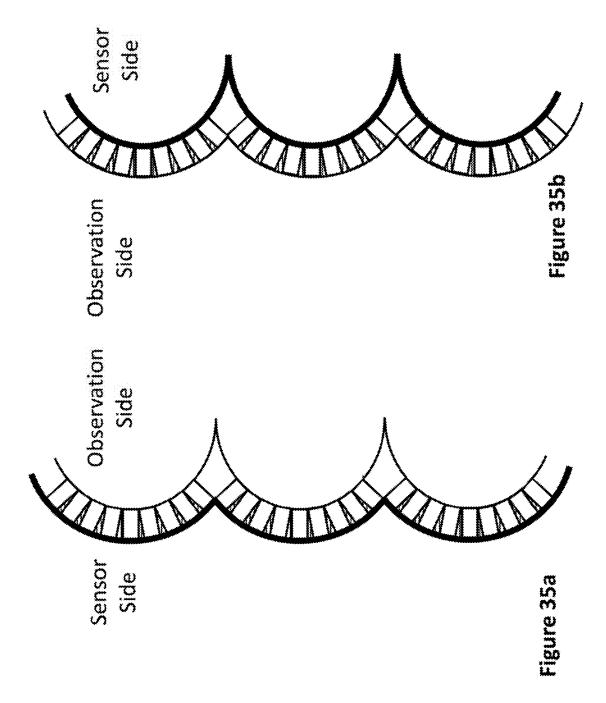
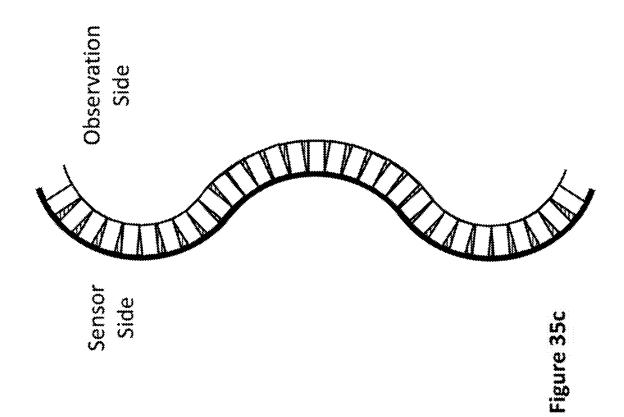


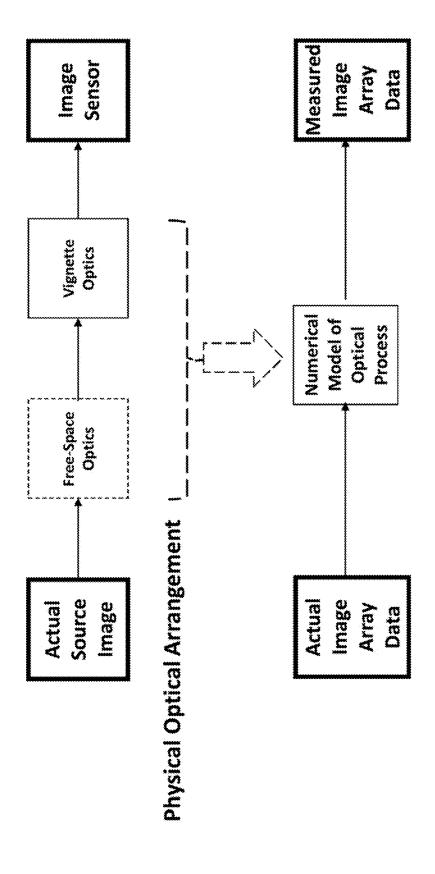
Figure 33a







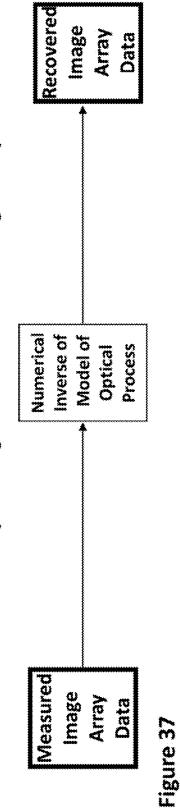




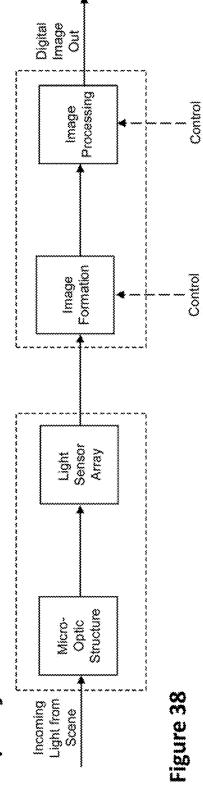
Mathematical Model of Physical Optical Arrangement

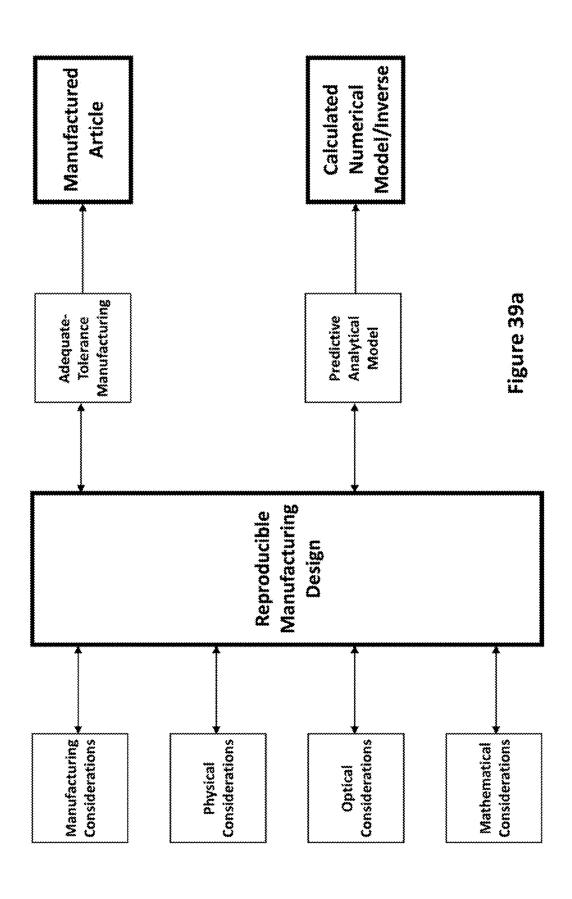
Figure 36

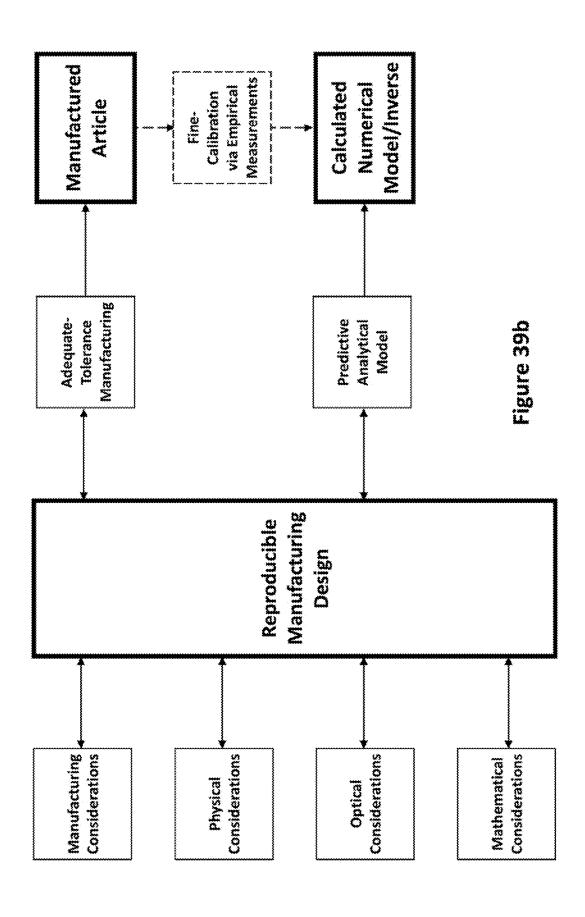
Mathematical Recovery of Image from Measured Image Array Data:

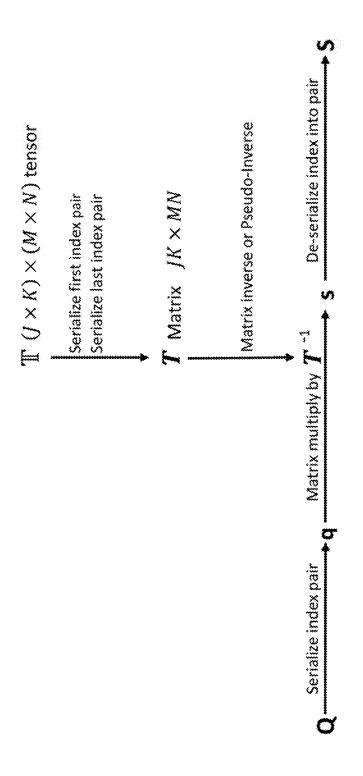


Example System Architecture









igure 40

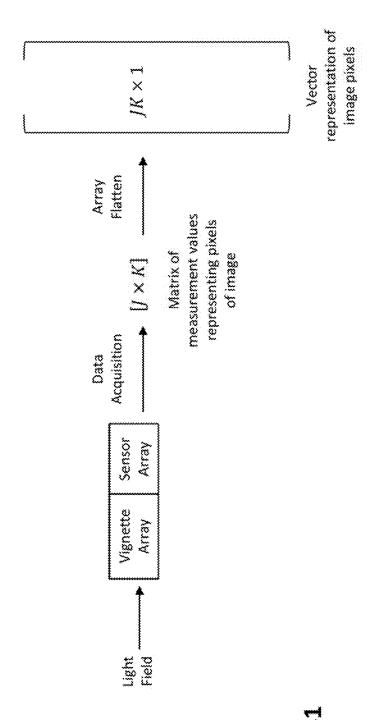


Figure 4

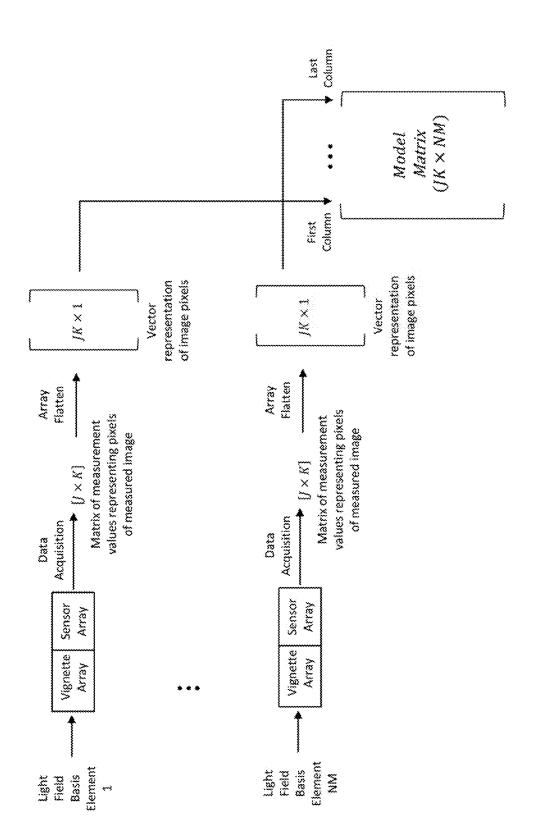


Figure 42

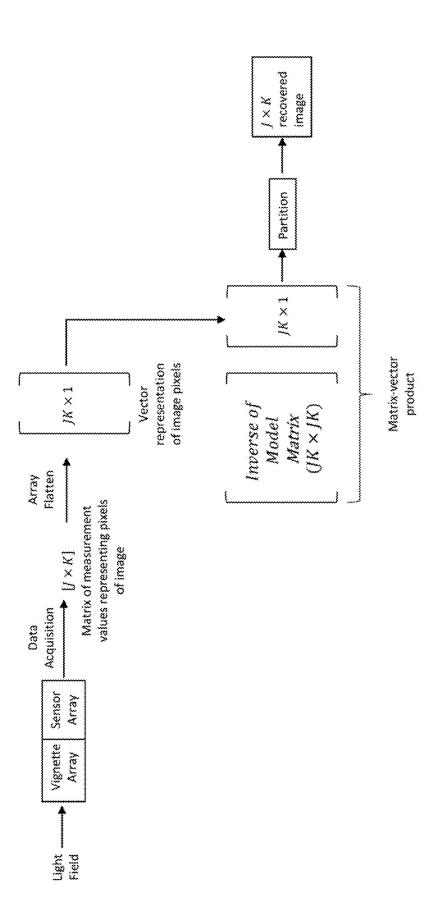
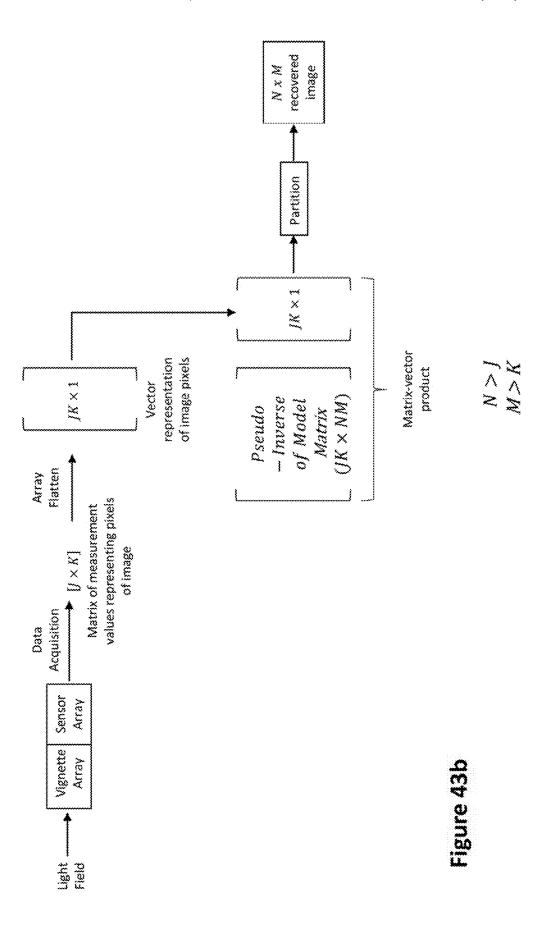
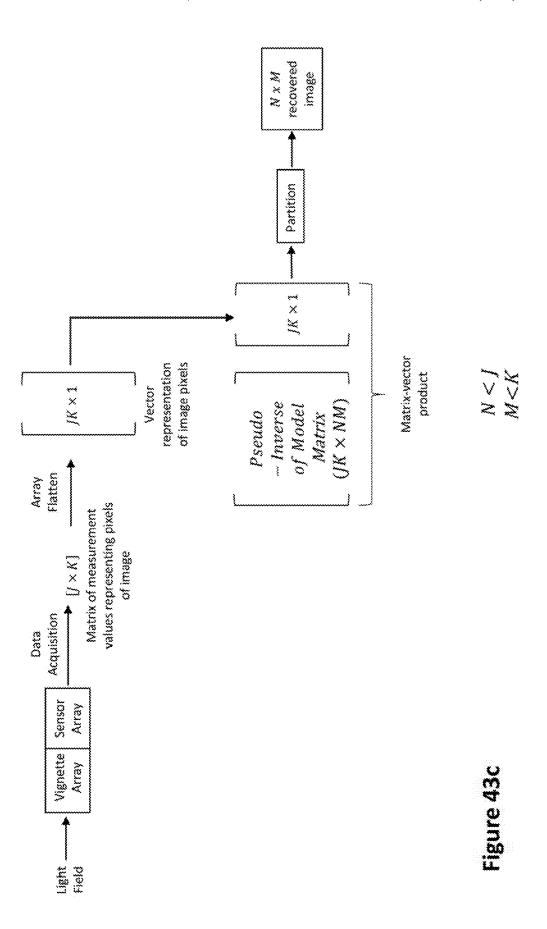


Figure 43a





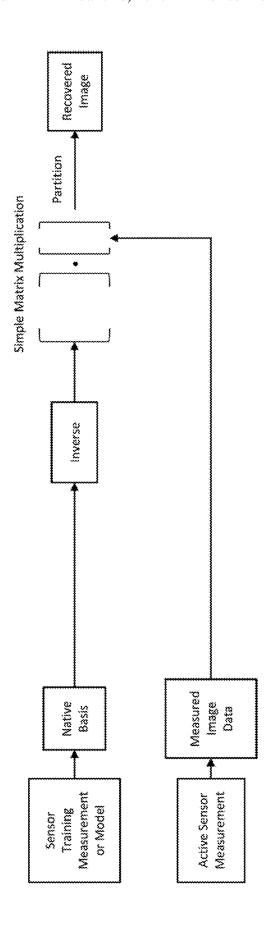
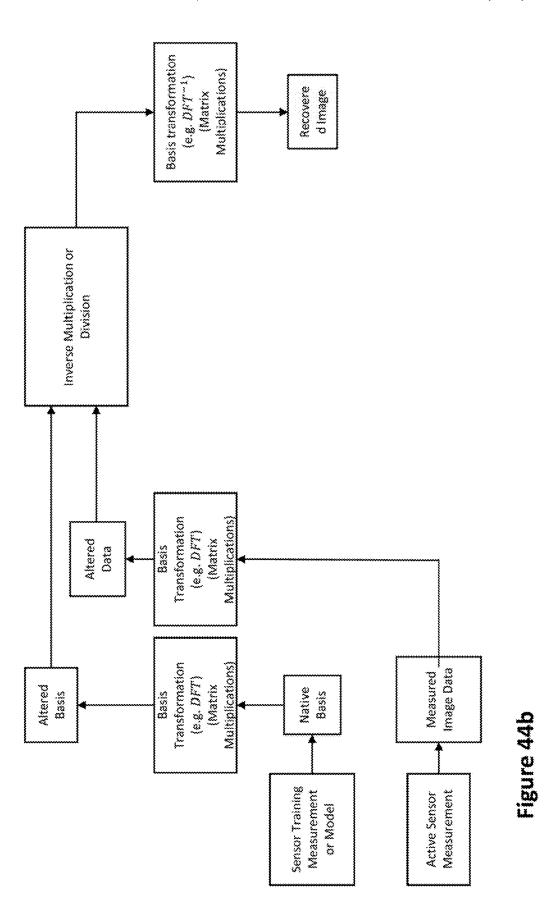
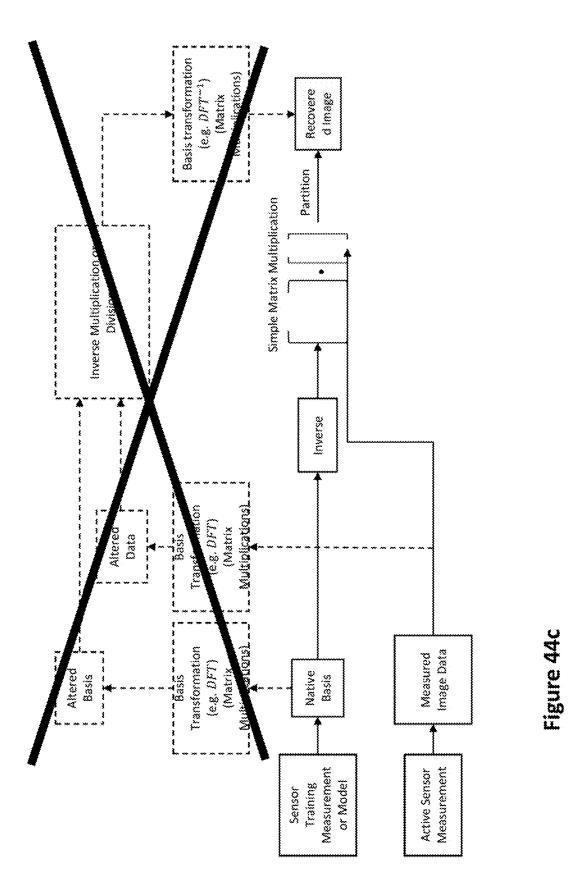


Figure 44a





Rambus

Assume x is flattened (vectorized) measured image and that measurements y include additive noise n

$$y = Ax + n$$

Find \hat{x} minimizing the error/cost function

$$C = ||A\hat{x} - y||^2 + ||F\hat{x}||^2$$

Optimal solutions have the form

 \hat{X}_{TIR} =function of SVDs of Φ_L , Φ_R and au

Optimal solutions have the form

 $\hat{x} = (A^T A + \Gamma^T \Gamma)^{-1} A^T y$

For equal error sensitivity

 $\hat{x} = (A^T A + \gamma I)^{-1} A^T y$

Figure 45

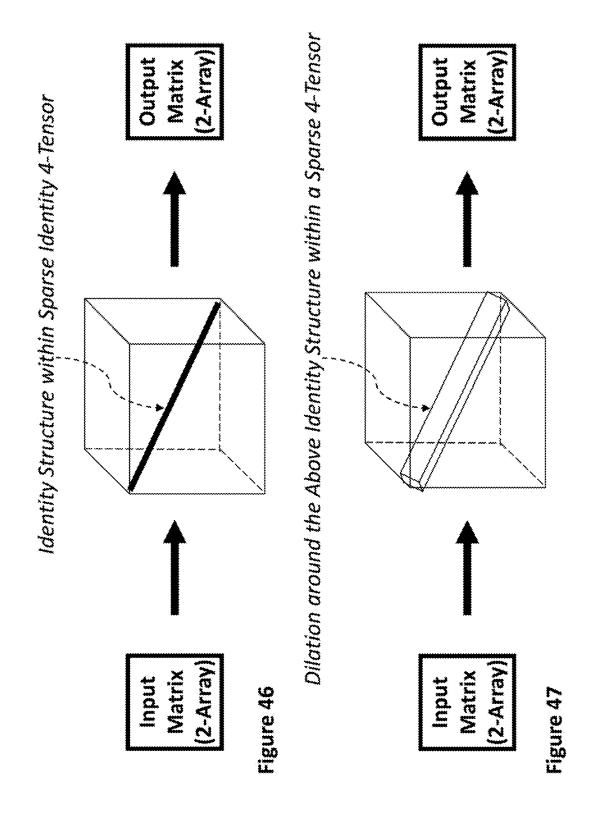
Rice Flat Cam

Assume mask is coordinate-separable

into for $\Phi_L X \Phi_R$

$$\hat{X}_{Ls} = \underset{X}{\text{arg min}} \left\| \Phi_L X \Phi_R^T - Y \right\|_2^2$$

$$\hat{X}_{Tik} = \underset{X}{\arg min} \| \Phi_L X \Phi_R^T - Y \|_2^2 + \tau \| X \|_2^2$$



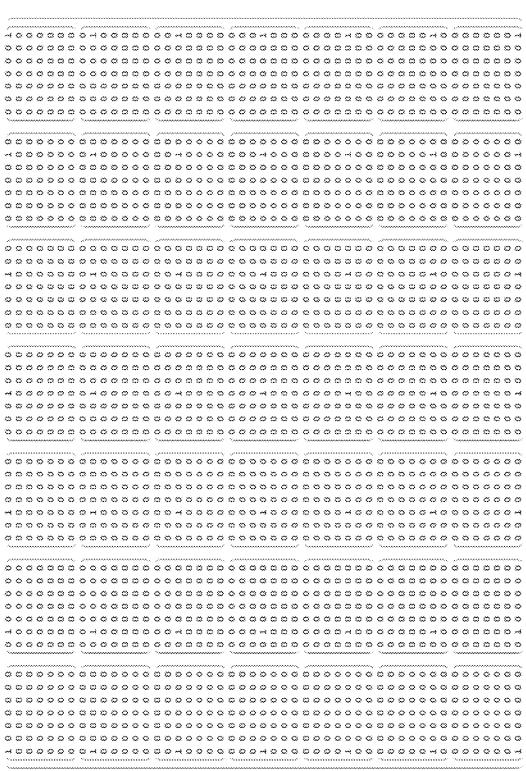
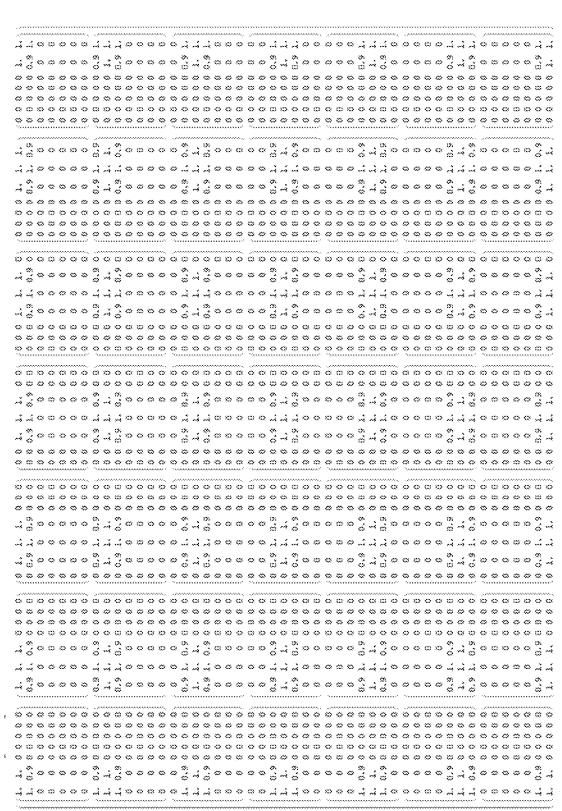


Figure 4



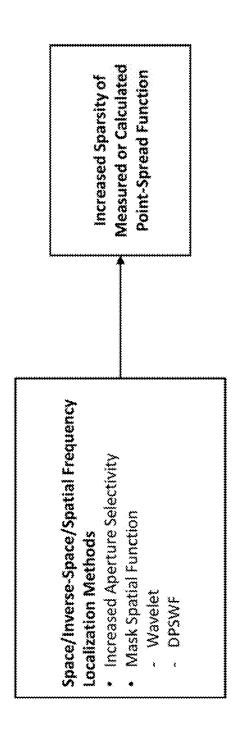
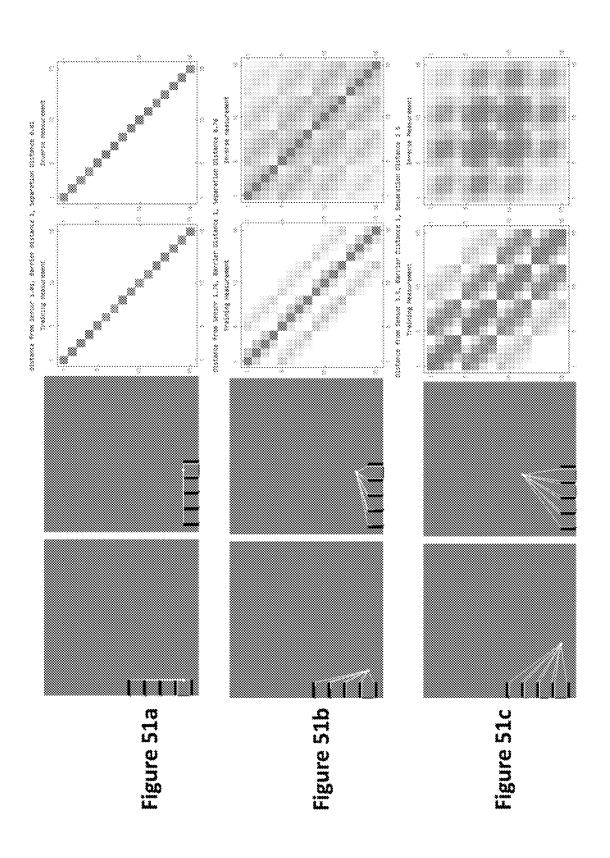
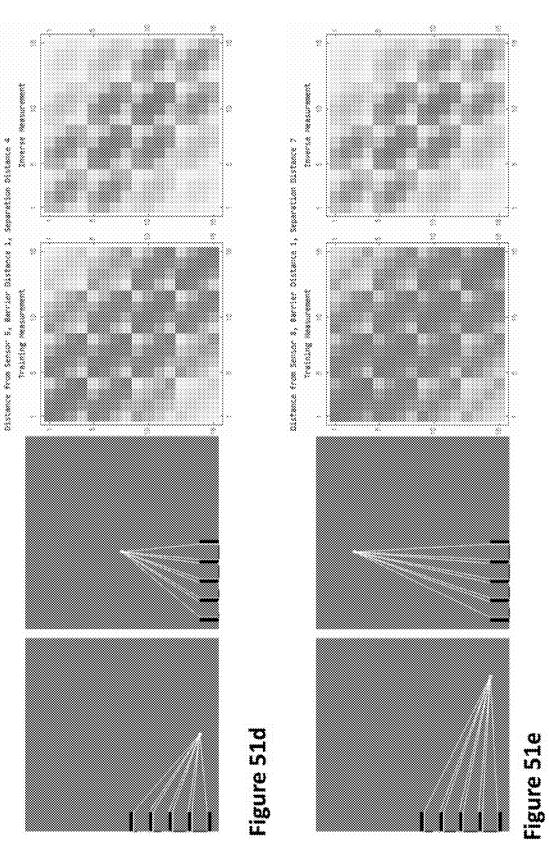
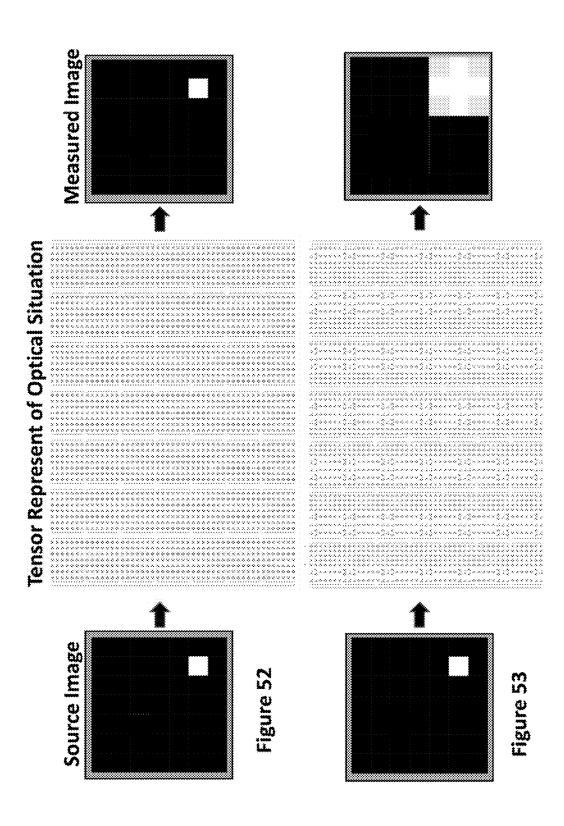
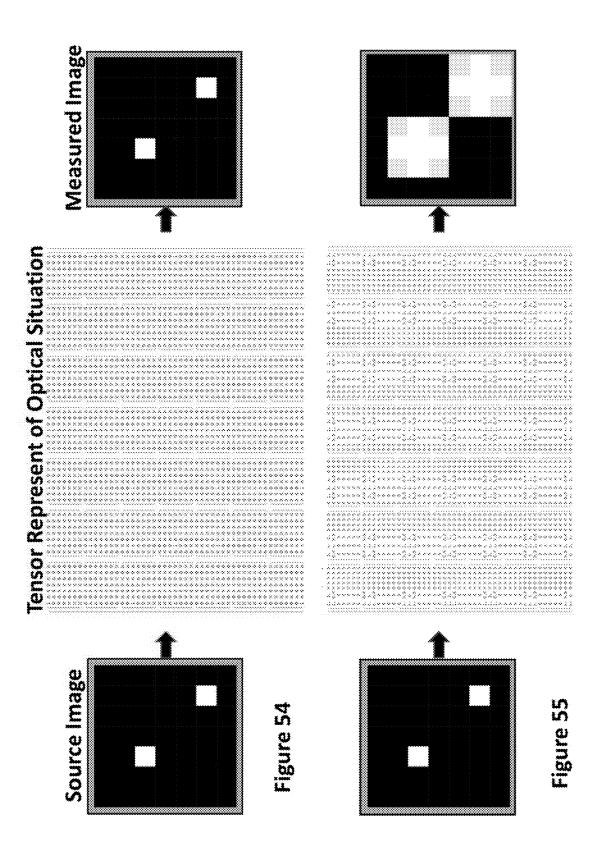


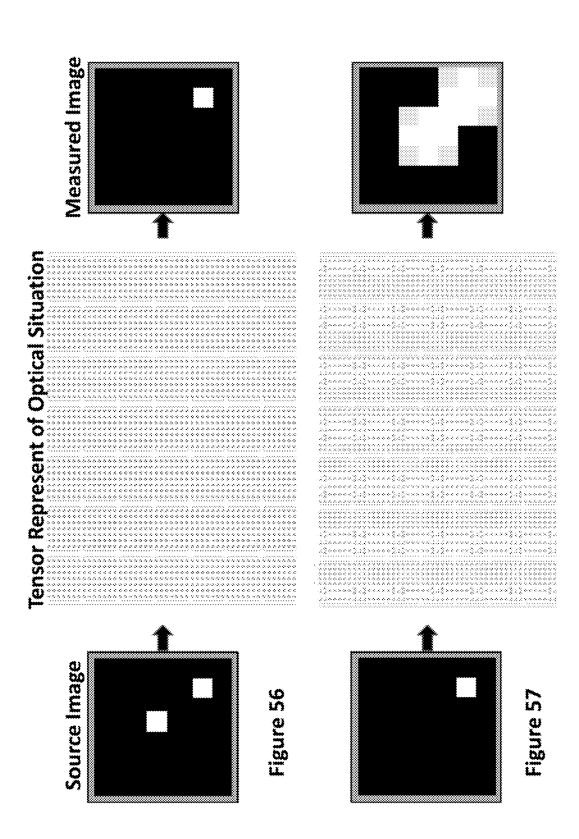
Figure 50



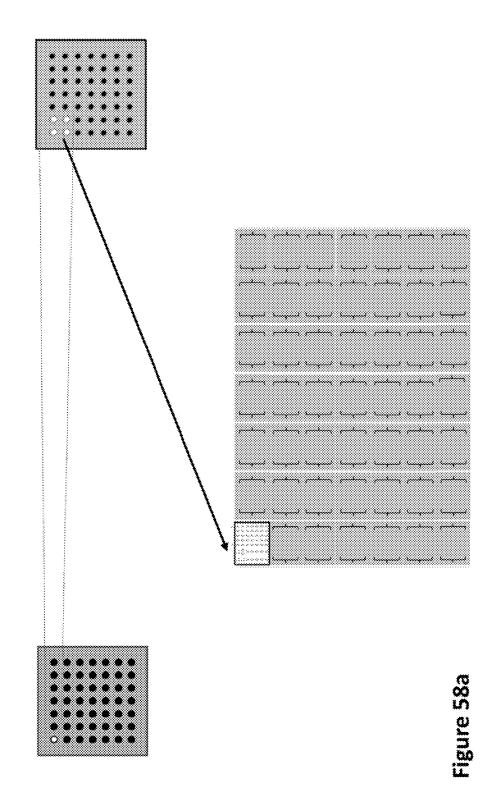




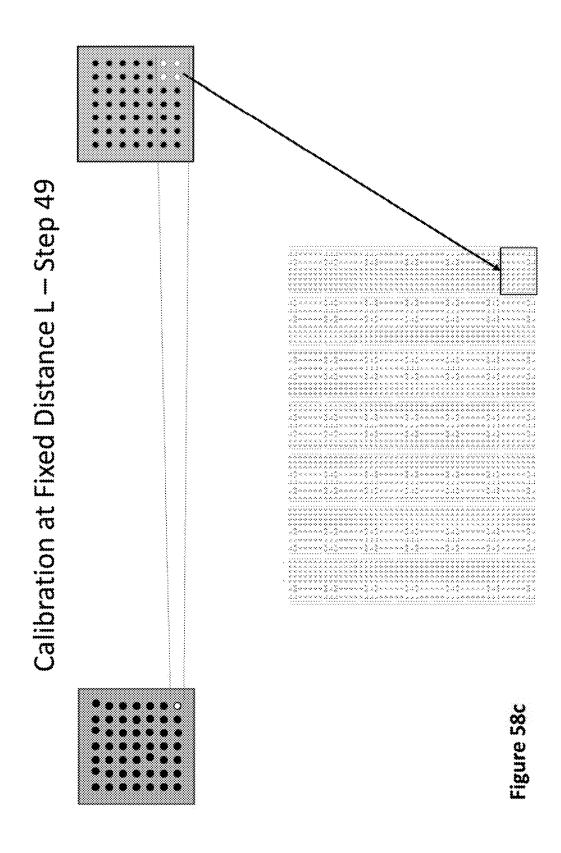




Calibration at Fixed Distance L - Step 1



Calibration at Fixed Distance L - Step 19 Figure 58b



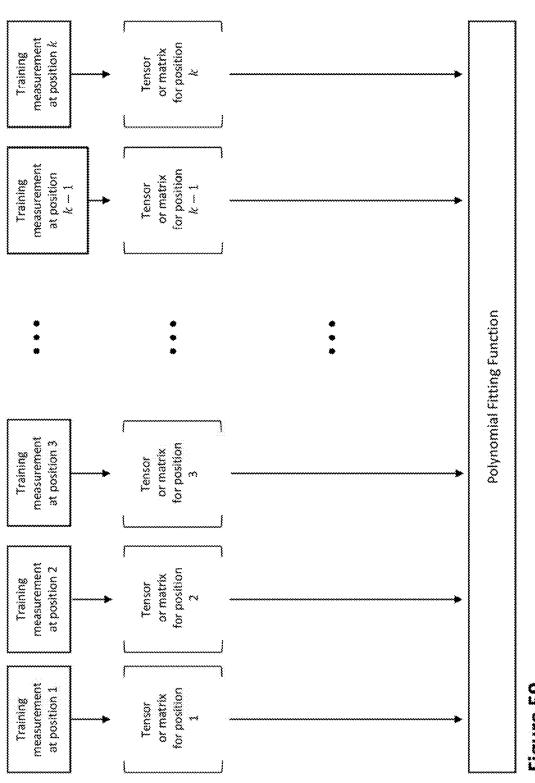


Figure 59

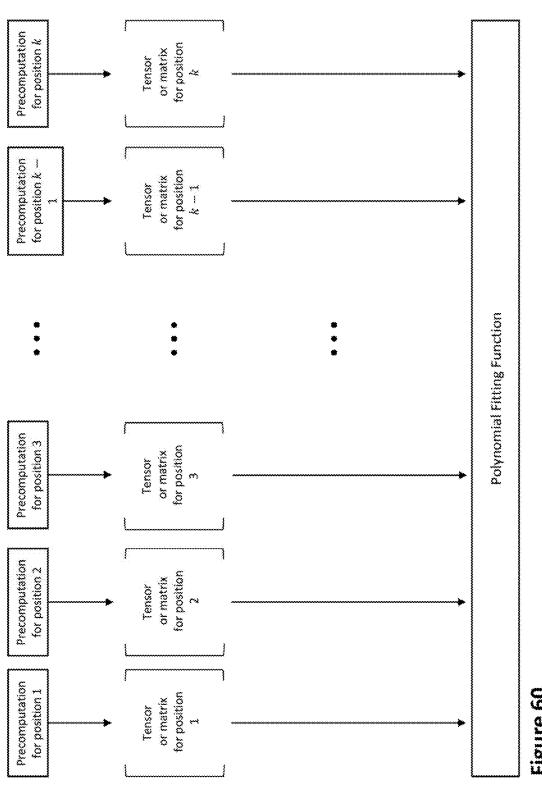


Figure 60

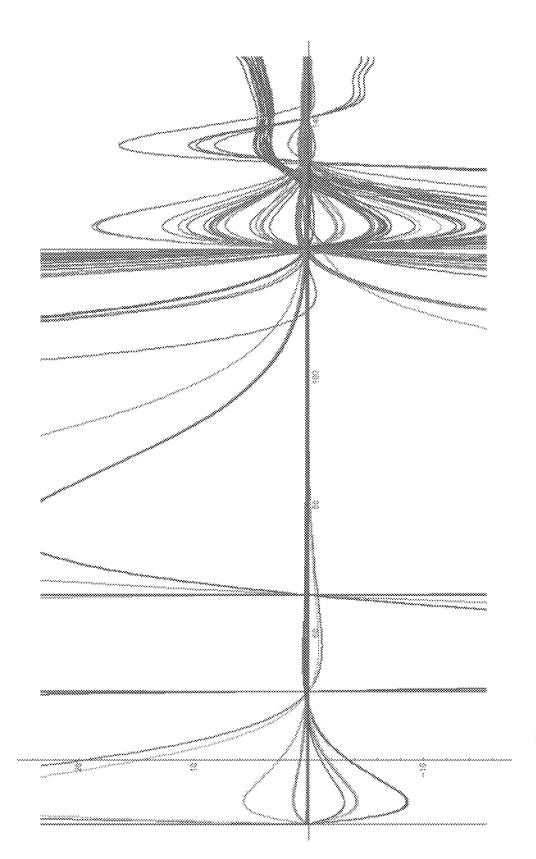
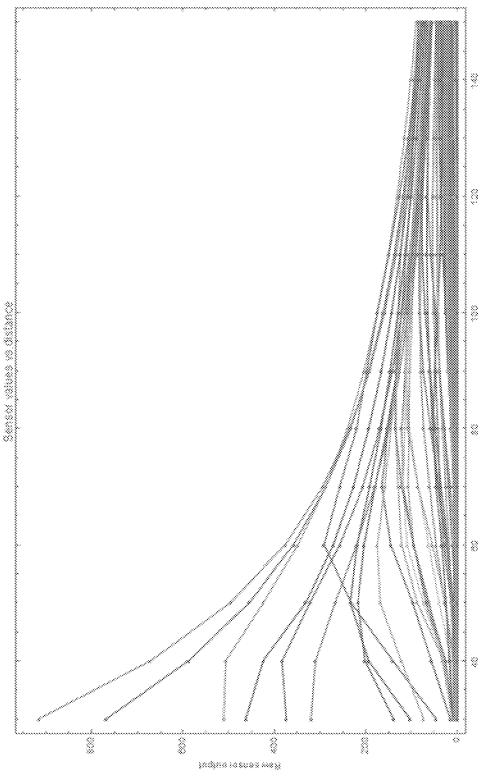
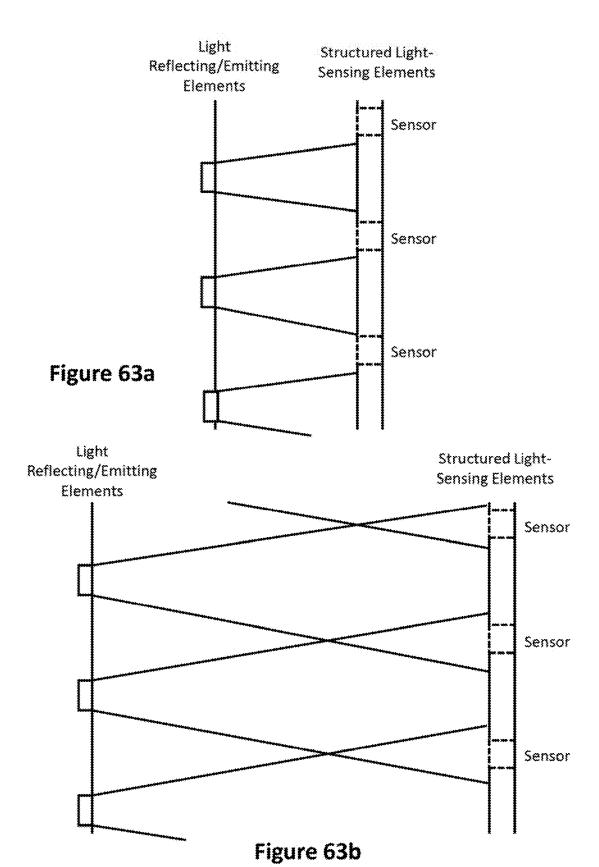


Figure 61



Piecewise-Linear Interpolation Between Measured-Dataset Separation-Distances

Figure 62



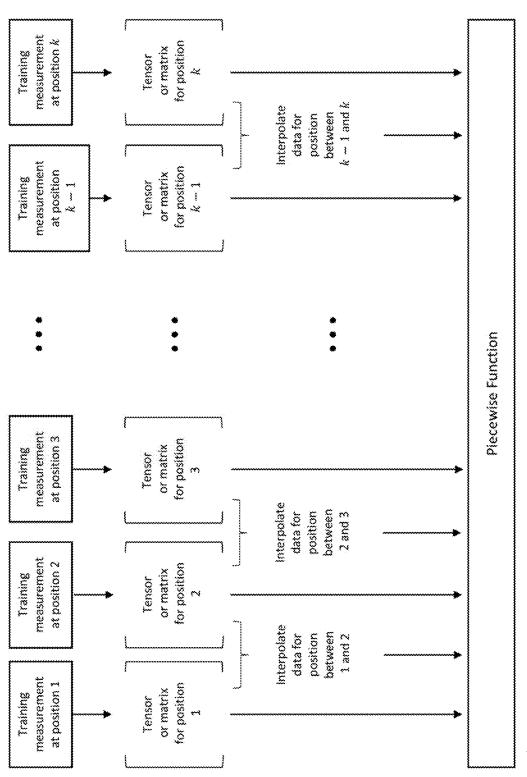
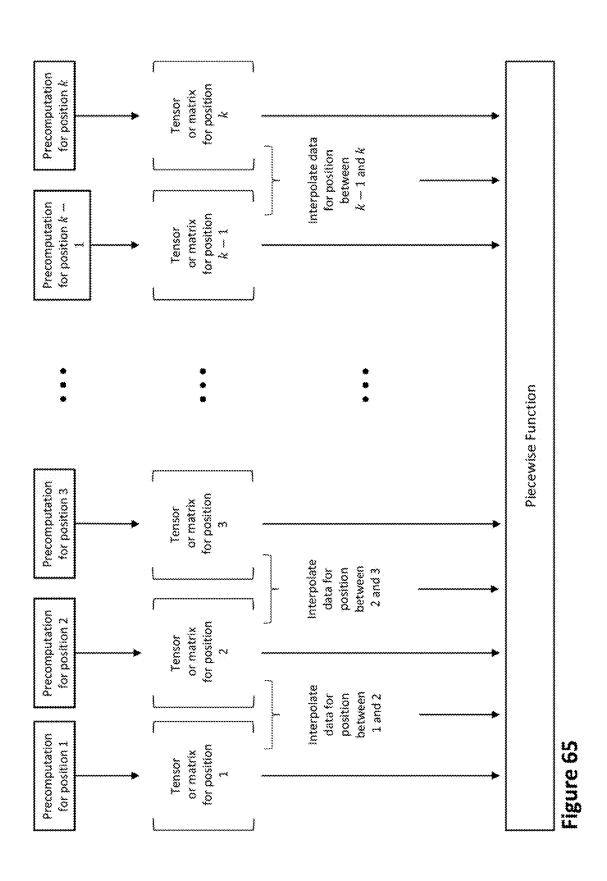
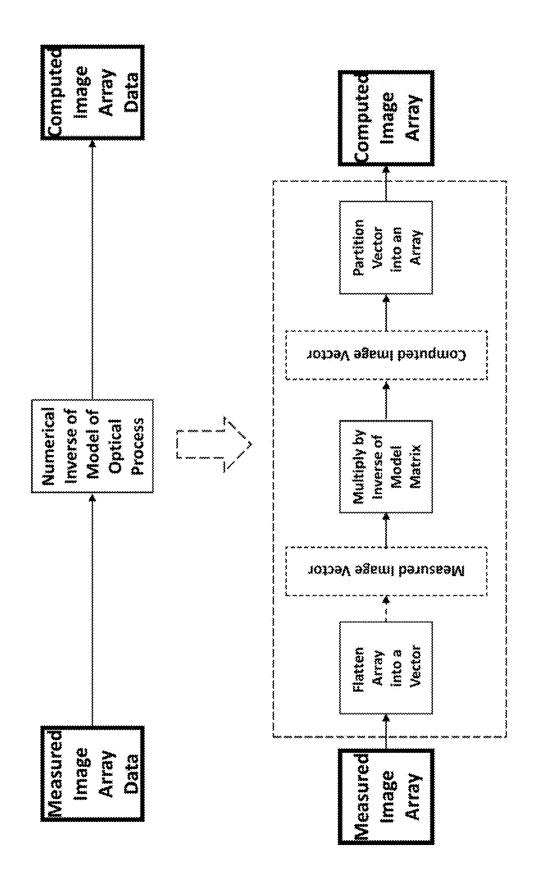


Figure 64

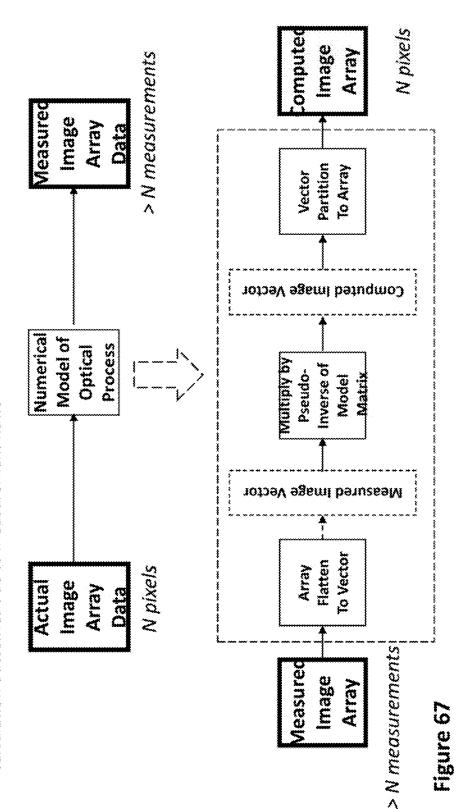


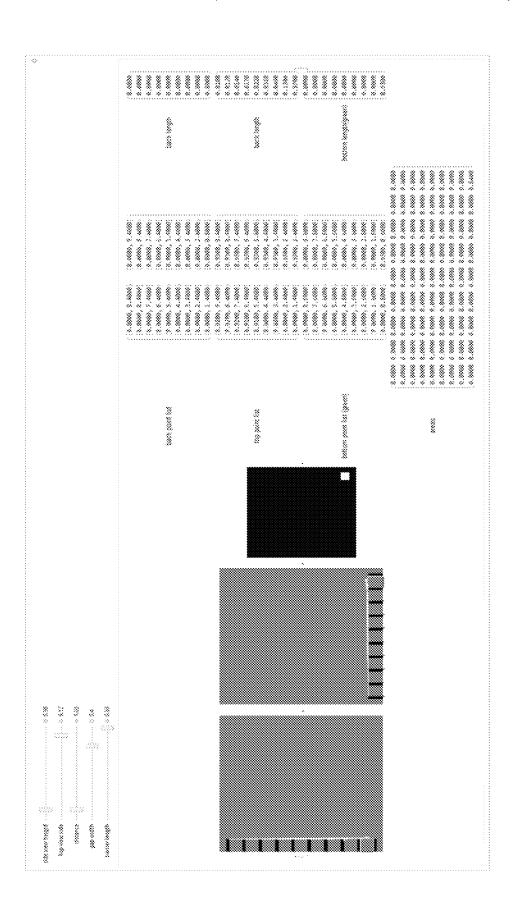


Mathematical Recovery of Image from Measured Image Array Data Figure 66

"Overspecified" Collection of Measurements:

- More measurements than needed
- Different subgroups of measurements may lead to inconsistent calculation outcomes due to measurement flaws





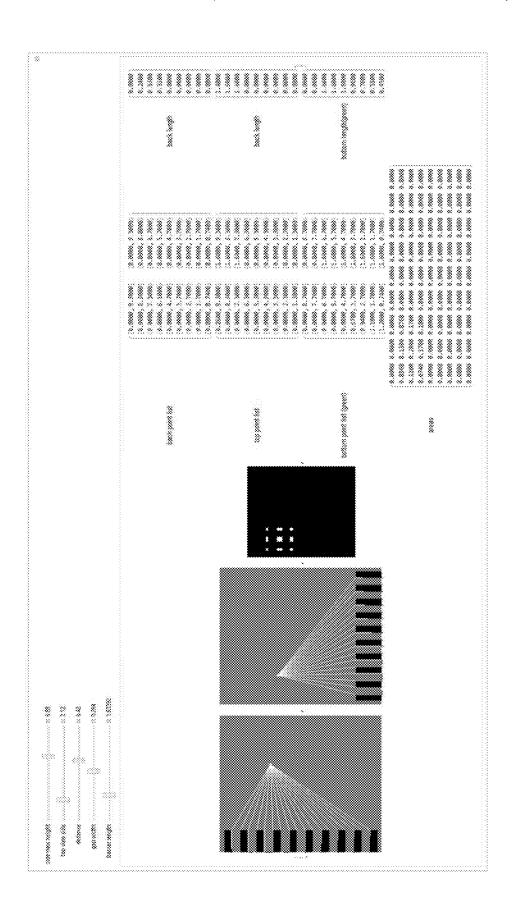
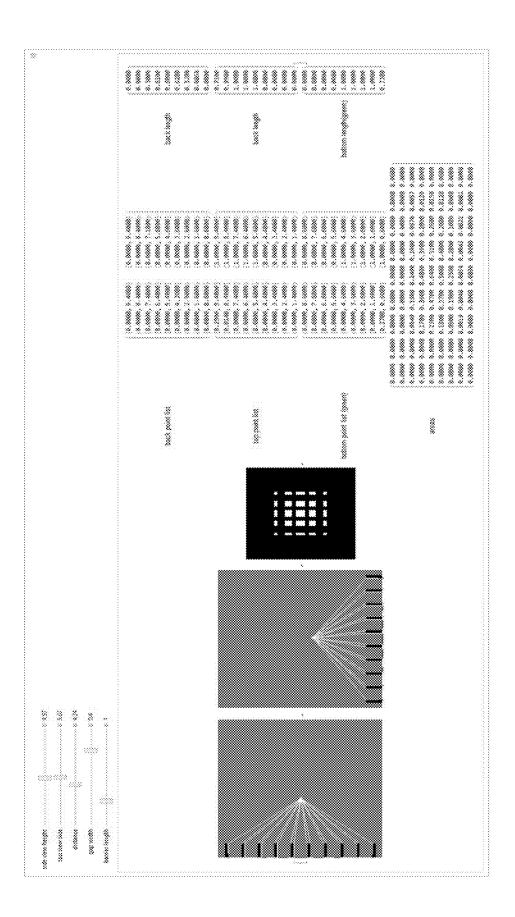
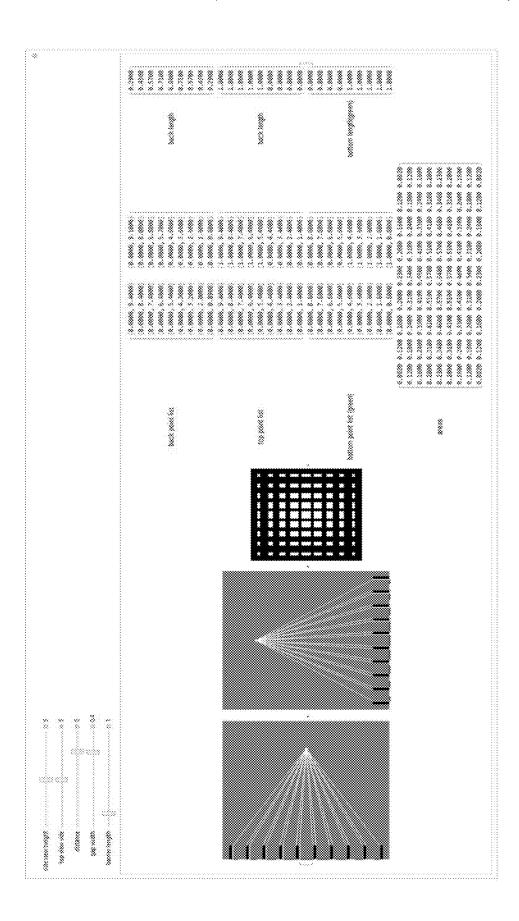
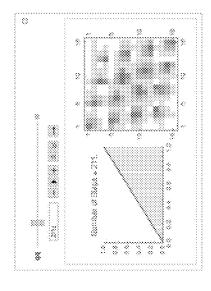
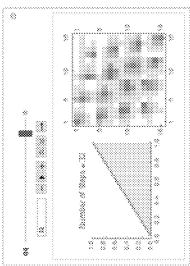


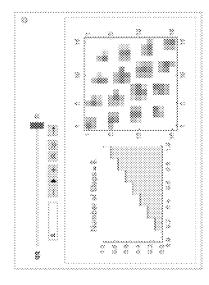
Figure 68t

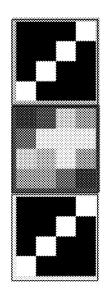


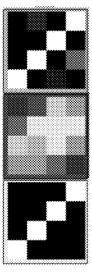












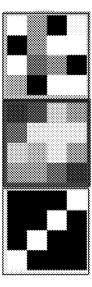


Figure 69a Quantization Control

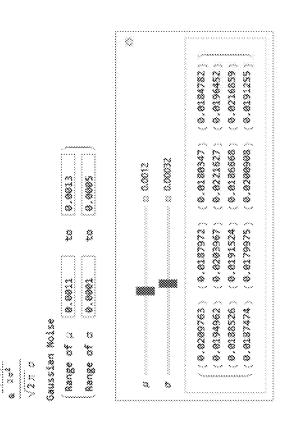


Figure 69c Added Noise Control

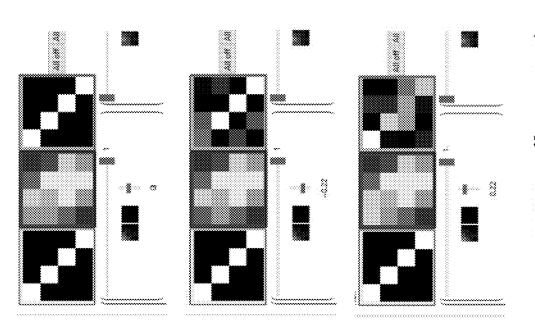


Figure 69b Offset Control

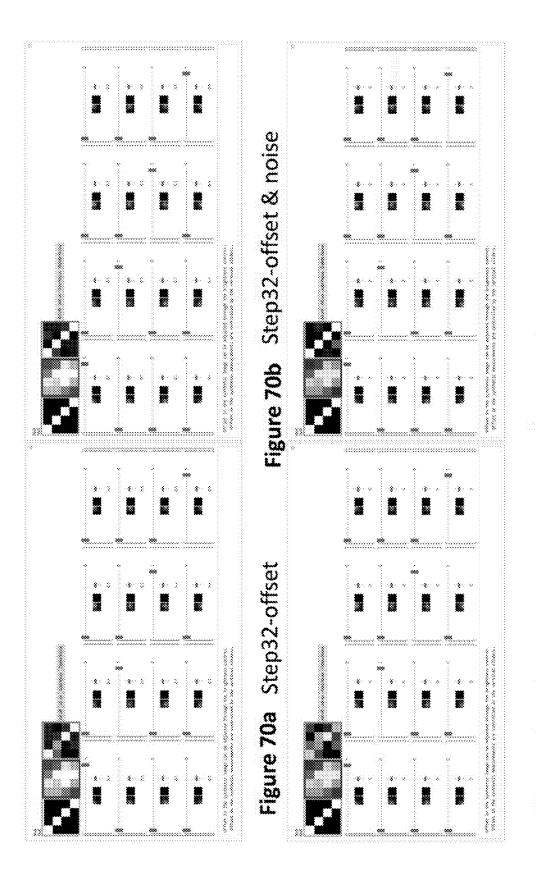
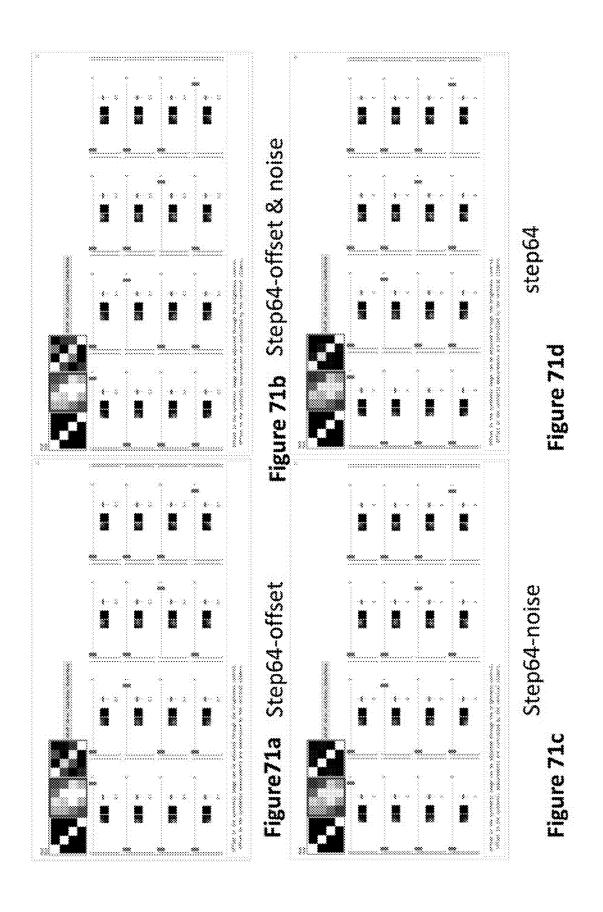
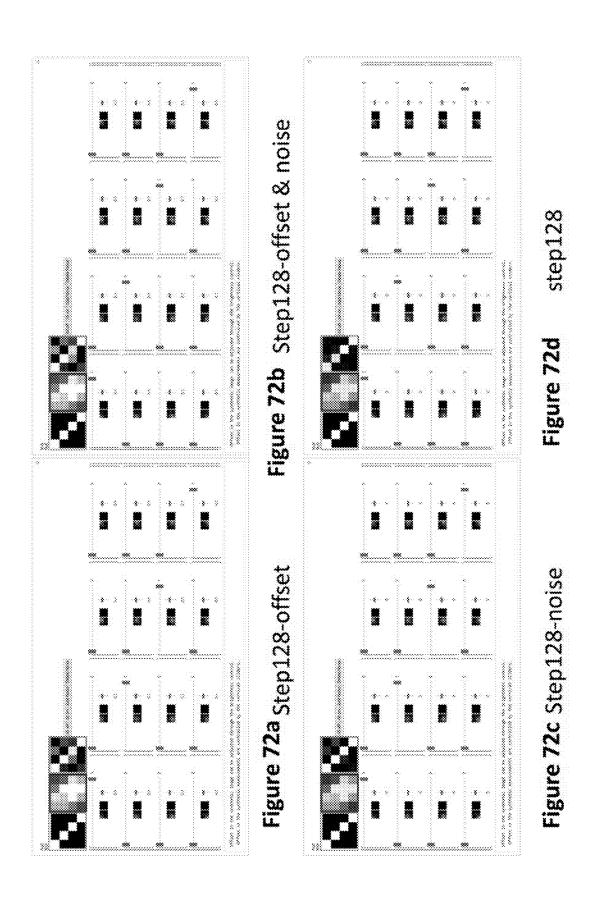
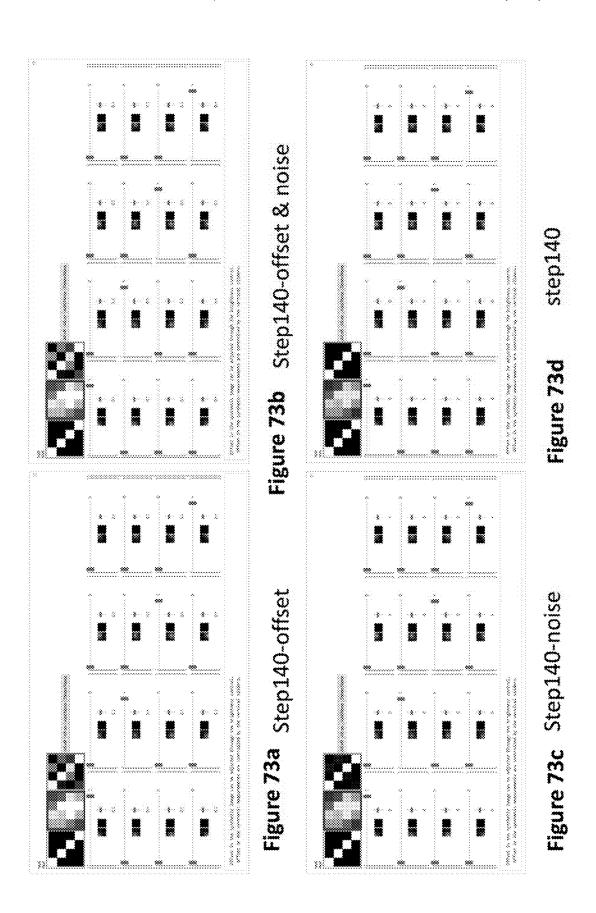


Figure 70c Step32-noise







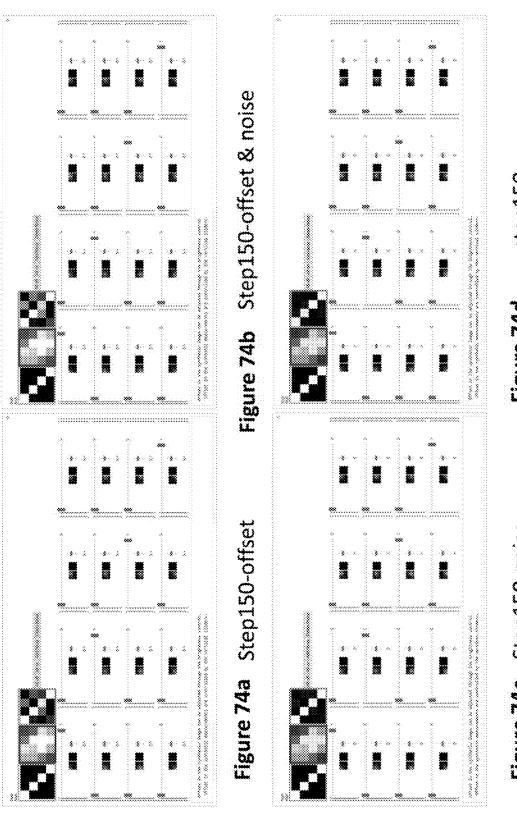


Figure 74c Step150-noise

Figure 74d

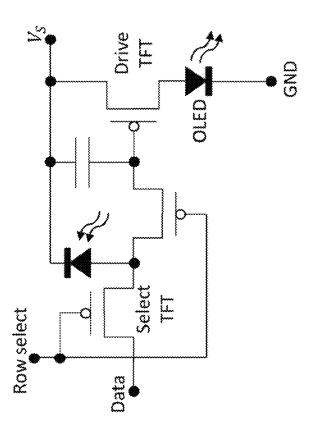


Figure 75b

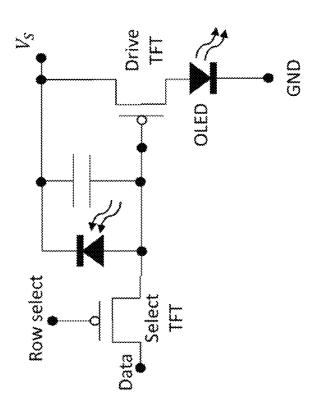


Figure 75a

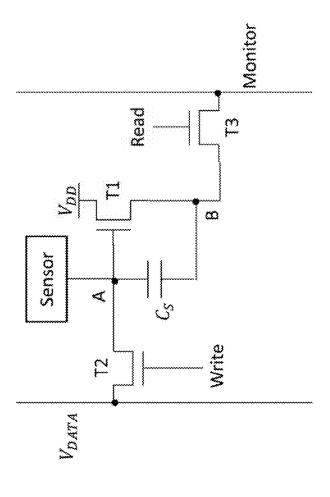


Figure 76b

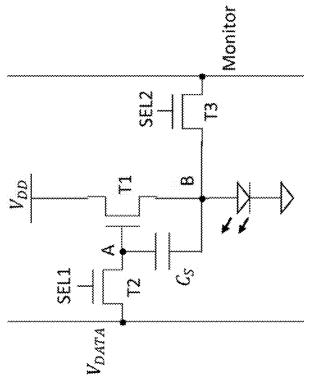


Figure 76a

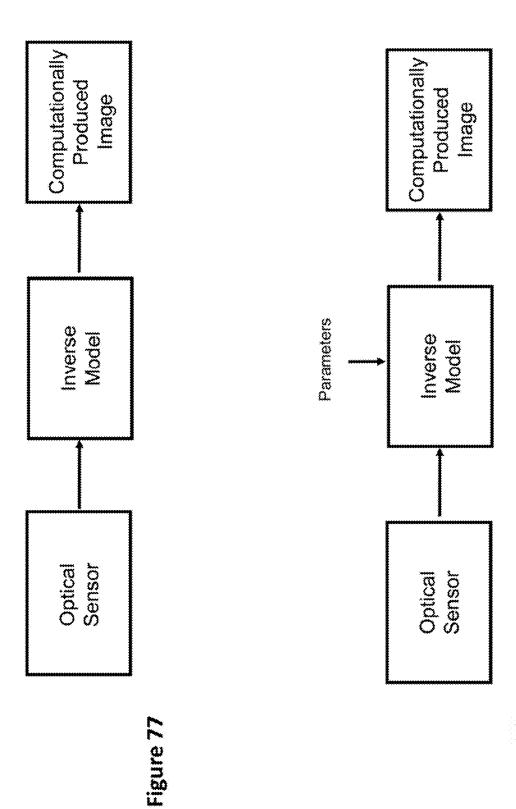
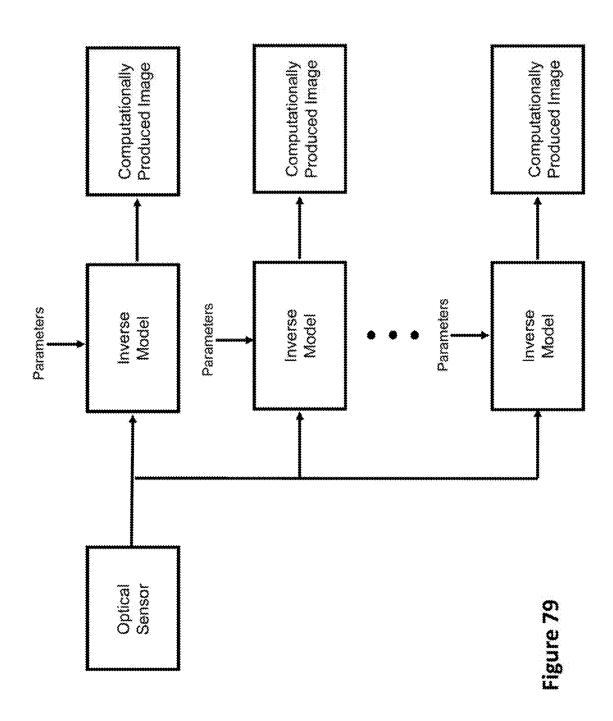


Figure 78



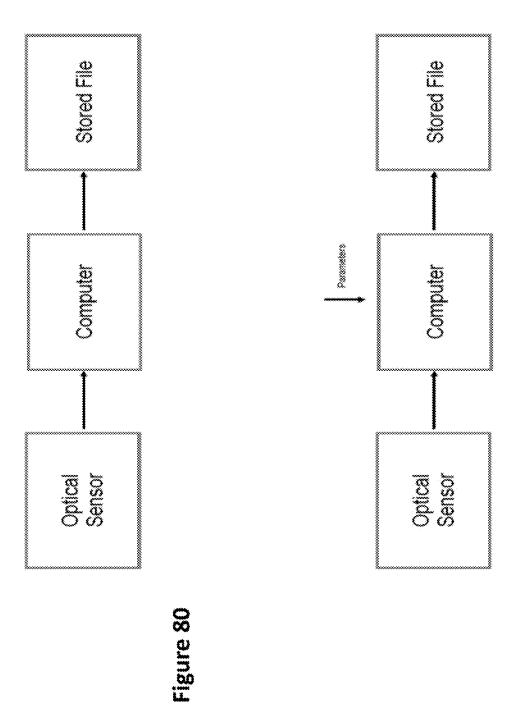
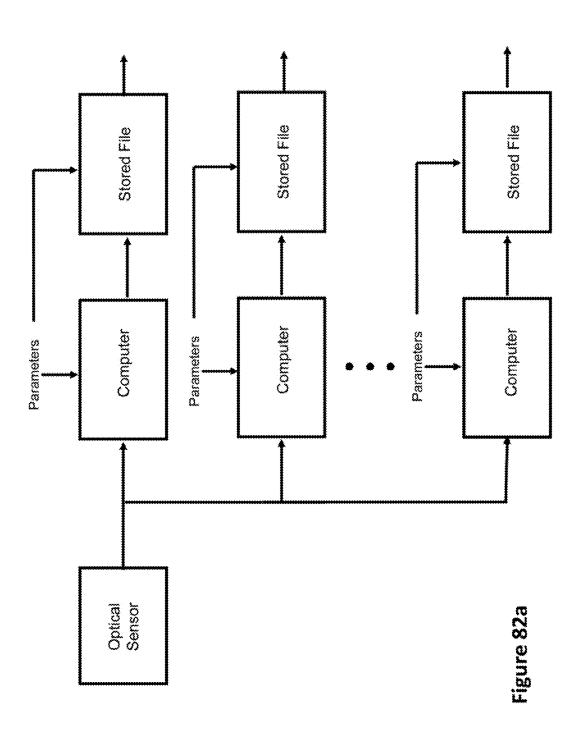


Figure 81



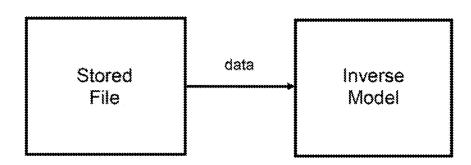


Figure 82b

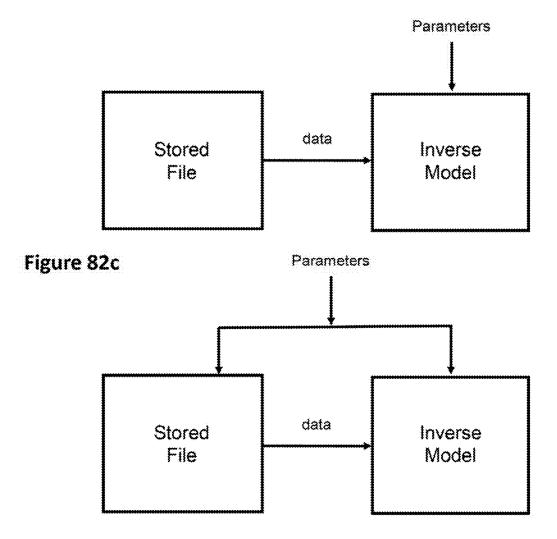
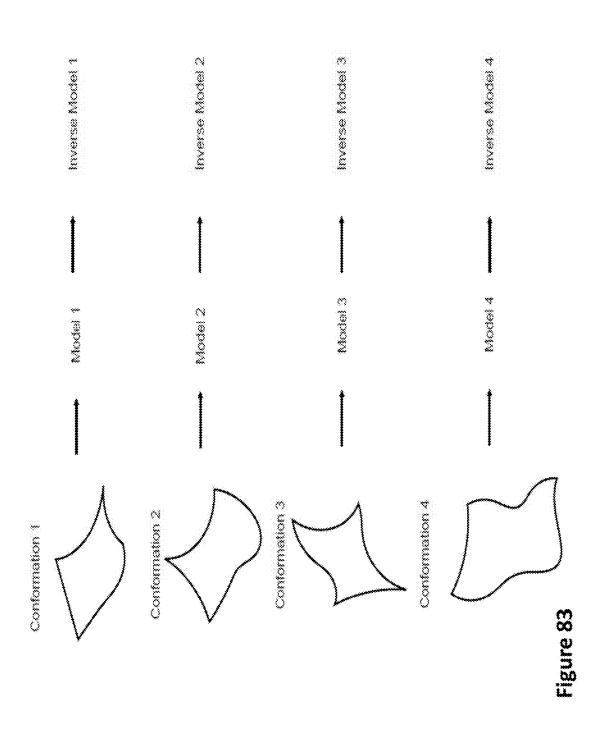
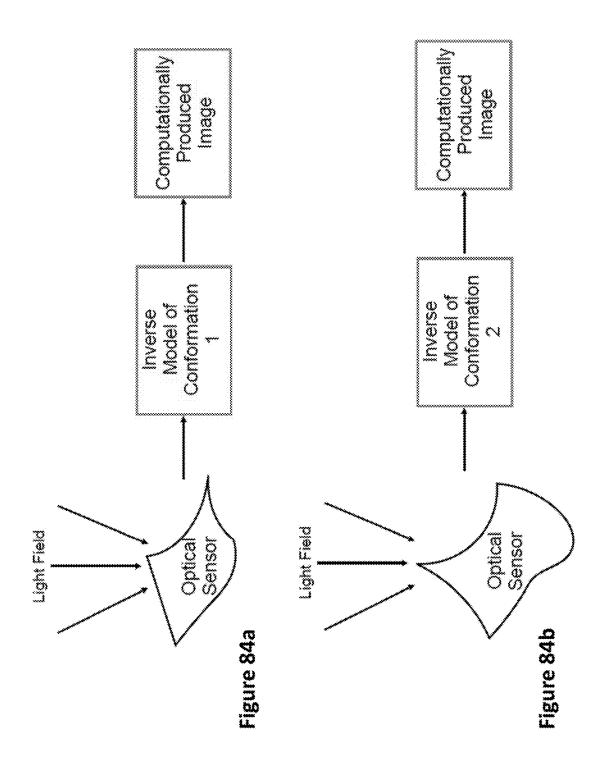
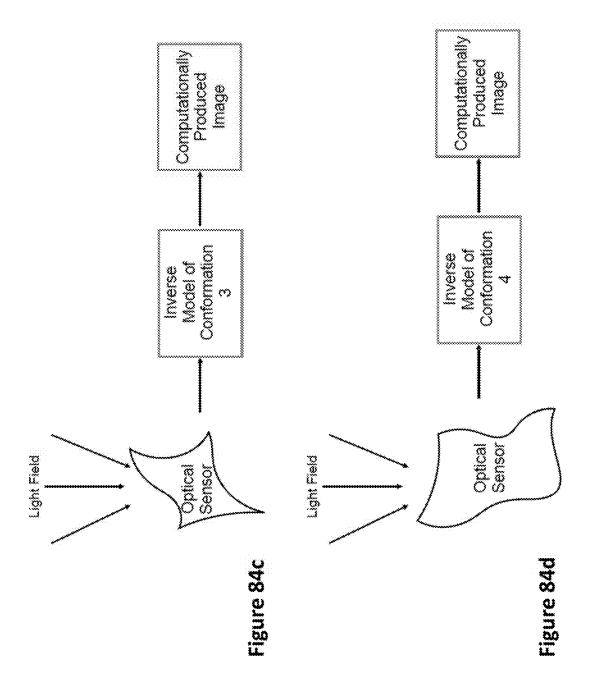
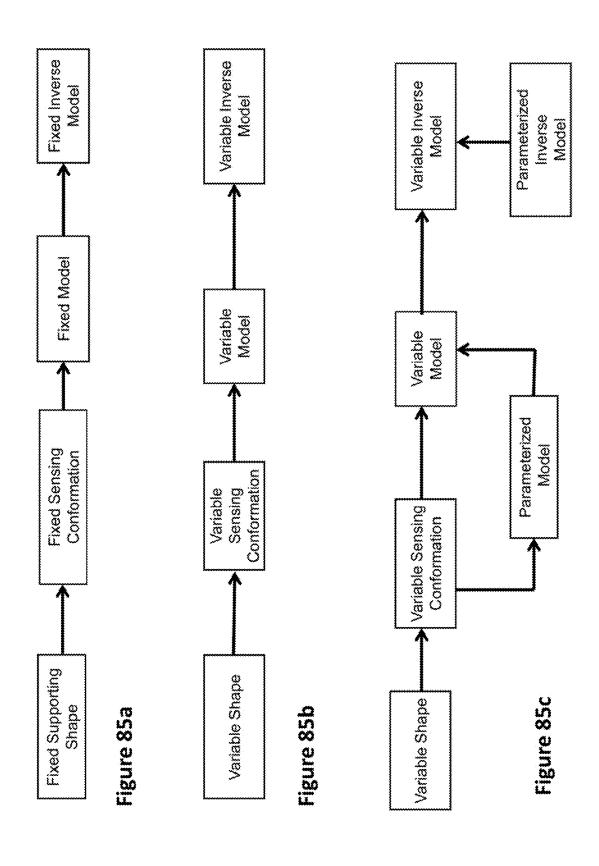


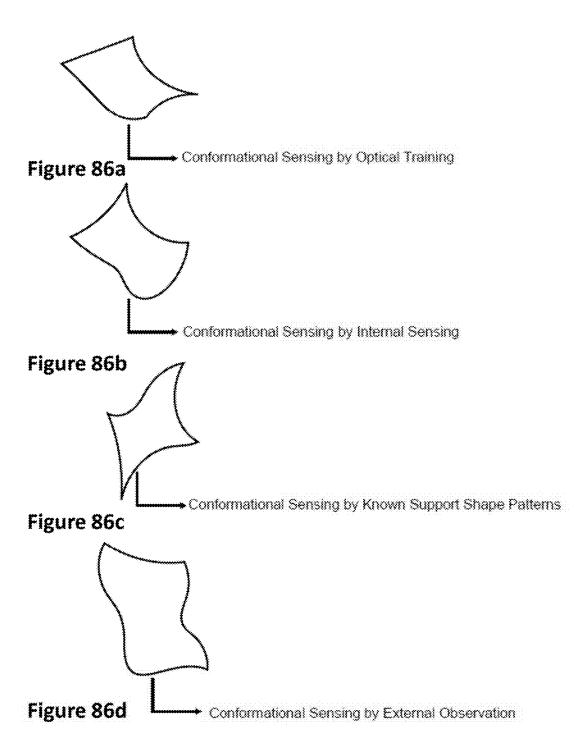
Figure 82d

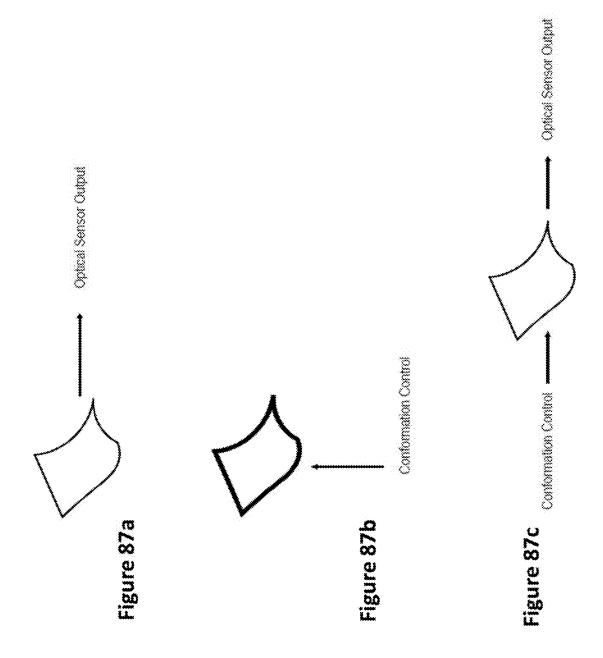












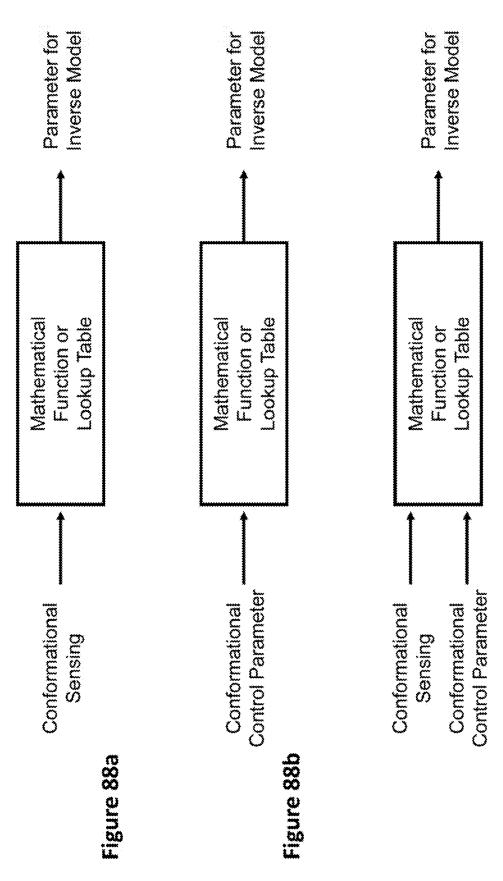


Figure 88c

ADVANCED LENSLESS LIGHT-FIELD IMAGING SYSTEMS FOR ENABLING A WIDE RANGE OF ENTIRELY NEW APPLICATIONS

CROSS REFERENCE TO RELATED APPLICATIONS

The present application is a continuation of U.S. patent application Ser. No. 15/647,230, filed on Jul. 11, 2017, which claims priority to U.S. Provisional Patent App. No. 62/360,472, filed on Jul. 11, 2016, and U.S. Provisional Application No. 62/528,384, filed on Jul. 3, 2017, which are all hereby incorporated herein by reference as if set forth in full.

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BACKGROUND OF THE INVENTION

Field of the Invention

The invention pertains to computational imaging and light-field sensors, and more specifically to lensless camera arrangements leveraging a wide range of curved, polygon, 35 rigid, flexible, elastic, and plastic attributes.

Overview of the Invention

FIG. 1 depicts an example conceptual view of the under- 40 lying principles of the invention, facilitating a wide range of implementation methods and architectures. In this depiction, an Optical Scene creates a Light-Field that is directed to an Optical Sensor which is preceded by one or more Lensless Optical Structure(s) that in some manner alters the light field 45 in a predictable spatial manner. The Optical Sensor produces (typically time-varying) electrical signals and/or computational data responsive (instantly and/or within some timedelay) to light incident to the surface or other substructure(s) within the Optical Sensor at any given moment. The 50 depicted Inverse Model can be configured to, in some appropriate manner, undo the effects of the incoming light's optical travel first within the Light-Field preceding the optical structure(s) and then through the Lensless Optical Structure(s) to where it reaches the Optical Sensor, resulting 55 as well as other past, current, and planned future patent in a computationally-produced image which, for example, can be arranged to be useful for human or machine use.

A family of technologies relating to lensless imaging wherein an (even primitive) light sensing array is configured by (simple or more complex) optical structures to create a 60 light-field sensor and focused images are obtained via numerical computation employing algorithms executed on one or more instances of a computational environment (for example comprising a computer, microprocessor, Graphical Processing Unit (GPU) chip, Digital Signal Processing 65 (DSP) chip, etc.) has been described in earlier patent filings by the present inventor. These include for example:

2

- U.S. Pat. No. 9,172,850 "Lensless imaging camera performing image formation in software employing microoptic elements creating overlap of light from distant sources over multiple photo sensor elements"
- U.S. Pat. No. 9,160,894 "Lensless imaging camera performing image formation in software and employing micro-optic elements that impose light diffractions"
- U.S. Pat. No. 8,830,375 "Vignetted optoelectronic array for use in synthetic image formation via signal processing, lensless cameras, and integrated camera-dis-
- U.S. Pat. No. 8,816,263 "Vignetted planar spatial lightfield sensor and spatial sampling designs for far-field lensless synthetic imaging via signal processing image formation"
- U.S. Pat. No. 8,754,842 "Combined display and image capture without simple or compound lenses for video conferencing eye-contact and other applications"
- U.S. Pat. No. 8,305,480 "Synthetic Image Formation via Signal Processing for Vignetted Optoelectronic Arrays, Lensless Cameras, and Integrated Camera-Displays"
- U.S. Pat. No. 8,284,290 "Synthetic Image Formation Signal Processing Hardware for Vignetted Optoelectronic Arrays, Lensless Cameras, and Integrated Camera-Displays'
- U.S. Pat. No. 8,125,559 "Image Formation for Large Photosensor Array Surfaces"
- U.S. Pat. No. 9,019,237 "Multitouch Parameter And Gesture User Interface Employing an LED-Array Tactile Sensor That Can Also Operate as a Display'
- C.A. 2,318,395 "Multifunction Communication Service Device"
- U.S. Pat. No. 9,632,344 "Use of LED or OLED Array to Implement Integrated Combinations of Touch Screen Tactile, Touch Gesture Sensor, Color Image Display, Hand-Image Gesture Sensor, Document Scanner, Secure Optical Data Exchange, and Fingerprint Processing Capabilities"
- U.S. application Ser. No. 13/547,024 "Use of OLED Displays as a High-Resolution Optical Tactile Sensor for High Dimensional Touchpad (HDTP) User Interfaces"
- Allowed U.S. application Ser. No. 13/072,588 "Color Imaging Using Color LED Array as Light-Field Image Sensor"
- U.S. application Ser. No. 14/333,177 "Vignetted planar spatial light-field sensor and spatial sampling designs for far-field lensless synthetic imaging via signal processing image formation"
- U.S. application Ser. No. 14/478,920 "Vignetted Optoelectronic Array for Use in Synthetic Image Formation via Signal Processing, Lensless Cameras, and Integrated Camera-Displays"
- filings. The approach can also be used to implement lensless microscopy and optical tomography, for example as has been described in earlier patent filings by the inventor, for example including:
 - U.S. Pat. No. 8,885,035 "Electronic imaging flow-microscope for environmental remote sensing, bioreactor process monitoring, and optical microscopic tomography"
- U.S. application Ser. No. 14/105,108 "Small-Profile Lensless Optical Microscopy Imaging and Tomography Instruments and Elements For Low Cost And Integrated Microscopy"

U.S. Pat. No. 9,594,239 "Optical Tomography for Microscopy, Cell Cytometry, Microplate Array Instrumentation, Crystallography, and Other Applications"

U.S. Pat. No. 9,594,019 "Optical Tomography for Microscopy, Cell Cytometry, Microplate Array Instrumenta- 5 tion, Crystallography, and Other Applications"

U.S. application Ser. No. 15/289,815 "Electronic Imaging Flow-Microscope for Environmental Remote Sensing, Bioreactor Process Monitoring, and Optical Microscopic Tomography"

U.S. application Ser. No. 15/457,963 "Cylindrical Optical Tomography for Microscopy, Cell Cytometry, Microplate Array Instrumentation, Crystallography, and Other Applications"

as well as other past, current, and planned future patent 15 filings. Broader uses and additional functions are possible as taught in yet other past and current patent filings as well as other planned and emergent patent filings.

As indicated in the above patent filings, an immense number of capabilities and features result from this 20 approach. For example, although the light sensing array can comprise a CMOS imaging chip, the light sensing array can comprise an array of printed organic-semiconductor photodiodes, including printed Organic Light Emitting Diodes (OLEDs) that are electrically interfaced and/or physically 25 devices, novel physical, optical, electronic and optoelecstructured to operate at least as light sensing (square) "pixel" or (rectangular) "pel" elements; because such a sensing array is fabricated by layered printing of inks (comprising conductive materials, semiconducting materials, and insulating materials, the types inks including transparent types) 30 on arbitrary surfaces (such as glass, rigid plastics, or flexible plastics) that may be flat or curved, the optical sensing array can be rendered in a wide variety of ways, shapes, sizes, curvatures, etc. on a flat, curved, bendable, deformable surface that may also be used for performing other function. 35 Further, the optical structures required to invoke light-field sensing capabilities can be as simple as a crudely formed array of vignetting passages, and these optical structures can be for example printed using light-path impeding inks, an applicable light-field sensor array can be entirely fabricated 40 by printing layers of electrical, structural, and optical inks on flat, curved, bendable, and/or deformable surface that can also be used for performing other structural, electrical, sensing, physically-supporting, physical-boundary, and/or physical-surface functions. It is noted that in addition to 45 tures arranged to be implemented by signal processing printed organic-semiconductor photodiodes and/or OLEDs, the light sensing array can alternatively or additionally comprise one or more of printed organic-semiconductor phototransistors, silicon or other crystal-lattice photodiodes, silicon or other crystal-lattice phototransistors, silicon or 50 other crystal-lattice LEDs, silicon or other crystal-lattice CMOS light sensors, charge-coupled light sensors, printed non-organic semiconductor photodiodes, printed non-organic semiconductor LEDs, printed non-organic semiconductor phototransistors, or other type of electrically-respon- 55 sive light-sensing elements. As described and implied in the above patent materials, and as to be further described and implied throughout the present patent applications, these advanced lensless light-field imaging systems and methods for enabling a wide range of entirely new applications.

These earlier inventor's patent families and the inventor's present patent application individually and collectively (1) employ many independent advancements in material science, organic electronics, and manufacturing processes optoelectronic devices, novel physical, optical, electronic and optoelectronic device configurations and (3) corresponding novel mathematical and signal flow structures arranged to be implemented by signal processing algorithms, and other novel system elements and method steps. The aforementioned independent advancements in material

science, organic electronics, and manufacturing processes include:

Materials, methods, and manufacturing techniques for bendable and flexible active and passive electronic and optoelectronic components and interconnections;

Materials, methods, and manufacturing techniques for printable/printed active and passive electronic and optoelectronic components and interconnections.

Materials, methods, and manufacturing techniques for transparent active and passive electronic and optoelectronic components and interconnections;

Materials, methods, and manufacturing techniques for multiply-layered/stackable active and passive electronic and optoelectronic components and interconnec-

Materials, methods, structures, and manufacturing techniques for implementing and optimizing light-sensing and light-emitting aspects of optoelectronic compo-

Novel adaptations of and structures for optoelectronic tronic device configurations comprised by the inventor's earlier patent families and used in the inventor's present patent application include for example but are not limited to:

Use of diffraction elements, vignetting structures, and other non-micro-optic elements to implement lightfield imaging sensing arrays;

Use of LED or OLED array as both a display and non-contact (spatially-separated) lensless camera;

Use of transparent optoelectronic elements to implement stacked wavelength-selective light-sensing elements analogous to Stacked Organic Light Emitting Diodes (SOLEDs);

Use of bandgap responses to implement color image sensing arrays without the use of filters. diffraction gratings, or other wavelength-selective optical elements:

Curved image sensor arrays;

Bent and flexible image sensor arrays.

Corresponding novel mathematical and signal flow strucalgorithms, and other novel system elements and method steps also configurations comprised by the inventor's earlier patent families and used in the inventor's present patent application include for example but are not limited to:

Image formation signal processing;

Color separation signal processing;

Use of Moore-Penrose pseudo-inverse or other generalized inverses to provide statistical robustness from over-specified measurement data;

Use of Moore-Penrose pseudo-inverse or other generalized inverses to provide spatial robustness (using overspecified measurement data) against damage or occultation of isolated sensor elements or groups of sensor elements:

Use of Graphics Processing Unit ("GPU") for image formation (particularly applicable when camera is integrated with a display sharing the same multiplexing environment).

The inventor's early inventions (as taught in the aforetogether with (2) novel adaptations of and structures for 65 cited patents) and present invention competes favorably with other lensless computational imaging approaches on their own terms in a number of ways, for example:

Significant computational efficiency advantage because no transform domain conversions are required; images are recovered by matrix multiplication of a long vector measurement vector by a pre-computed matrix, facilitating video-rate decoding

Far greater light capture efficiency (incoming light loss can be nearly zero, while coded apertures typically by their very nature invoke a 45%-50% minimum loss of incoming light);

Cost reduction via printing (readily including printed interface electronics);

Can be far thinner;

Can be far larger.

The inventor's early inventions (as taught in the aforecited patents) and present invention provides a number of features not available from other lensless computational imaging approaches, including but not limited to:

No separation distance between the sensor and any vignetting or aperturing array, allowing thinner image 20 sensor;

No need for any vignetting or aperturing array if the photosensing elements natively have adequate angular occultation or angular selectively;

Vignetting or aperturing can be done at the same spatial 25 separation as individual photosensing pixels;

No special frequency domain requirements on any vignetting or aperturing array;

Any vignetting or aperturing array can include internallyreflective structures and have arbitrarily thin walls to 30 preclude light loss;

Any vignetting or aperturing array can be also arranged to facilitate predictable or and/or reproducible surface plasmon propagation to selected light sensors comprised by the light sensor array in a manner that further 35 reduces light loss;

Truly arbitrary image sensor size;

Flat or arbitrarily-curved image sensor shape;

Distributed image sensing;

Angular diversity/redundancy advantage;

Enveloping imaging, contact imaging (including local illumination in contact imaging);

"Seeing skin"—rigid, flexible, deformable, manipulatable;

Integrated in a visual light-emitting display;

Overlay on provided surfaces;

Self-illuminating;

Zero separation distance focus;

Curved-surface contact focus;

Can provide one or more simultaneous computationally- 50 controlled focus (mixed focus);

Can provide one or more simultaneous computationally-controlled viewpoint(s);

Can provide one or more simultaneous computationally-controlled stereo/3D live imaging;

Can provide full-color and enhanced (meta-RGB) color image capture;

Can include IR and UV capabilities;

Can include multiple-wavelength spectroscopic capabilities without diffraction-grading or prism optics;

Can be integrated into a visual display.

FIG. 2 depicts an illustrative representational view of the confluence of the expanded features and capabilities taught in the inventor's 1999 patent family. This depiction and the elements therein are intended as only illustrative and representative and does not provide or suggest a comprehensive or exhaustive listing, structure, or characterization.

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Similarly, FIG. 3 depicts an illustrative representational view of the confluence of the expanded features and capabilities taught in the inventor's 2008 patent family. This depiction and the elements therein are intended as only illustrative and representative and does not provide or suggest a comprehensive or exhaustive listing, structure, or characterization. Additional patent families

A 2008-2009 patent family of the present inventor contributed additional implementations, features, and applications that include use as a display and a touch and touchgesture user interface. A 2010 patent family and 2011 patent family of the present inventor contributed additional implementations, features, and applications that include use not only as a display touch user interface, and touch-gesture user interface but also as a lensless imaging camera, a touch and touch-gesture user interface, free-space hand gesture interface, document scanner, fingerprint sensor, secure information exchange. Although not all of the applications, arrangements, and configurations of those 2008-2009, 2010, and 2011 patent families are explicitly considered in the present patent application, the technologies, systems, and methods described the present patent application are in various ways directly applicable and to the applications, arrangements, and configurations described in those patent families.

A 2009-2010 patent family and a 2013 patent family of the present inventor contributed the addition of optical tomography capabilities employing controlled light sources is also noted in FIG. 3. Although not all of the applications, arrangements, and configurations of those 2009-2010 and 2013 patent families are explicitly considered in the present patent application, the technologies, systems, and methods described the present patent application are in various ways directly applicable and to the applications, arrangements, and configurations described in those patent families.

FIG. 4 depicts an illustrative representational view of the confluence of the expanded features and capabilities associated with the present invention. This depiction and the elements therein are intended as only illustrative and representative and does not provide or suggest a comprehensive or exhaustive listing, structure, or characterization.

Relations to and Developments in Related Technologies

A brief review of the following related concepts and technologies are next provided:

- A. Lensless Coded Aperture Imaging;
- B. Lens-Based Light-Field Imaging;
- C. Use of LEDs as Light Sensors and Light Sensing Arrays;
- D. Flexible Cameras and Transparent Image Sensors;
- E. Transparent Electronics;
- F. Organic Semiconductors and Organic Optoelectronics;
- G. Printed Electronics and Optoelectronics;
- H. Flexible and Bendable electronics;
- I. Flexible and Bendable optoelectronics.

A summarizing functional- and timeline-comparison table is 55 then presented.

A. Relations to Lensless Coded Aperture Imaging

Coded apertures are planar, binary-valued (partially-opaque/partially-transmitting) optical masks gratings, grids, etc. positioned in front of an image sensor array and designed to cast structured shadows that permit mathematical calculations characterizing and permitting the imaging of incoming radiation fields. Originally developed for high-energy photon (x-rays, gamma rays, and other classes of high-energy non-visible wavelength photons) radiation-imaging that cannot be focused by lenses of curved mirrors, the beginnings of coded aperture imaging date back to at least 1968 [P62]. A number of coded aperture telescopes use this

high-energy imaging approach for imaging astronomical X-ray ad gamma ray sources.

Partially predating and later developing in parallel with the inventor's comprehensive lensless light-field imaging program (beginning with the inventor's 1999 patent family) is the related and now recently-popularized (2011-2016) coded-aperture lensless imaging (recently termed a lensless "Computational Renaissance" [P6]). Coded aperture imaging appears to have continued to develop in the exclusive context of high-energy photon non-visible (x-rays, gamma 10 rays, etc.) radiation-imaging for decades but developing a rich mathematical theory (see for example [P31], [P32], [P63], [P64]) relating to the theory of information codes and the relatively "flat" spectral properties of the optical Modulation Transfer Function (discussed in part in various earlier 15 papers but see [P45]) when the coded aperture employs various types of "Uniformly Redundant Array" codes ("URA", "MURA," etc.), variations or alternatives to these, or indeed randomly-generated patterns. At this writing it is not yet clear when attention to these coded aperture imaging 20 approaches were first adapted for use in visible-light imaging, but at this writing it does not appear this was explored or discussed in the literature before 2000. There was some work circa 1973 involving shadow casting and coded masks relating to holography [B8]. Further brief historical treat- 25 ment and reviews of technology developments in coded aperture lensless imaging are provided in [B1], [P5], and [P65].

By 2006 various forms of computer-controlled spatial-light modulators were being used to implement the optical 30 coded aperture function [P34], [P35], [P47], notably using the LCD of an LCD display screen as part of the MIT "BiDi Screen" [P34]. The MIT "BiDi Screen" also featured distance ranging obtained from the coded aperture, described earlier in [P68]. Although the MIT "BiDi Screen" included 35 coded aperture imaging, the images produced were not focused when any non-proximate distance from the screen.

As will be discussed later, most of these systems formulate the image recovery transformation as (1) an ill-posed, usually regularized, inverse problem and/or (2) a spectral-40 method transform problem.

Broader views of computations imaging have subsequently to appear in the literature (see for example [P66]) which migrate the "optical coding" paradigm/abstraction to other contexts, for example wavefront coding, including a 45 lens, sensor-plane coding, etc.). In addition, there have also been several relatively recent systems replacing coded apertures with other types of lensless optical elements:

The 2008 Rice University [P48] and later 2013 Bell Labs [P59], [P32], [P69], [P71], [P72] "single pixel" lensless 50 camera approach uses a computer-controlled aperture or micro-mirror spatial light modulator to sequentially implement a time-multiplexed series of coded aperture images. These approaches can include sub-Nyquist rate "compressive sampling" which can also be applied 55 more broadly than optical sensing; se for example [P60].

The post-2010 lensless imaging work at Cornell, later adopted to create ultraminiature imagers and pre-commercialized by Rambus [P4] (and winning best-paper 60 award at the 2013 SensorComm Conference), replaced the coded aperture with various types of admirable intricate-design spiral-arm diffraction elements whose optical Modulation Transfer Function possesses no spectral zeros (as explicitly anticipated in the inventor's 65 1999 patent family). The resulting diffracted light is measured by a small but conventional CMOS imaging

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sensor. Although the available Rambus papers and presentation slides describe various means of numerical image recovery, inversion by numerical division by the Fourier transform optical Modulation Transfer Function in the Fourier numerical domain has been described as the preferred method in an attended public presentation (again as explicitly taught in the inventor's 1999 patent family). The Rambus system also makes distance range measurements in keeping with similar abilities of coded aperture imaging [P34], [P47]. The spiral-arm diffraction element/CMOS imaging sensor approach was later admirably extended to longer wavelengths through use of a microbolometer to implement a miniature lensless far-field 8-14 µm thermal-wavelength infrared computational imager [P61].

Hitachi announced a lensless light-field imaging camera, targeted for 2018, that employs Moire patterns rather than a coded aperture [P11], [P12], [P13], [P14].

CalTech announced an early-stage computational imaging camera employing phase array methods [P39].

A University of Utah project utilizes a bare commercial CMOS image sensor set a large distance away from a large "low" resolution LED-display, using pixel-by-pixel training sequences (as taught in a 2008 inventor's patent family) and recovering the image as a regularized ill-posed inverse problem [P70].

Although the coded aperture imaging area and the three alternatives described above each have their own "world," it is possible to create an overarching framework that includes all of these. As will be discussed, it is the inventor's view that the inventor's comprehensive lensless light-field imaging program (beginning with the inventor's 1999 patent family) arguably if not straightforwardly includes and provides a framework admitting most of these in at least some sense, as well as including the many other original innovations from the inventor's comprehensive lensless light-field imaging program). For other selective perspectives and far more historical and contextual information see for example [P6], [P66]. From an even broader view, all such approaches can be abstracted into the notion of "computational imaging" from which various fundamental principles can be explored; for example see [P66], [P73].

As to further how the above compare and sequence over time with respect to the inventor's comprehensive lensless light-field imaging program, FIG. 5 depicts a more detailed view of the inventor's comprehensive lensless light-field imaging program (beginning with the inventor's 1999 patent family) and includes recently-popularized coded-aperture lensless imaging. FIG. 6 depicts a functional "timeline" view of lensless imaging, including both the inventor's comprehensive lensless light-field imaging program (beginning with the inventor's 1999 patent family) is and recentlypopularized (2011-2016) coded-aperture lensless imaging stemming from radiation-imaging work dating from 1968 [P62]. Additionally, FIG. 7 includes in its vertical time-line depiction representative literature in lensless imaging with respect to the inventor's comprehensive lensless light-field imaging program.

As an additional note, since the fate of many captured images is to be compressed by image compression algorithms comprising at least some linear transformation operations, the coded aperture could conceptually be modified to impose additional coding functions, in particular those useful in compressing an image suitable for image decompression on the viewing or applications side. This has been shown to be possible and considerable work has been done in this area; see for example.

B. Relations to Lens-Based Light-Field Imaging

A light-field is most generally a 5-dimensional vector function representation of physical arrangement of directional light paths and intensities at each point in a space of optical propagation. The ideas date back to Faraday but was 5 named and formalized in 1936 by Andrey Gershun. That said, the concept of a light field camera dates back to the 1908 "Integral Photograph" work and proposals by Gabriel Lippmann, winner that same year of the Nobel Prize for the invention of color photography (also known for being the predictor of the now widely employed converse piezoelectric effect and inventor of the telescope position compensating coelostat).

A Stanford team including Ren Ng formalized a light-field camera using a ('plenoptic") microlens-array technique 15 [P40], leading not long thereafter to the well-respected Lytro refocusable light-field camera [P41]. Toshiba subsequently announce a 2013 refocusable light-field OEM camera module product [P42] using miniaturized similar technology. Recent (2016) developments in this area implement light- 20 field imaging without the use of microlenses by employing layers of "optical" sensors instead [P43].

The inventor's 1999 patent family taught lensless computational imaging with light-field capabilities and (albeit for color imaging sensing) layered optical sensors. Also, as 25 indicated in the previous subsection, coded aperture image sensors are typically capable of performing as light-field cameras (see for example [P67]).

It is notated notion, description, mathematical treatment, and measurement, of light-fields, and image rendering from 30 them, have other historical and contemporary threads. A 2006 survey of light-field imaging from a simplified 4-dimensional representation computational imaging viewpoint employed in Image Based Rendering (IBR), computergraphics fly-bys and related applications is presented in 35 [P46]. Light-fields (and their analogs in acoustics, seismology, and energy fields) are also in various forms are inherently and thus fundamentally relevant to at least wave-field inversion and wave-field Inverse Source Problems (ISPs), tomography, holography, broader Image Based Rendering 40 (IBR) applications, and 3D graphics rendering; for a 'unified' treatment regarding imaging, wavefield inversion and tomography see for example the book by Devaney [B3]. Additionally there are various other methods for measuring and sampling empirical light-fields; a few examples are 45 described in the book by Zhang and Chen [B4].

Although presented before, FIG. 7 includes in its vertical time-line depiction representative literature in light-field imaging with respect to the inventor's comprehensive lensless light-field imaging program.

C. Use of LEDs as Light Sensors and Light Sensing Arrays A number of earlier U.S. patents and U.S. patent Applications discuss various aspects of using LED and OLED arrays used in various combinations or sequences of light sensing and light-emitting modes and in one manor or 55 time-line depiction representative patents discussed in this another the integration of light sensing and light-emitting semiconductors in a common display panel, control panel, or image reader. Some of these employ time-multiplexed operating modes, some of these spatially interleave light sensing and light-emitting semiconductor elements, but none of 60 these teach use as visual imaging camera.

U.S. Pat. No. 4,424,524 by Daniele (filed 1982) teaches a linear array of LEDs that selectively function as light emitters and light sensors for line-scanning a document on a rotating drum. No image display is involved.

U.S. Pat. No. 4,692,739 by Dorn teaches use of LEDs to form user operator panel control elements used both for 10

receiving data from an operator to change the logic state of a device and for displaying the entered data back to the operator; current is selectively applied to an LED to display the data and alternately a photo-current produced by the LED is sensed by detecting the fall-off in the photo-current caused by the operator covering the light-emitting diode. No image display or capture is

U.S. Pat. No. 5,424,855 by Nakamura teaches an array of LEDs controlled so as to emit light in a write mode and sense light in a read mode wherein each LED is alternately charged for a first interval, then allowed to discharge by flow of photocurrent for a second interval.

U.S. Pat. No. 5,929,845 by Wei teaches OLED array with individual OLEDs multiplexed between emitting and sensing modes (see text portion of the document, column 2 lines 4-17, and the preceding paragraph spanning columns 1 and 2).

U.S. Pat. No. 7,598,949 by Han teaches an "optical touch sensor" using LED-array as real-time photodiodes and co-integrated light-emitters. In the "preferred embodiment" he uses an array of discrete RGB LEDs, using (higher-energy/shorter-wavelength) blue LED elements for light emission and red LED elements as photodiodes (rather than time-multiplexing between emitting and sensing modes), and alludes OLEDs and printable manufacturing methods. A video demonstration (12 MB; viewable with MS Media Player and other populate viewers) is downloadable from http://mrl.nyu.edu/~jhan/ledtouch/index.html (visited Jul. 3, 2017).

U.S. Pat. No. 7,859,526 by Konicek teaches an LED array with individual LEDs multiplexed between emitting and sensing modes.

U.S. Pat. No. 8,026,879 by Booth teaches a somewhat different "optical touch sensor" and provides discussion of OLEDs as light-emitter and light-sensors (see abstract) but different use of photosensing.

U.S. Pat. No. 8,890,850 by Chung also teaches a related "optical touch sensor" and provides discussion of OLEDs as light-emitter and light-sensors; in particular note FIGS. 4-6.

Abandoned U.S. Patent Application 2009/0256810 by Pasquariello teaches a related "optical touch sensor" and provides some discussion of multiplexing LEDs between emitting and sensing modes.

These U.S. patents discuss possible applications as camera but do not teach image formation:

The series U.S. patents by Rostoker including U.S. Pat. Nos. 5,340,978, 5,519,205, 5,529,936, 5,734,155, 5,760,834, and 5,811,320.

U.S. Pat. No. 7,535,468 by Uy;

U.S. Pat. No. 6,787,810 by Choi et al.

Although presented before, FIG. 7 includes in its vertical section with respect to the inventor's comprehensive lensless light-field imaging program.

D. Flexible Cameras and Transparent Image Sensors

The limited work that has been done regarding flexible cameras has been largely in the enabling optics area. Many points regarding the value, radical enablement, and some applications of flexible cameras have been provided in papers and press releases stemming from projects at Columbia University [P37], [P38] involving work on bendable and deformable mini-lens arrays, elastic optics, and associated internal optical compensational adaptation for those. These efforts appeal for the need for the development of flexible

image sensors; the prototyping work employs traditional (color) camera sensors and camera lenses.

Another approach to flexible cameras, as well as flexible image sensors and transparent image sensors, involves grid of flexible light-sensing fibers that direct light to remotely- 5 located conventional camera element [P53].

Another third approach to flexible cameras, as well as flexible image sensors and transparent image sensors, underway in Austria [P28] also is directed to enabling optics; this effort uses novel optics and luminescent concentrator thin 10 transparent film to gather light from an area of a transparent bendable surface and direct it to the edges of the transparent bendable surface where it is provided to photodiode arrays at those edges. The images are monochrome. As to flexible image sensors, a flexible large-area photodetector array arranged as an image sensor employing organic photodiodes (discussed below) has been reported in 2008 [P54] where image-sensing capabilities have been demonstrated by projecting an image using external image projection equipment. More recently, IMEC has made several pre-commercializa- 20 tion developments announced in 2013 [P55] that overlap with the inventor's patents filed many years earlier.

Although presented before, FIG. 7 includes in its vertical time-line depiction representative literature in flexible cameras with respect to the inventor's comprehensive lensless 25 light-field imaging program.

E. Transparent Electronics

Developments in transparent electronics arguably began in earnest with the discoveries, adaptations, and refinements of transparent conductor materials (see for example [P56]. 30 Various transparent passive electronic components were subsequently developed and are important, but a key development was the invention of the first transparent thin-film transistor (TTFT) announced in 2003 ([B16] p. 1). TTFTs are presently widely used in display technology and can be 35 fabricated by various means, including spin-deposition and printing using ink-jet or other printing methods. Information on transparent electronic materials can be found in the book by Wagner, Keszler, and Presley [B16] (see Chapter 4) as well as information on transparent resistors ([B16] section 40 5.2.1), transparent capacitors ([B16] sections 5.2.2 and 5.3.4), transparent inductors ([B16] section 5.2.3), transparent PN diodes ([B16] section 5.3.1), transparent MIS (Metal-Insulator-Semiconductor diodes ([B16] section 5.3.1), and transparent thin-film transistors (TTFT) ([B16] 45 section 5.4). Additional information and applications are provided, for example, in the book by Facchetti and Marks [B17].

F. Organic Semiconductors and Organic Optoelectronics

Closely related with the areas of transparent electronics, 50 printed electronics and flexible electronics is the area of organic semiconductors and organic optoelectronics. Organic semiconductor materials facilitate many aspects of transparent electronics, printed electronics and flexible electronics, for example (a) replacing the band gap employed in 55 traditional crystalline semiconductors with the energy band transition between highest-occupied molecular orbitals and lowest-unoccupied molecular orbitals and (b) replacing the crystal lattice structure of traditional crystalline semiconductors with the structures of polymers. There are many 60 other aspects of organic semiconductors besides these. An introductory discussion of organic semiconductor materials is provided for example in Chapter 2 of the 2004 book by Gamota, Brazis, Kalyanasundaram, and Zhang [B22] and other perspectives of organic semiconductor are provided in 65 the 2013 book edited by Cantatore [B23], although dozens of suitable and more contemporary books and journal pub12

lications abound. One of many important aspects is that organic semiconductor materials can facilitating the use of solution-based ("ink") printing fabrication (see for example [B24]) and other techniques applicable to deposit on curved surfaces and large area surfaces and which facilitate flexible/bendable active electronics. Other important aspects of organic semiconductor materials include transparent capabilities and incorporation of a wide range of new optoelectronic capabilities.

A major commercial and technology aspect of organic electronics resulted from the development of an organic optoelectronic element known as the Organic Light Emitting Diode (OLED). Attributions are made that the OLED was discovered at Kodak when researching solar cells (see for example [B20] section 3.3) and Kodak was a leader in this area for many subsequent years. Combining with thin-film transistors, active-matrix OLED-array displays became commercially available and were used in mobile phones. Early active-matrix OLED-array displays suffered from various problems and limitations, but the underlying materials, devices, system designs, and manufacturing techniques are yielding constraint improvement, and every year or so new major products appear or announced. One example is the curved-screen OLED television sets, and the used of another generation of OLED displays have been announced for forthcoming new mass-market mobile phone products. Flexible OLED displays have been repeatedly demonstrated at the annual Consumer Electronics Shows for many consecutive years, and as will be considered again later, a bendable OLED display was included in a product-concept panoramic camera [P36]. Also as will be discussed later, transparent active-matrix OLED-array displays and transparent OLED-array pixel-addressing circuits using transparent thin-film transistors (TTFTs) and transparent capacitors, and transparent conductors have been developed (see for example [B16] section 6.3.5; [B17] Chapter 12; [B18]; [B19] section 8.2; [B23] Chapter 3.

OLED-array displays can be fabricated by printing (for example using semiconducting, conducting, insulative, and resistive inks) or non-printed methods; non-as discussion of non-printed fabrication methods can be found in [B19] chapter 3, sections 6.1 and section 6.3). Developments in materials and fabrication techniques also create extension to size (including use of OLED-array tiling; see for example [B19] section 8.3), and degrees of curvature (for example a dome-shaped OLED display [P10]. Flat panel imager addressing circuits employing thin-film transistors and PIN or MIS light sensors are also known; see for example [B18] sections 1.2, 2.2.1, 3.1, 3.2, 5.2, 6.1, and 6.2.

Attention is now is directed towards organic photodiodes. Organic photodiodes are widely viewed as providing an enabling route to new devices and new applications that were previously impossible and likely to remain outside the reach of conventional semiconductors. Although there remains great devoted favoritism in the image sensor community for crystalline semiconductor photodiodes monolithically-integrated with CMOS electronics (drawing on belief structures and early performance metrics), organic photodiodes are rapidly gaining immense validation and radically expanding interest. As stated in the opening of [P22]: "Powerful, inexpensive and even flexible when they need to be, organic photodiodes are a promising alternative to silicon-based photodetectors." More detail as to this is provided in the summarizing remarks in the opening of [P2] "Organic photodiodes (OPDs) are now being investigated for existing imaging technologies, as their properties make them interesting candidates for these applications. OPDs

offer cheaper processing methods, devices that are light, flexible and compatible with large (or small) areas, and the ability to tune the photophysical and optoelectronic properties—both at a material and device level . . . with their performance now reaching the point that they are beginning 5 to rival their inorganic counterparts in a number of performance criteria including the linear dynamic range, detectivity, and color selectivity." Additional important points are made in the opening remarks of [P17]: "There are growing opportunities and demands for image sensors that produce 10 higher-resolution images, even in low-light conditions. Increasing the light input areas through 3D architecture within the same pixel size can be an effective solution to address this issue. Organic photodiodes (OPDs) that possess wavelength selectivity can allow for advancements in this 15 regard. Further important remarks are provided in the opening words of [P30]: "Organic semiconductors hold the promise for large-area, low-cost image sensors and monolithically integrated photonic microsystems, published structures of organic photodiodes offer high external quantum 20 efficiencies (EQE) of up to 76% . . . we report on organic photodiodes with state-of-the-art EQE of 70% at 0 V bias, an on/off current ratio of 106 . . . , dark current densities below 10 nA/cm2..., and a lifetime of at least 3000 h..." Other general discussion of organic photodiodes can be found in 25 many references, for example [B21], [P21], [P27].

Like OLEDs and often using essentially the same materials, organic photodiodes can readily be transparent [P20] or semitransparent [P19], fabricated via printing (see for example [P15], [P74]), and flexible (see for example [P2], 30 [P54]). They can deliver high-sensitivity (see for example [P30], [P74]), overall high-performance (see for example [P2], [P17], [P19], [P22], [P30]). They can also include avalanche and photomultiplication (see for example [P18]). Additionally, like crystalline semiconductor LEDs when 35 used as light sensors, and have been affirmed to provide wavelength selective light-sensing properties (see for example [P2], [P17], [P18], [P19], [P22], [P55]) that forgo the need for optical filters (as pointed out years many prior in several of the inventor's patents) in, for example, color 40 imaging.

Many efforts have been directed towards combining OLED arrays with various types of photosensors to create sensors for biomedical applications. Many of these combine OLED with silicon-based photodetectors (see for example 45 [P16], [P23]), but there have been recent efforts involving combining OLEDs with organic photodiodes (see for example [P7], [P8], [P9]). As to the enabling value of such integrations, [P23] states "Point-of-care molecular diagnostics can provide efficient and cost-effective medical care, and 50 they have the potential to fundamentally change our approach to global health. However, most existing approaches are not scalable to include multiple biomarkers. As a solution, we have combined commercial flat panel OLED display technology with protein microarray technol- 55 ogy to enable high-density fluorescent, programmable, multiplexed biorecognition in a compact and disposable configuration with clinical-level sensitivity."

As with crystalline semiconductor photosensors, increased performance for some applications can often be 60 obtained by creating photo-sensitive transistors which, in effect, replace an electrically-responsive controlling input of a transistor with light-responsive controlling input. Accordingly, there is active work in the area of organic phototransistors and organic phototransistor arrays (see for example 65 [P25], [P27]), including for envisioned use as image detectors [P29]. Like organic photodiodes, organic phototransis-

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tors can also be wavelength selective (see for example [P24],[P26]), high performance (see for example [P24], [P25], [P26], [P29]), and flexible (see for example [P25], [P57]).

In addition to the aforedescribed transparent organic photodiode, transparent organic phototransistor and active matrix interface circuits for them, transparent charge-coupled devices are also known (see for example [B16] section 6.3.6).

G. Printed Electronics and Optoelectronics

Printed electronics and optoelectronics have already been mentioned through many of the above sections. Information regarding general materials for printed electronics can be found in a number of publications, for example [B17] p. 154, [B24], [B25], and [B26]. Organic semiconductor materials suitable for printing can be found in a number of publications, for example ([B22] Chapter 2). Printed electronics manufacturing processes can be found in a number of publications, for example [B22] Chapter 3. OLED-array display printed fabrication is discussed in, for example, [B19] section 6.2. Printed Organic Photodiodes are discussed in, for example, featuring high-performance [P74] and commercial availability [P15]. The important prospects for printable CMOS circuitry are discussed for example in [B16] p. 44; [B23] p. 124, and [P58].

H. Flexible and Bendable Electronics

Flexible and bendable electronics have already been mentioned through many of the above sections. Information regarding general materials for printed electronics can be found in a number of publications (see for example [B27], [B28], [B29], [B31], [B32], [P51]). General applications are discussed in [B27], [B28], [B29], and large area applications are discussed in [B30]. Fabrication by printing methods are discussed in many references (see for example [P51], [P52]), and performance improvements are frequently announced (see for example [P50]). The expected wide-acceptance of flexible electronics has been discussed in [P49]. The IOP-science multidisciplinary journal Flexible and Printed ElectronicsTM publishes cutting edge research across all aspects of printed, plastic, flexible, stretchable, and conformable electronics.

I. Flexible and Bendable Optoelectronics

Flexible and bendable electronics have already been mentioned through many of the above sections. Information regarding general materials for printed electronics can be found in a number of publications (see for example [B26]). Flexible TFTs for flexible OLED displays are discussed in for example [B19] section 8.1 and [P75]. High performance flexible organic photodiode arrays are discussed in for example [P54] and [P75]. High performance flexible organic phototransistors arrays are discussed in [P25]. Large-area flexible organic photodiodes sheet image scanners are discussed in [P75]. A prototype for a commercial (panoramic camera) product employing a flexible OLED display, (c) conformation deformation sensing is described in [P36]. Although not using flexible optoelectonics, the related work on transparent, flexible, scalable and disposable image sensors using thin film luminescent concentrators is presented in [P28].

J. Summarizing Functional- and Timeline-Comparison Table

Although presented earlier, FIG. 5 depicts a summarizing functional view of the inventor's comprehensive lensless light-field imaging program (beginning with the inventor's 1999 patent family), and FIG. 7 depicts a comparative

timeline table of representative patents and literature with respect to the inventor's comprehensive lensless light-field imaging program.

SUMMARY OF THE INVENTION

For purposes of summarizing, certain aspects, advantages, and novel features are described herein. Not all such advantages can be achieved in accordance with any one particular embodiment. Thus, the disclosed subject matter can be embodied or carried out in a manner that achieves or optimizes one advantage or group of advantages without achieving all advantages as taught or suggested herein.

The invention provides for a rigid or flexible surface to be configured to implement a lensless light-field sensor, producing electrical signals that can be used in real time, or stored and later retrieved, and provided to a computational inverse model algorithm executing on computational hardware comprising one or more computing elements so as to 20 implement a lensless light-field camera.

In another aspect of the invention, a rigid surface is configured to additionally function as a housing and thus operate as a "seeing housing".

In another aspect of the invention, a rigid surface is 25 configured to additionally function as a protective plate and thus operate as a "seeing armor".

In another aspect of the invention, a rigid surface is configured to additionally function as an attachable tile and thus operate as a "seeing tile".

In another aspect of the invention, a rigid surface is configured to additionally function as an attachable film and thus operate as a "seeing film".

In another aspect of the invention, a flexible surface is configured to additionally function as an attachable film and 35 material. thus operate as a "seeing film".

In another aspect of the invention, a flexible surface is configured to additionally function as a garment and thus operate as a "seeing garment".

In another aspect of the invention, a flexible surface is 40 configured to additionally function as a shroud and thus operate as a "seeing shroud".

In another aspect of the invention, a flexible surface is configured to additionally function as an enveloping skin and thus operate as a "seeing skin".

In another aspect of the invention, the rigid or flexible surface is small in size.

In another aspect of the invention, the rigid or flexible surface is large in size.

surface is flat.

In another aspect of the invention, the rigid or flexible surface is curved.

In another aspect of the invention, the rigid or flexible surface is rendered as a polytope.

In another aspect of the invention, the rigid or flexible surface is rendered as a dome.

In another aspect of the invention, the rigid or flexible surface is rendered as a part of a sphere.

In another aspect of the invention, the rigid or flexible 60 surface is rendered as a part of a spheroid.

In another aspect of the invention, the rigid or flexible surface is rendered as a sphere.

In another aspect of the invention, the rigid or flexible surface is rendered as a spheroid.

In another aspect of the invention, the rigid or flexible surface is transparent.

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In another aspect of the invention, the rigid or flexible surface is translucent.

In another aspect of the invention, the rigid or flexible surface is opaque.

In another aspect of the invention, the rigid or flexible surface performs contact sensing.

In another aspect of the invention, the rigid or flexible surface is configured to perform contact image sensing with near-zero separation distance.

In another aspect of the invention, the rigid or flexible surface is configured to perform contact image sensing with zero separation distance.

In another aspect of the invention, the rigid or flexible surface performs distributed optical imaging.

In another aspect of the invention, the rigid or flexible surface performs distributed optical sensing.

In another aspect of the invention, the rigid or flexible surface performs image sensing of ultraviolet light.

In another aspect of the invention, the rigid or flexible surface performs image sensing of infrared light.

In another aspect of the invention, the rigid or flexible surface performs image sensing of selected ranges of visible color light.

In another aspect of the invention, the rigid or flexible surface performs imaging.

In another aspect of the invention, the rigid or flexible surface performs distributed chemical sensing employing optical chemical sensing properties of at least one material.

In another aspect of the invention, the rigid or flexible surface performs distributed radiation sensing employing optical radiation sensing properties of at least one material.

In another aspect of the invention, the rigid or flexible surface performs distributed magnetic field sensing employing optical magnetic field sensing properties of at least one

In another aspect of the invention, the rigid or flexible surface is configured to emit light.

In another aspect of the invention, the rigid or flexible surface is configured to operate as a light-emitting display.

In another aspect of the invention, the rigid or flexible surface is configured to operate as a selectively self-illuminating contact imaging sensor.

In another aspect of the invention, the computational inverse model algorithm is configured to provide variable 45 focusing.

In another aspect of the invention, the computational inverse model algorithm is configured to mixed depth-offield focusing.

In another aspect of the invention, the computational In another aspect of the invention, the rigid or flexible 50 inverse model algorithm is configured to implement a viewpoint with a controllable location.

In another aspect of the invention, the computational inverse model algorithm is configured to implement a plurality of viewpoints, each viewpoint having a separately 55 controllable location.

In another aspect of the invention, the computational inverse model algorithm is configured to provide pairs of outputs so as to function as a stereoscopic camera.

In another aspect of the invention, the computational inverse model algorithm is configured to capture a panoramic view.

In another aspect of the invention, the computational inverse model algorithm is configured to capture a 360degree view.

In another aspect of the invention, the computational inverse model algorithm is configured to capture a partial spherical view.

In another aspect of the invention, the computational inverse model algorithm is configured to capture a full spherical view.

In another aspect of the invention, the rigid or flexible surface is configured to perform enveloping image sensing with near-zero separation distance.

In another aspect of the invention, the rigid or flexible surface is configured to perform contact enveloping sensing with zero separation distance.

In another aspect of the invention, the rigid or flexible surface is configured to operate as a selectively self-illuminating enveloping imaging sensor.

In another aspect of the invention, the computational inverse model algorithm is configured to operate at slow15 comprises multiplexing electronics.

In another aspect of the invention, the computational inverse model algorithm is configured to operate at conventional video rates.

In another aspect of the invention, the computational 20 inverse model algorithm and computational hardware is configured to operate at high-speed video rates.

In another aspect of the invention, a lensless light-field imaging system comprising

An array of light sensing elements, each light-sensing 25 element comprising a light-sensing area and configured to generate an electrical photocurrent responsive to the amplitude of incoming light striking the light-sensing surface, each light-sensing surface arranged to experience angularly-varying sensitivity responsive to the 30 direction of each path of incoming light striking the light-sensing surface,

First electronics for interfacing the array of light sensing elements, the electronics configured to provide a plurality of voltage levels, each voltage level responsive to 35 a specific light-sensing element in the array of light sensing elements,

Second electronics for converting each of the plurality of voltage levels into a corresponding electronically-reprality of electronically-represented digital numbers,

An algorithm for executing on a computational processor, the algorithm for computing a two-dimensional image representation from plurality of electronically-repre- 45 sented digital numbers, the two-dimensional image representation corresponding to portion of a focused image at a particular separation distance value measured perpendicular to the light-sensing surface of a particular light sensing element in the array of light 50 sensing elements, there being a plurality of separation distance values,

Wherein each of the digital numbers are responsive to the amplitude of incoming light striking the light-sensing surface of a unique associated light sensing element in 55 the array of light sensing elements and a plurality of focused image portions, and

Wherein the plurality of separation distance values are not appreciably the same numeric value.

In another aspect of the invention, the light sensing 60 elements of the array of light sensing elements are oriented in space to form a curved surface.

In another aspect of the invention, spatial positions of the plurality of focused image portions form a planar surface.

In another aspect of the invention, the light sensing 65 elements of the array of light sensing elements are oriented in space to form a planar surface.

In another aspect of the invention, the spatial positions of the plurality of focused image portions form a curved surface.

In another aspect of the invention, the light sensing elements of the array of light sensing elements are oriented in space to form a curved surface and the spatial positions of the plurality of focused image portions form a curved surface.

In another aspect of the invention, the algorithm is controlled by a at least one separation distance parameter.

In another aspect of the invention, the algorithm is controlled by a plurality of localized separation distance param-

In another aspect of the invention, the first electronics

In another aspect of the invention, the first electronics comprises at least one transimpedance amplifier circuit.

In another aspect of the invention, the light sensing elements comprise organic photodiodes.

In another aspect of the invention, the light sensing elements comprise organic light emitting diodes.

In another aspect of the invention, the light sensing elements comprise organic diodes that are co-optimized for both light emission and light sensing.

In another aspect of the invention, the light sensing elements are arranged to emit light for some interval of time.

In another aspect of the invention, the light sensing elements are arranged to emit light for some interval of time under the control of the first electronics.

In another aspect of the invention, the angularly-varying sensitivity of the light sensing elements results at least in part from the structure of the light sensing elements.

In another aspect of the invention, the angularly-varying sensitivity of the light sensing elements results at least in part from a structure attached to the array of light sensing

In another aspect of the invention, the array of light sensing elements is fabricated by a printing process.

In another aspect of the invention, the structure attached resented digital number, the result comprising a plu- 40 to the array of light sensing elements is fabricated by a printing process.

> In another aspect of the invention, the structure attached to the array of light sensing elements comprises segregated optical paths.

In another aspect of the invention, the segregated optical paths are created by separating surfaces.

In another aspect of the invention, the separating surfaces are at least partially-reflective.

In another aspect of the invention, the separating surfaces are configured to facilitate surface plasmon propagation.

In another aspect of the invention, at least one of the light sensing elements is color selective.

In another aspect of the invention, color selective property results from a band gap property of a semiconductor device element comprised by the at least one light sensor.

In another aspect of the invention, the algorithm comprises array multiplication of numerical values responsive to the plurality of electronically-represented digital numbers.

In another aspect of the invention, the algorithm comprises array multiplication of numerical values obtained from the calculation of a generalized inverse matrix.

In another aspect of the invention, the algorithm comprises array multiplication of numerical values obtained from an interpolation.

In another aspect of the invention, the algorithm comprises array multiplication of numerical values obtained from a predictive analytical model.

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In another aspect of the invention, the algorithm comprises array multiplication of numerical values derived from a predictive analytical model.

In another aspect of the invention, the algorithm comprises array multiplication of numerical values derived from 5 empirical measurements.

BRIEF DESCRIPTION OF THE DRAWINGS

The above and other aspects, features and advantages of 10 the present invention will become more apparent upon consideration of the following description of preferred embodiments taken in conjunction with the accompanying drawing figures, wherein:

- FIG. 1 depicts an example conceptual view of the under- 15 lying principles of the invention, facilitating a wide range of implementation methods and architectures.
- FIG. 2 depicts an illustrative representational view of the confluence of the expanded features and capabilities taught in the inventor's 1999 patent family.
- FIG. 3 depicts an illustrative representational view of the confluence of the expanded features and capabilities taught in the inventor's 2008 patent family. The 2009 addition of optical tomography capabilities is also noted.
- FIG. 4 depicts an illustrative representational view of the 25 confluence of the expanded features and capabilities associated with the present invention. This depiction and the elements therein are intended as only illustrative and representative and does not provide or suggest a comprehensive or exhaustive listing, structure, or characterization.
- FIG. 5 depicts a more detailed view of the inventor's comprehensive lensless light-field imaging program (beginning with the inventor's 1999 patent family) is and recently-popularized coded-aperture lensless imaging.
- popularized coded-aperture lensless imaging.

 FIG. 6 depicts a functional "timeline" view of non- 35 pinhole lensless imaging, including both the inventor's comprehensive lensless light-field imaging program (beginning with the inventor's 1999 patent family) is and recently-popularized (2011-2016) coded-aperture lensless imaging (recently termed a lensless "Computational Renaissance" 40 [P6]) stemming from radiation-imaging work dating from 1968 [P62].
- FIG. 7 depicts a timeline of representative technologyrelated patents and literature with respect to the inventor's comprehensive lensless light-field imaging program.
- FIG. 8a, adapted from FIG. 42 of the present inventor's U.S. Pat. No. 8,830,375 and related cases, depicts a vector space of trade-offs for semiconducting diode-junction devices.
- FIG. **8***b*, adapted from FIG. **4**2 of the present inventor's 50 U.S. Pat. No. 8,830,375 and related cases, depicts an adaptation of FIG. **8***a* wherein different optimizations are used for implementing single function diode-junction devices such as (but not limited to) switching diodes versus lightemitting diodes (LEDs) versus photodiodes.
- FIG. 9a, adapted from the figure available on the internet at https://en.wikibooks.org/wiki/Introduction_to_Inorganic_Chemistry/Electronic_Properties_of_Materials:_Superconductors_and_Semiconductors#/media/File:Pn-Junction-E.PNG as retrieved Jul. 3, 2017 (top portion), 60 depicts a representation of the active carrier flow of a forward biased switching diode wherein, by design, current-flow directional switching functions are optimized and light-emission and light-detection capabilities of PN junctions are suppressed.
- FIG. 9b, adapted from the figure available on the internet at https://en.wikibooks.org/wiki/Introduction_to_

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Inorganic_Chemistry/Electronic_Properties_of_ Materials:_Superconductors_and_Semiconductors#/media/ File:PnJunction-E.PNG as retrieved Jul. 3, 2017 (middle portion), depicts the blocked carrier flow of a reversed biased situation for the switching diode depicted in FIG. 9a.

FIG. 9c, adapted from the figure available on the internet at https://en.wikibooks.org/wiki/Introduction_to_Inorganic_Chemistry/Electronic_Properties_of_

Materials: Superconductors and Semiconductors#/media/File:PnJunction-E.PNG as retrieved Jul. 3, 2017 (bottom portion), depicts an energy-band representation of a switching diode wherein, by design, current-flow directional switching functions are optimized and light-emission and light-detection capabilities of PN junctions are suppressed.

FIG. 9d, adapted from the image available at http://www.leamabout-electronics.org/Semiconductors/diodes_23.php as visited on Jun. 20, 2017, depicts a representation of the physical construction of a switching diode wherein, by design, current-flow directional switching functions are optimized and light-emission and light-detection capabilities of PN junctions are suppressed.

FIG. **10***a*, adapted from the top portion of a figure available on the internet at https://en.wikipedia.org/wiki/Light-emitting_diode#/media/File:PnJunction-LED-E.svg as retrieved Jul. 3, 2017, depicts a carrier-process representation of an operating (inorganic or organic) semiconducting PN junction light-emitting diode (LED).

FIG. 10b, adapted from the bottom portion of a figure available on the internet at https://en.wikipedia.org/wiki/Light-emitting_diode#/media/File:PnJunction-LED-E.svg as retrieved Jul. 3, 2017, depicts an energy-transition representation of an operating (inorganic or organic) semiconducting PN junction light-emitting diode (LED).

FIG. 11a, adapted from figure 4.7.1 of the on-line notes "Principles of Semiconductor Devices" by B. Van Zeghbroeck, 2011, available at https://ecee.colorado.edu/~bart/book/book/chapter4/ch4_7. htm as retrieved Jul. 3, 2017, depicts an abstracted structural representation of an example (inorganic or organic) simple ("simple-heterostructure") semiconducting PN junction light-emitting diode (LED).

FIG. 11b, adapted from Figure 7.1 of the on-line table of figures available on the internet at https://www.ecsarpi.edu/~schubert/Light-Emitting-Diodes-dot-org/chap07/chap07.htm as retrieved Jul. 3, 2017, depicts an abstracted structural representation of an example (inorganic or organic) more complex double-heterostructure semiconducting PN junction light-emitting diode (LED), here effectively configured as a two-PN junction sandwich. FIG. 12a (adapted from G. Gu, G. Parthasarathy, P. Burrows, T. Tian, I. Hill, A. Kahn, S. Forrest, "Transparent stacked organic light emitting devices. I. Design principles and transparent compound electrodes," Journal of Applied Physics, October 1999, vol. 86 no. 8, pp. 4067-4075) depicts an example high-level structure of a three-color transparent Stacked OLED ("SOLED") element.

- FIG. 12b (also adapted from G. Gu, G. Parthasarathy, P. Burrows, T. Tian, I. Hill, A. Kahn, S. Forrest, "Transparent stacked organic light emitting devices. I. Design principles and transparent compound electrodes," Journal of Applied Physics, October 1999, vol. 86 no. 8, pp. 4067-4075) depicts a more detailed structure of a three-color transparent SOLED element.
- FIG. **13***a*, depicts an example energy-transition representation of an operating (inorganic or organic) simple semiconducting PN junction photodiode.
- FIG. 13b, simplified and adapted from the first two figures in "Comparison of waveguide avalanche photodiodes with InP and InAlAs multiplication layer for 25 Gb/s operation"

by J. Xiang and Y. Zhao, Optical Engineering, 53(4), published Apr. 28, 2014, available at http://opticalengineering.spiedigitallibrary.org/article.aspx?articleid=1867195 as retrieved Jul. 3, 2017, depicts an example structural representation of an example simple layered-structure PIN (inorganic or organic) simple semiconducting PN junction photodiode.

FIG. 14a, adapted from FIG. 2 of U.S. Pat. No. 7,202,102 "Doped Absorption for Enhanced Responsivity for High Speed Photodiodes" to J. Yao, depicts a combined energy/structure representation of a more specialized example layered-structure avalanche semiconducting PN junction photodiode

FIG. 14b, adapted from the first two figures in "Comparison of waveguide avalanche photodiodes with InP and 15 InAlAs multiplication layer for 25 Gb/s operation" by J. Xiang and Y. Zhao, Optical Engineering, 53(4), published Apr. 28, 2014, available at http://opticalengineering.spiedigitallibrary.org/article.aspx?articleid=1867195 as retrieved Jul. 3, 2017, depicts an example structural representation of an example layered-structure avalanche semiconducting PN junction photodiode.

FIG. **15***a* depicts material science and fabrication relationships among (1) transparent/non-transparent electronics and optoelectronics, (2) flexible/non-flexible electronics and 25 optoelectronics, (3) printed/non-printed electronics and optoelectronics, and (4) organic/non-organic electronics and optoelectronics.

FIG. 15b provides a version of FIG. 15a where certain types of the electronics and optoelectronics are marked with 30 asterisks (*) to signify functional contributions to various aspects of the present invention.

FIG. **16***a*, adapted from [P5], depicts a schematic representation of the arrangements and intended operational light paths for a pinhole camera.

FIG. **16**b, adapted from [P5], depicts a schematic representation of the arrangements and intended operational light paths for a (simplified or single-lens) lens-based camera.

FIG. **16**c, adapted from [P5], depicts a schematic representation of the arrangements and intended operational light 40 paths for a mask-based camera, such as those discussed in [P62]-[P67].

FIG. **16***d* depicts to a schematic representation of some aspects of the present invention and the inventor's more comprehensive lensless light-field imaging program.

FIG. 17 depicts an array of parallel-oriented vignetting cavities; the bottom of each cavity can comprise or direct isolated light to light-sensing structure.

FIG. 18, adapted from FIG. 12 of the present inventor's U.S. Pat. No. 8,816,263 and related cases, illustrates a 50 simplified view of how a vignette structure can limit the range of incident angles at which rays of light within a light field are able to reach the surface of the light-sensing element within a vignetting structure covering a light-sensing element. (Importantly, reflective effects within the 55 vignette and diffraction effects are not illustrated.)

FIG. 19, composited and adapted from FIGS. 8 and 9a through 9b of the present inventor's U.S. Pat. No. 8,830,375 and related cases, illustrates a simplified view of the process by which the degree of vignette overlap increases as separation between the object in the scene and its distance from the micro-optic structure and light sensor array increases and how the degree of vignette overlap increases from 0% to values approaching 100% as the separation distance between a scene object and the micro-optic structure and light sensor 65 array increases. (Importantly, reflective effects within the vignette and diffraction effects are not illustrated.)

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FIGS. **20***a* through **20***c* depict illustrative representations of reflection and scattering effects within a vignette. (Importantly, diffraction effects are not illustrated.)

FIG. 21, adapted from FIG. 11b of the present inventor's U.S. Pat. No. 8,816,263 and related cases, depicts an array of parallel-oriented instances of alternating short" light-sensing structures and "tall", each parallel-oriented instance alternately staggered to create vignetting cavities surrounded by the sides of neighboring "tall" structures (which in some implementations can be light-emitting), the bottom of each cavity comprising a "short" light-sensing structure. In some implementations, the "tall" structures can be light-emitting.

FIGS. **22***a* through **22***c* depict differing illustrative 3-dimensional views of a plane the containing the sensing surface of a planar image sensor arrangement, and extending spatially in front of the planar image sensor a coordinate grid defining numerically quantizing regions on an incoming light field that can be observed by the planar image sensor arrangement. Depending on the directional capabilities of the planar image sensor arrangement, the shape of the observable light field can have a different shape than the illustrative rectangular parallelepiped.

FIG. 23a depicts an example spatial quantization of a light field extending spatially in front of the planar image sensor into a lattice of distinct indexable volume elements (voxels).

FIG. 23b depicts an example spatial quantization of the light field voxel lattice of FIG. 23a by representing the aggregate of light-emission, light reflection, and/or light propagation within the voxel as (1) having a composite quantitative value of light representing the combined aggregate of light-emission, light reflection, and/or light propagation within the volume of voxel which is (2) concentrated at a point in the interior of the voxel.

FIG. 24 depicts a pair of illustrative 3-dimensional views of an example arrangement comprising a planar array of (emitted and/or reflected) light source elements and a parallel planar array of light-sensing elements, and a spatially-quantized light-field representation between the planes. The roles of planar array of light source elements and a parallel array of light-sensing elements can be interchanged.

FIGS. **25***a* and **25***b* depict a pair of illustrative 3-dimensional views of an example variation of the arrangement depicted in FIG. **24** wherein a planar array of (emitted and/or reflected) light source elements and a planar array of light-sensing elements, are not parallel planes. The roles of planar array of light source elements and a parallel array of light-sensing elements can be interchanged.

FIG. 26a depicts another illustrative 3-dimensional view of an example variation of the arrangement depicted in FIGS. 25a and 25b wherein the dihedral angle between the planes is farther from parallel. The roles of planar array of light source elements and a parallel array of light-sensing elements can be interchanged.

FIG. **26***b* depicts an illustrative 3-dimensional view of another example of the arrangements depicted in FIGS. **25***a*, **25***b*, and **26***a* wherein the dihedral angle between the planes is sloped in two dimensions. The roles of planar array of light source elements and a parallel array of light-sensing elements can be interchanged.

FIGS. **27***a* and **27***b* depict a pair of illustrative 3-dimensional views of an example of a non-planar curved surface and a planar surface with a spatially-quantized light-field representation between the two surfaces.

FIGS. **28***a* and **28***b* depict a pair of illustrative 3-dimensional views of a variation on FIGS. **27***a* and **27***b* featuring different example non-planar curved surface.

FIG. **29***a* depicts an illustrative example of non-planar curved surface sensor and non-planar curved surface object with a spatially-quantized light-field representation between the two surfaces. Either or both of the curved surfaces can be configured to be a camera.

FIG. **29***b* depicts an example cross-section of a (rigid or flexible) curved imaging surface, for example as may be fabricated by printing or other deposition fabrication processes

FIGS. 30a through 30c depict a variety of illustrative 10 3-dimensional views of an example variation of the arrangement depicted in FIGS. 24, 25a, 25b, 26a, and 25b wherein the array of (emitted and/or reflected) light source elements are split among a plurality of smaller parallel planes at different separation distances from the planar array of lightsensing elements. Depending on the spatial arrangement, some portions of some of the smaller parallel planes can be observationally occulted from some regions of the planar surface. The roles of the plurality of planar arrays of light source elements and a parallel array of light-sensing elements can be interchanged.

FIGS. **31***a* and **31***b* depict a variety of illustrative 3-dimensional views of an example variation of the arrangement depicted in FIGS. **24**, **25***a*, **25***b*, **26***a*, and **25***b* wherein the array of (emitted and/or reflected) light source elements are 25 distributed over a connected group of planes, at least one parallel to the planar array of light-sensing elements.

FIGS. **32***a* through **32***c* depict a variety of illustrative 3-dimensional views of an example wherein the array of (emitted and/or reflected) light source elements are distributed over a complex collection of connected and disconnected planes, some of which are parallel to the planar array of light-sensing elements, and some of which observationally occulted others from some regions of the planar surface by being situated directly in front of others.

FIGS. 33a and 33b depict example inward-directed or outward-directed sensor-pixel lattice locations distributed on a rigid or elastic curved convex-shaped surface.

FIGS. **34***a* through **34***d* depicts examples of pairs of curved and sharply-angled surfaces, one of the pair inside 40 the other of that pair. In any of the arrangements depicted, at least one of the inner surface and the outer surface can be a camera arranged to view the other surface. As considered elsewhere, the camera can be configured to provide self-illumination.

FIGS. **35***a* through **35***c* depict illustrative examples of bumpy and/or pitted sensor surfaces that can provide angular diversity. Such arrangements can also be used to provide sensor robustness via spatial diversity, to provide directed angle-orientation viewing, and to provide other types of 50 functions. These can be combined with the generous recovery capabilities described in the mathematical treatment to follow, and enhanced further by the statistical corrections obtainable using the Moore-Penrose pseudo-inverse, to provide immense imaging robustness to a wide range of deg- 55 radation and partial occultation effects.

FIG. 36 depicts example correspondences between a physical optical arrangement comprising an optical process (including for example vignetting optics and free-space separation should the image sensor not be in contact with the 60 actual source image) and a mathematical model of that physical optical arrangement (transforming an actual image array data to measured image array data by a numerical model of the optical process.

FIG. 37 depicts an illustrative example of Mathematical 65 Recovery of an approximate representation of the actual Image from Measured Image Array Data obtained by oper-

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ating on the Measured Image Array Data by a Numerical Inverse of the Model of the Optical Process as depicted in FIG. 36

FIG. 38, adapted from FIG. 2b of the present inventor's U.S. Pat. No. 8,830,375 and related cases, depicts an exemplary embodiment comprising a micro-optic structure, a light sensor array, an image formation signal processing operation and an optional additional subsequent image processing operations, herein the micro-optic structure and light sensor array are grouped into a first subsystem, and the image formation signal processing operation and subsequent image processing operations are grouped into a second subsystem. As discussed in the present inventor's U.S. Pat. No. 8,830,375 and related cases, various other arrangements are possible and provided for by aspects of the invention.

FIG. 39a depicts an example scheme wherein manufacturing, physical, optical, and mathematical considerations are used to create a reproducible manufacturing design such that is adequate manufacturing tolerances are obtained an analytical predictive model can be used to produce numerical models of the optical situations to be recovered without the use of empirical measurements.

FIG. **39***b* depicts an example variation on the scheme presented in FIG. **39***a* wherein post-manufacturing empirical measurements are used to further fine-calibrate the system performance of each particular manufactured article.

FIG. **40** depicts an example representation of example serialization processes and de-serialization processes for image recovery from an inverse or pseudo-inverse model as provided for by the invention.

FIG. 41 depicts a representation of example serialization processes transforming a measured image produced by a light-field travelling through an optical structure (here a vignette array) at being measured by a sensor array.

FIG. 42 depicts a representation of example empirical image-basis "training" sequence, or alternatively a collection of predictive-model-generated image-bases that directly populate a JK×NM matrix providing a numerical model of the optical environment from which a future image will later be recovered as provided for by aspects of the invention.

FIG. 43a depicts a representation of example image recovery process using an inverse square-matrix representing an approximate inverse model as provided for by the invention.

FIG. 43b depicts a representation of example image recovery process using a generalized-inverse or pseudo-inverse matrix representing an approximate pseudo-inverse underspecified model as provided for by the invention.

FIG. **43**c depicts a representation of example image recovery process using a generalized-inverse or pseudo-inverse matrix representing an approximate pseudo-inverse overspecified model as provided for by the invention.

FIG. **44***a* depicts a simple computational approach for image recovery as provided for by the invention.

FIG. **44***b* depicts an example representation of a far more numerically-complex spectral or transform computation (which numerically amounts to additional basis rotation transformation steps) as would be used in spectral or transform methods.

FIG. **44**c depicts a comparison of the more direct computational approach depicted in FIG. **44**a and the approach depicted in FIG. **44**b, demonstrating comparative reasons to reject the far more numerically-complex spectral or transform computational approached represented in FIG. **44**b.

FIG. **45** depicts the use of classical ill-posed inverseproblem regularization methods as employed in the Rambus [P4] and Rice University "Flat Cam" [P5] implementations

as well as other coded aperture imaging implementations. These classical ill-posed inverse-problem regularization methods are widely used in many areas but also have an established role in optical systems design and analysis; see for example [B5] and [B6].

FIG. **46** depicts an abstract representation of an "Identity structure" within a (necessarily-sparse) Identity 4-tensor.

FIG. 47 depicts an abstract representation of a dilation around the "Identity structure" within a (necessarily-sparse) Identity 4-tensor.

FIG. 48 depicts a $((7\times7)\times(7\times7))$ "matrix-of-matrices" representation of a $(7\times7\times7\times7)$ Identity 4-tensor as abstracted in FIG. 46.

FIG. **49** depicts an example $((7\times7)\times(7\times7))$ "matrix-of-matrices" representation of the dilation around the "Identity 15 structure" of a $(7\times7\times7\times7)$ 4-tensor as abstracted in FIG. **46**.

FIG. **50** depicts an abstract representation of the trade-off between Space/Inverse-Space/Spatial Frequency Localization Methods and the sparcity of numerical model tensors, matrices, and their inverses. This can be used, for example, 20 in designing vignetting and aperture arrays.

FIGS. **51***a* through **51***e* depict how the sparcity of an example numerical model matrix serializing a numerical model 4-tensor degrades as the image source moves farther and farther from the image sensor (using numerical models 25 at each distances predicted by an analytical geometric predictive model provided for by the invention).

FIG. **52** depicts an example $((7\times7)\times(7\times7))$ "matrix-of-matrices" representation of the numerical model 4-tensor and example measured image (right) at zero separation 30 distance from a single-illuminated-pixel source image (left). As described elsewhere, the source image need not be on a parallel plane and can be distributed arbitrarily in space.

FIG. 53 depicts an example $((7\times7)\times(7\times7))$ "matrix-of-matrices" representation of the numerical model 4-tensor 35 and example measured image (right) at a small non-zero separation distance from the same single-illuminated-pixel source image (left) as in FIG. 52.

FIG. **54** depicts an example $((7\times7)\times(7\times7))$ "matrix-of-matrices" representation of the numerical model 4-tensor 40 and example measured image (right) at zero separation distance from a two-illuminated-pixel source image (left). As described elsewhere, the source image need not be on a parallel plane and can be distributed arbitrarily in space.

FIG. **55** depicts an example $((7\times7)\times(7\times7))$ "matrix-of- 45 matrices" representation of the numerical model 4-tensor and example measured image (right) at a small non-zero separation distance from the same two-illuminated-pixel source image (left) as in FIG. **54**.

FIG. **56** depicts an example $((7\times7)\times(7\times7))$ "matrix-of- 50 matrices" representation of the numerical model 4-tensor and example measured image (right) at zero separation distance from a more closely-spaced two-illuminated-pixel source image (left). As described elsewhere, the source image need not be on a parallel plane and can be distributed 55 arbitrarily in space.

FIG. **57** depicts an example $((7\times7)\times(7\times7))$ "matrix-of-matrices" representation of the numerical model 4-tensor and example measured image (right) at a small non-zero separation distance from the same more closely-spaced 60 two-illuminated-pixel source image (left) as in FIG. **56**.

FIGS. **58***a* through **58***c* depict three of forty-nine steps of an example empirical training sequence as provided for by the invention. In an implementation of the invention, such a procedure could be performed for a selected collection of 65 one or more separation distances between the image sensor and the source image. As described elsewhere, the source

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image need not be on a parallel plane and can be distributed arbitrarily in the observable space.

FIG. **59** depicts an example polynomial fitting function interpolation method for interpolating the numerical model, its inverse/pseudo-inverse, and/or other functions for separation distances values lying between k empirically-trained separation distances. As described elsewhere, the source image need not be on a parallel plane and can be distributed arbitrarily in the observable space

FIG. **60** depicts an example polynomial fitting function interpolation method for interpolating the numerical model, its inverse/pseudo-inverse, and/or other functions for separation distances values lying between k separation distances used by a predictive-model. As described elsewhere, the source image need not be on a parallel plane and can be distributed arbitrarily in the observable space.

FIG. 61 depicts an example of very poor curve-fit interpolation of the matrix elements of the numerical model between measure data distances resulting from not having correct or sufficient terms in a model polynomial.

FIG. **62** depicts an example piecewise-linear interpolation of the matrix elements of the numerical model between k empirically-trained separation distances.

FIG. 63a depicts how with very small separation distances and certain non-alignment of source-pixel locations and sensor pixel locations some sensor pixel locations cannot receive light from proximate source-pixel locations, while FIG. 63b depicts how at slightly greater separation distances this condition does not occur; such processes can give rise to the rising and falling of selected curves in the example empirical training data shown in the example of FIG. 61.

FIG. **64** depicts an example piecewise-linear interpolation method for interpolating the numerical model, its inverse/pseudo-inverse, and/or other functions for separation distances values lying between k empirically-trained separation distances. As described elsewhere, the source image need not be on a parallel plane and can be distributed arbitrarily in the observable space.

FIG. **65** depicts an example piecewise-linear interpolation method for interpolating the numerical model, its inverse/pseudo-inverse, and/or other functions for separation distances values lying between k separation distances used by a predictive-model. As described elsewhere, the source image need not be on a parallel plane and can be distributed arbitrarily in the observable space.

FIG. **66** depicts an abstract representation of the mathematical recovery of image from measured image array data.

FIG. 67 depicts a variation on the representation of the mathematical recovery of image from measured image array data shown in FIG. 66 wherein more measurements are made than needed, resulting in an over-specified collection of measurements that can be expected to lead to inconsistent calculation outcomes when different subgroups of measurements are used to solve for the recovered image. As provided for by the invention, a Moore-Penrose pseudo-inverse operation gives a least-squares fit to the expected inconsistent outcomes; this is depicted in the bottom portion of the figure.

FIG. **68***a* through **68***d* depict example numerical model outcomes responsive to a single-illuminated pixel as generated for various separation distances by an example predictive analytical geometric model. The particular example predictive analytical geometric model used only accounts for vignette occultation as calculated by simple ray-trancing and does not include the effects of vignette-internal reflec-

tions, vignette-internal scattering, vignette-aperture diffraction, surface plasmoid propagation, etc.

FIG. **69***a* depicts three example interactive quantizationeffect modeling outcomes wherein controllable quantization is artificially imposed on measurement data so as to predictively model and characterize the effects of quantizing nonlinearities imposed by electronic digital-to-analog converter processes on empirical training, predictive-model generated, and real-time measurements as they influence the quality of image recovery.

FIG. **69***b* depicts three example interactive offset-effect modeling outcomes wherein controllable measurement offset is artificially imposed on measurement data so as to predictively model and characterize the effects of measurement offsets imposed by electronic digital-to-analog converter processes on empirical training, predictive-model generated, and real-time measurements as they influence the quality of image recovery.

FIG. **69**c depicts an example interactive noise-modeling 20 control used to introduce synthetically-generated noise and noise processes so as to predictively model and characterize its effects. The selection shown controls additive Gaussian noise, but other noise processes associated with photodiodes can similarly be introduced.

FIGS. 70a through 70d depict example interactive modeling outcomes showing the effect of noise, offset, and both these for a 32-step (5-bit) quantized ("DN" [B2]) measurement dynamic range.

FIGS. 71a through 71d depict example interactive modeling outcomes showing the effect of noise, offset, and both these for a 64-step (6-bit) quantized ("DN") measurement dynamic range.

FIG. **72***a* through **72***d* depict example interactive modeling outcomes showing the effect of noise, offset, and both 35 these for a 128-step (7-bit) quantized ("DN") measurement dynamic range.

FIGS. 73a through 73d depict example interactive modeling outcomes showing the effect of noise, offset, and both these for a 140-step (slightly more than 7-bit) quantized 40 ("DN") measurement dynamic range.

FIG. 74a through 74d depict example interactive modeling outcomes showing the effect of noise, offset, and both these for a 150-step (yet more than 7-bit) quantized ("DN") measurement dynamic range.

FIG. 75a, adapted from [B7] Figure C2.5.16(a), depicts a first example pixel-cell multiplexed-addressing circuit for an individual OLED within an OLED array that includes a dedicated light-coupled monitoring photodiode for use in regulating the light output of the individual OLED so as to 50 prevent user-observed fading or other brightness-variation processes.

FIG. **75***b*, adapted from [B7] Figure C2.5.16(b), depicts a second example pixel-cell multiplexed-addressing circuit for an individual OLED within an OLED array that includes 55 a dedicated light-coupled monitoring photodiode for use in regulating the light output of the individual OLED so as to prevent user-observed fading or other brightness-variation processes.

FIG. **76***a*, adapted from [B18], depicts an example pixel-60 cell multiplexed-addressing circuit for an individual OLED within an OLED array with a monitoring feature.

FIG. **76***b*, also adapted from [B18], depicts an example pixel-cell multiplexed-addressing circuit for an isolated high-performance photodiode or phototransistor within a 65 high-performance photodiode or phototransistor array with a forced-measurement provision.

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FIG. 77 depicts a simplified view of FIG. 1 showing only the signal and computational portion of FIG. 1 as will be useful in a subsequent discussion.

FIG. **78** depicts a variation of the arrangement represented in FIG. **77** wherein the Inverse Model is rendered as a parameterized Inverse Model which can be altered responsive to one or more provided parameters.

FIG. 79 depicts a variation of the arrangement represented in FIG. 78 wherein the electrical signals and/or computational data produced by the Optical Sensor are in parallel provided in whole or selected (or selectable) part to a plurality of Inverse Models, each producing one or more computationally-produced images responsive to the sensor data.

FIG. 80 depicts a variation of the arrangement represented in FIG. 78 wherein the electrical signals and/or computational data produced by the Optical Sensor is handled by a computer or computational element (such as a microprocessor, GPU, DSP chip, ALU, FPLA, combination of two or more these, pluralities of these, etc.) in some fashion that at least permits the electrical signals and/or computational data produced by the Optical Sensor to be stored as a file.

FIG. **81** depicts a variation of the arrangement represented in FIG. **78** wherein the aforementioned handling by a computer or computational element is controlled in some manner by a control parameter.

FIG. **82***a* depicts a variation of the arrangement represented in FIG. **81** wherein a plurality of stored files is created, for example with different parameter values associated with each stored file.

FIG. **82***b* depicts an example arrangement wherein a stored file is used by a fixed Inverse Model to create a computationally-produced image.

FIG. **82**c depicts an example arrangement wherein a stored file is used by a parameterized Inverse Model to create a computationally-produced image, and further wherein parameter value(s) associated the parameterized Inverse Model are externally associated with each stored

FIG. **82***d* depicts an example arrangement wherein a stored file is used by a parameterized Inverse Model to create a computationally-produced image, and further wherein parameter value(s) associated the parameterized Inverse Model are derived from or obtained from the stored file.

FIG. 83 depicts four example conformations of a particular bendable, flexible, and/or or pliable optical-sensor/optical-structure sheet, each conformation giving rise to an associated model for how a light field is sensed in the context of reconstructing an image, and each model giving rise to its own associated inverse model. It is noted that, as dependent on the properties and limitations of the optical-structure, there can be small blind spots in regions of sufficiently-high curvature.

FIG. **84***a* through FIG. **84***d* depict how various conformations can be used to render a computationally derived image

FIG. **85***a* depicts an example arrangement for an optical-sensor/optical-structure of fixed conformation.

FIG. **85***b* depicts an example arrangement for an optical-sensor/optical-structure of variable conformation, for example should the surface bend, deform, hinge, expand, contract, etc.

FIG. **85**c depicts a variation of FIG. **85**b wherein the model and the Inverse Model are parameterized.

FIG. **86***a* depicts an arrangement useful for using optical training to sense the present conformation of an optical-

sensor/optical-structure of variable conformation, for example should the surface bend, deform, hinge, expand, contract, etc.

FIG. **86**b depicts an arrangement useful for using internal sensing means to sense the present conformation of an 5 optical-sensor/optical-structure of variable conformation. for example should the surface bend, deform, hinge, expand, contract, etc.

FIG. 86c depicts an arrangement useful for using information about a movable or changing support structure or contact arrangement to identify the present conformation of an optical-sensor/optical-structure of variable conformation, for example should the surface bend, deform, hinge, expand, contract, etc.

FIG. **86***d* depicts an arrangement useful for using external observation mean, for example such as one or more observing video camera(s) means to sense the present conformation of an optical-sensor/optical-structure of variable conformation, for example should the surface bend, deform, 20 hinge, expand, contract, etc.

FIG. 87a depicts an optical-sensor/optical-structure of variable conformation, for example should the surface bend, deform, hinge, expand, contract, etc. producing an output signal and/or output data.

FIG. 87b depicts a controllable variable-conformation material whose shape/conformation can be controlled by externally-provide control stimulus.

FIG. 87c depicts an optical-sensor/optical-structure of variable conformation, for example should the surface bend, 30 deform, hinge, expand, contract, etc. producing an output signal and/or output data fabricated on, with, or co-integrated with controllable variable-conformation material whose shape/conformation can be controlled by externallyprovide control stimulus.

FIG. 88a depicts use of conformational sensing information to derive or compute parameter values for a parameterized Inverse Model.

FIG. 88b depicts use of conformational control parameter information to derive or compute parameter values for a 40 parameterized Inverse Model.

FIG. 88c depicts use of both conformational sensing information and conformational control parameter information to derive or compute parameter values for a parameterized Inverse Model.

DETAILED DESCRIPTION

In the following description, reference is made to the accompanying drawing figures which form a part hereof, 50 and which show by way of illustration specific embodiments of the invention. It is to be understood by those of ordinary skill in this technological field that other embodiments may be utilized, and structural, electrical, as well as procedural changes may be made without departing from the scope of 55 conductors_and_Semiconductors#/media/File:PnJunctionthe present invention.

In the following description, numerous specific details are set forth to provide a thorough description of various embodiments. Certain embodiments may be practiced without these specific details or with some variations in detail. In 60 some instances, certain features are described in less detail so as not to obscure other aspects. The level of detail associated with each of the elements or features should not be construed to qualify the novelty or importance of one feature over the others.

FIG. 7 depicts a timeline of representative patents and literature and patents in lensless imaging and light-field **30**

imaging with respect to the inventor's comprehensive lensless light-field imaging program.

FIG. 8a, adapted from FIG. 42 of the present inventor's U.S. Pat. No. 8,830,375 and related cases, depicts a vector space of trade-offs for semiconducting diode-junction devices. As taught in the inventor's earlier patents, there are opportunities to, rather than exclusively optimize for lightsensing or light-emission, to instead co-optimize for both light-sensing and light-emission.

The present invention provides for co-optimizing of doping, electrode configurations, structure, and other attributes for both light-sensing and light-emission, giving rise to entirely new kinds of semiconductor optoelectronic elements and devices. Rapidly evolving organic semiconductor material science methods, including polymer properties and meta-material properties, can be used to improve quantum efficiency, noise performance, transparency, size requirements, electrical characteristics, etc. as well as facilitate useful manufacturing techniques such as high-resolution printing. Additional features, such as angular-selectivity and wavelength selectivity, can also be included. Additional structures, such as vignetting or aperturing arrays, reflective optical path walls to reduce incident light-loss, angular diversity, curvature, flexibility, etc. can be co-integrated, and can for example be designed to produce predictable reproducible optical sensing behaviors. Exotic features, such as predictable or and/or reproducible surface plasmon propagation to selected light sensors to further reduce incoming light loss and use of quantum dots, can be included.

FIG. 8b, adapted from FIG. 42 of the present inventor's U.S. Pat. No. 8,830,375 and related cases, depicts an adaptation of FIG. 8a wherein different optimizations are used for implementing single function diode-junction devices such as (but not limited to) switching diodes versus lightemitting diodes (LEDs) versus photodiodes.

FIG. 9a, adapted from the figure available on the internet at https://en.wikibooks.org/wiki/Introduction to Inorganic-_Chemistry/Electronic_Properties_of_Materials:_Superconductors_and_Semiconductors#/media/File:PnJunction-E.PNG as retrieved Jul. 3, 2017 (top portion), depicts a representation of the active carrier flow of a forward biased switching diode wherein, by design, current-flow directional switching functions are optimized and light-emission and light-detection capabilities of PN junctions are suppressed.

FIG. 9b, adapted from the figure available on the internet at https://en.wikibooks.org/wiki/Introduction_to_Inorganic-Chemistry/Electronic Properties of Materials: Superconductors_and_Semiconductors#/media/File:PnJunction-E.PNG as retrieved Jul. 3, 2017 (middle portion), depicts the blocked carrier flow of a reversed biased situation for the switching diode depicted in FIG. 9a.

FIG. 9c, adapted from the figure available on the internet at https://en.wikibooks.org/wiki/Introduction_to_Inorganic-_Chemistry/Electronic_Properties_of_Materials:_Super-E.PNG as retrieved Jul. 3, 2017 (bottom portion), depicts an energy-band representation of a switching diode wherein, by design, current-flow directional switching functions are optimized and light-emission and light-detection capabilities of PN junctions are suppressed.

FIG. 9d, adapted from the image available at http:// www.leamabout-electronics.org/Semiconductors/diodes 23.php as visited on Jun. 20, 2017, depicts a representation of the physical construction of a switching diode wherein, by design, current-flow directional switching functions are optimized and light-emission and light-detection capabilities of PN junctions are suppressed.

FIG. **10***a*, adapted from the top portion of a figure available on the internet at https://en.wikipedia.org/wiki/Light-emitting_diode#/media/File:PnJunction-LED-E.svg as retrieved Jul. 3, 2017, depicts a carrier-process representation of an operating (inorganic or organic) semiconducting 5 PN junction light-emitting diode (LED).

FIG. **10***b*, adapted from the bottom portion of a figure available on the internet at https://en.wikipedia.org/wiki/Light-emitting_diode#/media/File:PnJunction-LED-E.svg as retrieved Jul. 3, 2017, depicts an energy-transition representation of an operating (inorganic or organic) semiconducting PN junction light-emitting diode (LED).

FIG. 11a, adapted from Figure 4.7.1 of the on-line notes "Principles of Semiconductor Devices" by B. Van Zeghbroeck, 2011, available at https://ecee.colorado.edu/~bart/ 15book/book/chapter4/ch4_7. htm as retrieved Jul. 3, 2017, depicts an abstracted structural representation of an example (inorganic or organic) simple ("simple-heterostructure") semiconducting PN junction light-emitting diode (LED).

FIG. 11b, adapted from Figure 7.1 of the on-line table of 20 figures available on the internet at https://www.ecsarpi.edu/~schubert/Light-Emitting-Diodes-dot-org/chap07/
chap07.htm as retrieved Jul. 3, 2017, depicts an abstracted structural representation of an example (inorganic or organic) more complex double-heterostructure semiconducting PN junction light-emitting diode (LED), here effectively configured as a two-PN junction sandwich. When component layers are properly doped, a P-I-N ("P-type"/"Intrinsic"/"N-type") structure is formed, confining charge carriers into a "small" energy gap surrounded by abrupt 30 energy discontinuities that can be used to create a quantum well; the charge carriers recombine in the "Intrinsic" region and emit photons with wavelengths defined by corresponding discrete permissible energy transitions.

FIG. **12***a* (adapted from G. Gu, G. Parthasarathy, P. 35 Burrows, T. Tian, I. Hill, A. Kahn, S. Forrest, "Transparent stacked organic light emitting devices. I. Design principles and transparent compound electrodes," Journal of Applied Physics, October 1999, vol. 86 no. 8, pp. 4067-4075) depicts an example high-level structure of a three-color transparent 40 Stacked OLED ("SOLED") element.

FIG. 12b (also adapted from G. Gu, G. Parthasarathy, P. Burrows, T. Tian, I. Hill, A. Kahn, S. Forrest, "Transparent stacked organic light emitting devices. I. Design principles and transparent compound electrodes," Journal of Applied 45 Physics, October 1999, vol. 86 no. 8, pp. 4067-4075) depicts a more detailed structure of a three-color transparent SOLED element.

FIG. **13***a*, depicts an example energy-transition representation of an operating (inorganic or organic) simple semi- 50 conducting PN junction photodiode.

FIG. 13b, simplified and adapted from the first two figures in "Comparison of waveguide avalanche photodiodes with InP and InAlAs multiplication layer for 25 Gb/s operation" by J. Xiang and Y. Zhao, Optical Engineering, 53(4), pub-55 lished Apr. 28, 2014, available at http://opticalengineering.spiedigitallibrary.org/article.aspx?articleid=1867195 as retrieved Jul. 3, 2017, depicts an example structural representation of an example simple layered-structure PIN (inorganic or organic) simple semiconducting PN junction photodiode.

FIG. 14a, adapted from FIG. 2 of U.S. Pat. No. 7,202,102 "Doped Absorption for Enhanced Responsivity for High Speed Photodiodes" to J. Yao, depicts a combined energy/structure representation of a more specialized example layered-structure avalanche semiconducting PN junction photodiode.

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FIG. 14b, adapted from the first two figures in "Comparison of waveguide avalanche photodiodes with InP and InAlAs multiplication layer for 25 Gb/s operation" by J. Xiang and Y. Zhao, Optical Engineering, 53(4), published Apr. 28, 2014, available at http://opticalengineering.spiedigitallibrary.org/article.aspx?articleid=1867195 as retrieved Jul. 3, 2017, depicts an example structural representation of an example layered-structure avalanche semiconducting PN junction photodiode.

FIG. 15a depicts material science and fabrication relationships among (1) transparent/non-transparent electronics and optoelectronics, (2) flexible/non-flexible electronics and optoelectronics, (3) printed/non-printed electronics and optoelectronics, and (4) organic/non-organic electronics and optoelectronics.

FIG. **15***b* provides a version of FIG. **15***a* where certain types of the electronics and optoelectronics are marked with asterisks (*) to signify functional contributions to various aspects of the present invention.

FIG. **16***a*, adapted from [P5], depicts a schematic representation of the arrangements and intended operational light paths for a pinhole camera. The box represents a light-tight enclosure with a pinhole opening on the left side that blocks much of the incoming light field (depicted as approaching from the right) but permits transmission of narrow-diameter incoming light rays to enter the enclosure and travel through a region of free-space so as to widen the light area to match that of a (typically rectangular) image sensor, film emulsion, display surface, etc.

FIG. 16b, adapted from [P5], depicts a schematic representation of the arrangements and intended operational light paths for a (simplified or single-lens) lens-based camera. The box represents a light-tight enclosure with a lens and supporting opening for the lens on the left side that bends most rays of the incoming light field (depicted as approaching from the right) for transmission and travel through a region of free-space defined by the lens focal length and the lens law equation so as to create focused image of a selected depth-of-field onto a (typically rectangular) image sensor, film emulsion, display surface, etc.

FIG. 16c, adapted from [P5], depicts a schematic representation of the arrangements and intended operational light paths for a mask-based camera, such as those discussed in [P62]-[P67]. The relatively flatter box represents a light-tight enclosure with a masked opening on the left side that blocks some of the incoming light field (depicted as approaching from the right) and permits transmission the remaining incoming light rays to enter the enclosure and travel through a shorter region of free-space so as to widen the light area to match that of a (typically rectangular) image sensor.

FIG. 16d depicts to a schematic representation of some aspects of the present invention and the inventor's more comprehensive lensless light-field imaging program. No free space is needed and any vignetting optical structure can directly contact and/or be co-integrated or layered upon (by deposition, printing, etc.) the image sensor surface. The optical width of such a vignetting optical structure can be as small as one light-sensing pixel in a light-sensing array, and such a vignetting optical structure can (unlike a mask or the Rambus [P4] diffraction element) have a very simple structure.

The invention further provides for vignetting arrays, aperturing arrays, or other optical structures attached to, cofabricated on, or co-fabricated with an array of light sensors

to include for example, reflective optical path walls to reduce incident light-loss, angular diversity, curvature, flexibility, etc.

The invention further provides for vignetting arrays, aperturing arrays, or other optical structures attached to, cofabricated on, or co-fabricated with an array of light sensors to be designed to produce predictable reproducible optical sensing behaviors. The invention further provides for vignetting arrays, aperturing arrays, or other optical structures attached to, co-fabricated on, or co-fabricated with an array of light sensors to include or facilitate advance light-processing features such as predictable or and/or reproducible surface plasmon propagation to selected light sensors to further reduce incoming light loss, use of quantum dots, etc.

Additionally, the invention provides for each light-sensing pixel element in a light-sensing array to comprise one or separate wavelength-selective light-sensing sub-elements, for example as taught in the inventor's 1999 and 2008 patent families. In some implementations these sub-elements can 20 be spatially adjacent and share the same vignetting or other light-structuring pathway. In other implementations it is advantageous to stack two or more wavelength-selective light-sensing sub-elements in layers, analogous to Stacked Organic Light Emitting Diodes (SOLEDs) as discussed in 25 the inventor's 1999 and 2008 patent families. It is further noted that structures stacking layers of two or more wavelength-selective light-sensing sub-elements can be designed to limit or advantageously structure different vignetting effects each wavelength-selective light-sensing sub-element will experience at each particular depth in the layered stack. It is noted that recent (2016) developments in this area implement light-field imaging (without the use of microlenses) employing layers of "optical" sensors [P43].

FIG. 17 depicts an array of parallel-oriented vignetting cavities; the bottom of each cavity can comprise or direct isolated light to light-sensing structure.

FIG. 18, adapted from FIG. 12 of the present inventor's U.S. Pat. No. 8,816,263 and related cases, illustrates a 40 simplified view of how a vignette structure can limit the range of incident angles at which rays of light within a light field are able to reach the surface of the light-sensing element within a vignetting structure covering a light-sensing element. (Importantly, reflective effects within the 45 vignette and diffraction effects are not illustrated.)

FIG. 19, composited and adapted from FIGS. 8 and 9a through 9b of the present inventor's U.S. Pat. No. 8,830,375 and related cases, illustrates a simplified view of the process by which the degree of vignette overlap increases as separation between the object in the scene and its distance from the micro-optic structure and light sensor array increases and how the degree of vignette overlap increases from 0% to values approaching 100% as the separation distance between a scene object and the micro-optic structure and light sensor 55 array increases. (Importantly, reflective effects within the vignette and diffraction effects are not illustrated.)

FIGS. **20***a* through **20***c* depict illustrative representations of reflection and scattering effects within a vignette. (Importantly, diffraction effects are not illustrated.)

FIG. 21, adapted from FIG. 11 b of the present inventor's U.S. Pat. No. 8,816,263 and related cases, depicts an array of parallel-oriented instances of alternating short" light-sensing structures and "tall", each parallel-oriented instance alternately staggered to create vignetting cavities surrounded by the sides of neighboring "tall" structures (which in some implementations can be light-emitting), the bottom

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of each cavity comprising a "short" light-sensing structure. In some implementations, the "tall" structures can be light-emitting.

Light-Field Origins, Propagation, and Lensless-Light-Field Sensing

Returning to the depiction illustrated in FIG. 1, an Optical Scene creates a Light-Field that is directed to an Optical Sensor which is preceded by one or more Lensless Optical Structure(s) that in some manner alters the light field in a predictable spatial manner. The Optical Sensor produces (typically time-varying) electrical signals and/or computational data responsive (instantly and/or within some time-delay) to light incident to the surface or other substructure(s) within the Optical Sensor at any given moment.

In terms of the mathematical development above, objects or situations producing reflected, refracted, and/or light-emitted contributions to the Light-Field can be represented in a spatially-quantized manner as a light-field source array.

FIGS. **22***a* through **22***c* depict differing illustrative 3-dimensional views of a plane the containing the sensing surface of a planar image sensor arrangement, and extending spatially in front of the planar image sensor a coordinate grid defining numerically quantizing regions on an incoming light field that can be observed by the planar image sensor arrangement. Depending on the directional capabilities of the planar image sensor arrangement, the shape of the observable light field can have a different shape than the illustrative rectangular parallelepiped.

FIG. 23a depicts an example spatial quantization of a light field extending spatially in front of the planar image sensor into a lattice of distinct indexable volume elements (voxels).

FIG. 23b depicts an example spatial quantization of the light field voxel lattice of FIG. 23a by representing the aggregate of light-emission, light reflection, and/or light 35 propagation within the voxel as (1) having a composite quantitative value of light representing the combined aggregate of light-emission, light reflection, and/or light propagation within the volume of voxel which is (2) concentrated at a point in the interior of the voxel. If the light-field is indexed by wavelength or wavelength range, the composite quantitative value can be represented as a function of an associated wavelength index or quantized-wavelength index. The point within each voxel in the light field can be used to define a spatially-quantized vector field representing a physical spatially-continuous vector field (and/or numerical representation thereof). Accordingly, composite quantitative value of light representing the combined aggregate of light-emission, light reflection, and/or light propagation within the volume of voxel can further be represented as a function with a directional argument. In such a manner, the spatial and spectral (wavelength) aspects of a spatially (and if relevant, spectrally) quantized representation of a physical light field can be computationally represented as a multipleindex array.

Case A: Fixed Separation Distance:

Although it will be shown that the constraints on this arrangement can be extremely relaxed, in can be initially convenient to regard the objects or situations producing contributions to the light-field as lying in a plane parallel to an image sensor plane, and the contributions to the light-field comprising a planar (for example rectangular, other shapes explicitly admissible) array of light-providing "light-source" spatially-quantized pixels, each "light-source" pixel emitting light that in various manners make their way to a parallel spatially-separated image sensor plane. The image sensor plane comprises a planar (for example rectangular, other shapes explicitly admissible) array of light-providing

spatially-quantized "light-sensing" pixels, these "light-sensing" pixels producing an electrical signal that can be further processed. The discussion and capabilities of this development explicitly include cases with zero separation distance between at least a planar array of light-providing "light-source" pixels and at least a planar array of "light-sensing" pixels.

As an illustration of Case A, FIG. **24** depicts a pair of illustrative 3-dimensional views of an example arrangement comprising a planar array of (emitted and/or reflected) light source elements and a parallel planar array of light-sensing elements, and a spatially-quantized light-field representation between the planes. Note the roles of planar array of light source elements and a parallel array of light-sensing elements can be interchanged.

Case B: Continuous Spatially-Varying Separation Distances—Non-Parallel Planes:

Relaxing the constraints in Case A, the above-described planes of (a) the objects or situations producing contributions to the light-field and (b) the image sensor are not parallel but rather oriented at some non-parallel and non-perpendicular dihedral angle. The resulting light-field has separation mixed distances. The discussion and capabilities of this development explicitly include cases with zero separation distance between at least a subset (even a 1-dimensional edge or even a single point) of a planar array of light-providing "light-source" pixels and a subset (even a 1-dimensional edge or even a single point) of at least a planar array of "light-sensing" pixels.

As an illustration of Case B, FIGS. **25***a* and **25***b* depict a pair of illustrative 3-dimensional views of an example variation of the arrangement depicted in FIG. **24** wherein a planar array of (emitted and/or reflected) light source elements and a planar array of light-sensing elements, are not 35 parallel planes. Note the roles of planar array of light source elements and a parallel array of light-sensing elements can be interchanged.

As another illustration of Case B, FIG. **26***a* depicts another illustrative 3-dimensional view of an example variation of the arrangement depicted in FIGS. **25***a* and **25***b* wherein the dihedral angle between the planes is farther from parallel. Note the roles of planar array of light source elements and a parallel array of light-sensing elements can be interchanged.

As yet another illustration of Case B, FIG. **26***b* depicts an illustrative 3-dimensional view of another example of the arrangements depicted in FIGS. **25***a*, **25***b*, and **26***a* wherein the dihedral angle between the planes is sloped in two dimensions. Note the roles of planar array of light source 50 elements and a parallel array of light-sensing elements can be interchanged.

Example C: Continuous Spatially-Varying Separation Distances—Curved Surfaces

Relaxing the constraints in Case A in yet another way, one 55 or both of (a) the objects or situations producing contributions to the light-field and/or (b) the image sensor reside on smoothly-curved non-planar surface. The resulting light-field has separation mixed distances and in some cases possible occultation depending on variations in curvature. 60 The discussion and capabilities of this development explicitly include cases with zero separation distance between at least a subset (even a 1-dimensional edge or even a single point) of a planar array of light-providing "light-source" pixels and a subset (even a 1-dimensional edge or even a 65 single point) of at least a planar array of "light-sensing" pixels.

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As an illustration of Case C, FIGS. 27a and 27b depict a pair of illustrative 3-dimensional views of an example of a non-planar curved surface and a planar surface with a spatially-quantized light-field representation between the two surfaces. Note that conceptually that (1) the planar surface could comprise light-sensing elements that observe the non-planar curved surface which in this role comprises (reflective or emitting) light source elements, or (2) if the imaging surface can be rendered as the depicted illustrative non-planar curved surface, the non-planar curved surface could comprise light-sensing elements that observe the planar surface which in this role comprises (reflective or emitting) light source elements. It is noted that regions of the non-planar curved surface that are convex or concave with respect to the planar surface can be observationally occulted from some regions of the planar surface.

As another illustration of Case C, FIGS. **28***a* and **28***b* depict a pair of illustrative 3-dimensional views of a variation on FIGS. **27***a* and **27***b* featuring different example non-planar curved surface. Note here, too, that conceptually that (1) the planar surface could comprise light-sensing elements that observe the non-planar curved surface which in this role comprises (reflective or emitting) light source elements, or (2) if the imaging surface can be rendered as the depicted illustrative non-planar curved surface, the non-planar curved surface could comprise light-sensing elements that observe the planar surface which in this role comprises (reflective or emitting) light source elements. It is also noted that regions of the non-planar curved surface that are convex or concave with respect to the planar surface can be observationally occulted from some regions of the planar surface.

As a variation of Case C, FIG. 29 depicts an illustrative example cross-section of a non-planar (rigid or flexible) curved surface sensor and non-planar curved surface object with a spatially-quantized light-field representation between the two surfaces. Either or both of the curved surfaces can be configured to be a camera, and such arrangements can be fabricated by printing or other deposition fabrication processes. Depending on the spatial arrangement, some portions of some of one of the curved surfaces can be observationally occulted from some regions of the other curved surface. Note the roles of the plurality of planar arrays of light source elements and a parallel array of light-sensing elements can be interchanged.

Case D: Multiple Parallel Planes of Mixed Discrete Separation Distances:

Relaxing the constraints in Case A in still another way, either one or both of (a) the objects or situations producing contributions to the light-field and/or (b) the image sensor resides on more than one planar surfaces but with various separation distances, typically a mix of separation distances. A resulting light-field comprises mixed separation distances with abrupt changes in the separation distance.

As an illustration of Case D, FIGS. **30***a* through **30***c* depict a variety of illustrative 3-dimensional views of an example variation of the arrangement depicted in FIGS. **24**, **25***a*, **25***b*, **26***a*, and **25***b* wherein the array of (emitted and/or reflected) light source elements are split among a plurality of smaller parallel planes at different separation distances from the planar array of light-sensing elements. Depending on the spatial arrangement, some portions of some of the smaller parallel planes can be observationally occulted from some regions of the planar surface. Note the roles of the plurality of planar arrays of light source elements and a parallel array of light-sensing elements can be interchanged.

Case E: Combinations of at Least One Parallel Planes and at Least One Non-Multiple Parallel Plane:

Generalizing in Case D further, one or more instances of the situations of Case A and Case B are combined, resulting in a more complex light-field. In many situations occultation of portions of light fields can occur, for example in cases where one non-transparent source array blocks at least a portion of the light emitted by another source array as viewed by (one or more of the) sensor array(s).

As an illustration of Case E, FIGS. **31***a* and **31***b* depict a variety of illustrative 3-dimensional views of an example variation of the arrangement depicted in FIGS. **24**, **25***a*, **25***b*, **26***a*, and **25***b* wherein the array of (emitted and/or reflected) light source elements are distributed over a connected group of planes, at least one parallel to the planar array of light-sensing elements. Depending on the spatial arrangement, some portions of some of the non-parallel planes can be observationally occulted from some regions of the planar surface. Note the roles of the plurality of planar arrays of light source elements and a parallel array of light-sensing elements can be interchanged.

Case F: More Complex Combinations of Mixed Discrete and Continuous Spatially-Varying Separation Distances:

Generalizing in Case E further, one or more instances of 25 the situations of at least one of Case A and Case B are combined with at least one instance of the situation of Case C, resulting in yet a more complex light-field. In many situations occultation of portions of light fields can occur, for example in cases where one non-transparent source array 30 blocks at least a portion of the light emitted by another source array as viewed by (one or more of the) sensor array(s).

As an illustration of Case F, FIGS. **32***a* through **32***c* depict a variety of illustrative 3-dimensional views of an example 35 wherein the array of (emitted and/or reflected) light source elements are distributed over a complex collection of connected and disconnected planes, some of which are parallel to the planar array of light-sensing elements, and some of which observationally occulted others from some regions of 40 the planar surface by being situated directly in front of others. Note the roles of the plurality of planar arrays of light source elements and a parallel array of light-sensing elements can be interchanged.

FIGS. 33a and 33b depict example inward-directed or 45 outward-directed sensor-pixel lattice locations distributed on a rigid or elastic curved convex-shaped surface. As considered elsewhere, leveraging the co-integration of lightemitting and light-sensing elements as taught in the inventor's 1999 patent family, the camera can be configured to 50 provide self-illumination, for example when used as an elastically-fitted cap that serves as a zero-separation-distance contact-imaging camera monitoring the surface of an enclosed object. As explained elsewhere, since an arbitraryshaped "focus-surface" can be computationally defined, 55 should the elastic cap only make contact with some portions of an object enshrouded by such a (self-illuminating if needed) elastic cap, focused images of the entire encapsulated region of the non-occulted surface of the enshrouded object can be produced.

FIGS. **34***a* through **34***d* depicts examples of pairs of curved and sharply-angled surfaces, one of the pair inside the other of that pair. In any of the arrangements depicted, at least one of the inner surface and the outer surface can be a camera arranged to view the other surface. As considered 65 elsewhere, the camera can be configured to provide self-illumination.

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FIGS. 35a through 35c depict illustrative examples of bumpy and/or pitted sensor surfaces that can provide angular diversity. Such arrangements can also be used to provide sensor robustness via spatial diversity, to provide directed angle-orientation viewing, and to provide other types of functions.

FIG. 36 depicts example correspondences between a physical optical arrangement comprising an optical process (including for example vignetting optics and free-space separation should the image sensor not be in contact with the actual source image) and a mathematical model of that physical optical arrangement (transforming an actual image array data to measured image array data by a numerical model of the optical process.

FIG. 37 depicts an illustrative example of Mathematical Recovery of an approximate representation of the actual Image from Measured Image Array Data obtained by operating on the Measured Image Array Data by a Numerical Inverse of the Model of the Optical Process as depicted in FIG. 36.

FIG. 38, adapted from FIG. 2b of the present inventor's U.S. Pat. No. 8,830,375 and related cases, depicts an exemplary embodiment comprising a micro-optic structure, a light sensor array, an image formation signal processing operation and an optional additional subsequent image processing operations, herein the micro-optic structure and light sensor array are grouped into a first subsystem, and the image formation signal processing operation and subsequent image processing operations are grouped into a second subsystem. As discussed in the present inventor's U.S. Pat. No. 8,830,375 and related cases, various other arrangements are possible and provided for by aspects of the invention.

FIG. **39***a* depicts an example scheme wherein manufacturing, physical, optical, and mathematical considerations are used to create a reproducible manufacturing design such that is adequate manufacturing tolerances are obtained an analytical predictive model can be used to produce numerical models of the optical situations to be recovered without the use of empirical measurements.

FIG. **39***b* depicts an example variation on the scheme presented in FIG. **39***a* wherein post-manufacturing empirical measurements are used to further fine-calibrate the system performance of each particular manufactured article.

FIG. **40** depicts an example representation of example serialization processes and de-serialization processes for image recovery from an inverse or pseudo-inverse model as provided for by the invention.

FIG. 41 depicts a representation of example serialization processes transforming a measured image produced by a light-field travelling through an optical structure (here a vignette array) at being measured by a sensor array.

FIG. 42 depicts a representation of example empirical image-basis "training" sequence, or alternatively a collection of predictive-model-generated image-bases that directly populate a JK×NM matrix providing a numerical model of the optical environment from which a future image will later be recovered as provided for by aspects of the invention.

FIG. **43***a* depicts a representation of example image recovery process using an inverse square-matrix represent-60 ing an approximate inverse model as provided for by the invention.

Generalized Inverse/Pseudo-Inverse Remarks

There are a number of types of generalized inverses that have been developed and surveyed in the literature; for example see [B9] Section 3.3, [B10] pp. 110-111, and the tables in [B11] pp. 14-17. Some types of generalized inverses are uniquely-defined while others are non-uniquely

defined in terms of infinite families. The notion of a generalized inverse applies to not only to finite-dimensional matrices but more broadly to (infinite-dimensional) linear operators; see for example [B12].

The Moore-Penrose generalized inverse, a special case of 5 the Bjerhammar "intrinsic inverses" (see [B10] p. 105 and [P1], is uniquely-defined ([B13] p. 180), exists for any rectangular (or square) matrix regardless of matrix rank ([B13] p. 179, [B14] p. 196, [B15] p. 19) and provides many properties found in matrix inverse ([B14], p. 196) and 10 beyond.

In particular, the Moore-Penrose generalized inverse inherently provides a unique solution providing a "Least-Squares" statistical fit in cases where solvable subsets of the larger number of equations give different inconsistent solutions; see for example [B15] pp. 17-19.

There are other types of generalized inverses that also provide least-squares properties; for example see entries annotated (3.1) and (3.2) in the table pp. 14 as well as sections 3.1-3.2 of [B11] as well as section 4.4.1 of [B13]. 20

Further, the Moore-Penrose generalized inverse can be used to determine whether a solution to a set of linear equations exists ([B13] pp. 190-191).

Various extended definitions and generalized forms of the Moore-Penrose generalized inverse exist; see for example 25 section 4.4.3 of [B13].

Some of the other types of generalized inverses are not useful for solving over-specified systems of linear equations (more equations than variables), for example the Drazin inverse which is restricted to square matrices and has more 30 abstract applications; see for example [B13] Section 5.5.

FIG. 43b depicts a representation of example image recovery process using a generalized-inverse or pseudoinverse matrix representing an approximate pseudo-inverse underspecified model as provided for by the invention. 35 Underspecified arrangements have been of interest in sub-Nyquist rate "compressive sampling" which can also be applied more broadly than optical sensing (see for example [P60]), and naturally fit into the classical regularized illposed inverse problem paradigm employed endemically in 40 the coded aperture lensless imaging systems and approaches reviewed in review section A at the opening of the present patent application. The regularized ill-posed inverse problem paradigm gives rise to Moore-Penrose pseudo-inverse matrices or matrices similar to those (as presented in [P4] for 45 example). Additionally, it is noted that the Moore-Penrose pseudo-inverse matrices and some of the other types of generalized inverse matrices can provide "best-fit" (Least square error) solutions to underspecified (fewer numbers of measurements than needed to uniquely solve for an image), 50 fully-specified (exactly the number of measurements needed to uniquely solve for an image), and overspecified (fewer numbers of measurements than needed to uniquely solve for an image) situations and arrangements. However, the use of the Moore-Penrose pseudo-inverse matrices and other types 55 of generalized inverses as taught in the inventor's 2008 patent family are directed to deliver additional advantages for pre-designed overspecified measurement situations and not the result of the regularized ill-posed inverse problem paradigm now widely used in coded aperture imaging and 60 many other types of optical systems design and analysis see for example [B5], [B6]).

FIG. **43**c depicts a representation of example image recovery process using a generalized-inverse or pseudo-inverse matrix representing an approximate generalized-inverse or pseudo-inverse overspecified model as provided for by the invention.

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Use of a generalized-inverse or pseudo-inverse (and use of the Moore-Penrose pseudo-inverse in particular) in solving for a "best-fit" image from overspecified (and likely inconsistent) measurement data was introduced in a 2008 inventor's patent family. It is noted that slightly-related work in the area of improving digital Image resolution by use of "oversampling" can be found in the far earlier publication by Wiman [P3], but that is a different idea and goal. Rather, the inventor's use of use of a generalized-inverse or pseudo-inverse (and Moore-Penrose pseudo-inverse in particular) in solving for a "best-fit" image from overspecified (and likely inconsistent) measurement data provides robustness of image recovery with respect to damage or occultation of portions of the image sensor, etc.

FIG. 44a depicts a simple computational approach for image recovery as provided for by the invention, for example as taught in the inventor's 1999 and 2008 patent families. Such a depicts a simple computational approach compares favorably with far more numerically-complex spectral or transform computation (which numerically amounts to additional basis rotation transformation steps) as would be used in spectral or transform methods. For comparison, FIG. 44b depicts an example representation of a far more numerically-complex spectral or transform computation (which numerically amounts to additional basis rotation transformation steps) as would be used in spectral or transform methods.

The inventor's comprehensive lensless light-field imaging program (beginning with the inventor's 1999 patent family) includes a framework covering the approaches depicted in FIGS. **44***a* and **44***b* and various situations leading to these such as deconvolution methods. It is the inventor's view that the inventor's comprehensive lensless light-field imaging program (beginning with the inventor's 1999 patent family) includes a framework admitting most of visual-light coded aperture and angular-selective light-sensor approaches to various degrees.

FIG. 44c depicts a comparison of the approach depicted in FIG. 44a and the approach depicted in FIG. 44b, demonstrating comparative reasons to reject the far more numerically-complex spectral or transform computational approached represented in FIG. 44b.

FIG. **45** depicts the use of classical ill-posed inverseproblem regularization methods as employed in the Rambus [P4] and Rice University "Flat Cam" [P5] implementations as well as other coded aperture imaging implementations. These classical ill-posed inverse-problem regularization methods are widely used in many areas but also have an established role in optical systems design and analysis; see for example [B5] and [B6].

FIG. **46** depicts an abstract representation of an "Identity structure" within a (necessarily-sparse) Identity 4-tensor.

FIG. **47** depicts an abstract representation of a dilation around the "Identity structure" within a (necessarily-sparse) Identity 4-tensor.

FIG. **48** depicts a $((7\times7)\times(7\times7))$ "matrix-of-matrices" representation of a $(7\times7\times7\times7)$ Identity 4-tensor as abstracted in FIG. **46**.

FIG. **49** depicts an example $((7\times7)\times(7\times7))$ "matrix-of-matrices" representation of the dilation around the "Identity structure" of a $(7\times7\times7\times7)$ 4-tensor as abstracted in FIG. **46**.

FIG. **50** depicts an abstract representation of the trade-off between Space/Inverse-Space/Spatial Frequency Localization Methods and the sparcity of numerical model tensors, matrices, and their inverses.

FIGS. 51a through 51e depict how the sparcity of an example numerical model matrix serializing a numerical

model 4-tensor degrades as the image source moves farther and farther from the image sensor (using numerical models at each distances predicted by an analytical geometric predictive model provided for by the invention).

FIG. **52** depicts an example $((7\times7)\times(7\times7))$ "matrix-of-5 matrices" representation of the numerical model 4-tensor and example measured image (right) at zero separation distance from a single-illuminated-pixel source image (left). As described elsewhere, the source image need not be on a parallel plane and can be distributed arbitrarily in space.

FIG. 53 depicts an example $((7\times7)\times(7\times7))$ "matrix-of-matrices" representation of the numerical model 4-tensor and example measured image (right) at a small non-zero separation distance from the same single-illuminated-pixel source image (left) as in FIG. 52.

FIG. **54** depicts an example $((7\times7)\times(7\times7))$ "matrix-of-matrices" representation of the numerical model 4-tensor and example measured image (right) at zero separation distance from a two-illuminated-pixel source image (left). As described elsewhere, the source image need not be on a 20 parallel plane and can be distributed arbitrarily in space.

FIG. 55 depicts an example $((7\times7)\times(7\times7))$ "matrix-of-matrices" representation of the numerical model 4-tensor and example measured image (right) at a small non-zero separation distance from the same two-illuminated-pixel 25 source image (left) as in FIG. 54.

FIG. **56** depicts an example $((7\times7)\times(7\times7))$ "matrix-of-matrices" representation of the numerical model 4-tensor and example measured image (right) at zero separation distance from a more closely-spaced two-illuminated-pixel 30 source image (left). As described elsewhere, the source image need not be on a parallel plane and can be distributed arbitrarily in space.

FIG. 57 depicts an example $((7\times7)\times(7\times7))$ "matrix-of-matrices" representation of the numerical model 4-tensor 35 and example measured image (right) at a small non-zero separation distance from the same more closely-spaced two-illuminated-pixel source image (left) as in FIG. 56.

FIGS. **58***a* through **58***c* depict three of forty-nine steps of an example empirical training sequence as provided for by 40 the invention. In an implementation of the invention, such a procedure could be performed for a selected collection of one or more separation distances between the image sensor and the source image. As described elsewhere, the source image need not be on a parallel plane and can be distributed 45 arbitrarily in the observable space.

Lensless Light-Field Imaging as an Associated Inverse Problem

The Inverse Model depiction illustrated in FIG. 1 can be configured to, in some appropriate manner, undo the effects of the incoming light's optical travel first within the Light-Field preceding the optical structure(s) and then through the Lensless Optical Structure(s) to where it reaches the Optical Sensor where the incident light converted to an electrical signal that can be further processed. If a mathematical model is a close match to the composite effects of these optical and optoelectrical processes, and if the model is mathematically invertible, applying the inverse of the model to the measured data can create a computationally-produced image which, for example, can be further arranged to be useful for human or machine use.

The Inverse Model can, for example, be implemented as a matrix, a 4-tensor, or other mathematical and/or data and/or logical operation.

The Inverse Model can be fixed or adjustable, can be 65 implemented in a lumped or distributed manner, and can be unique or variationally-replicated in various manners. The

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optical structure can be fixed or reconfigurable, and can be arranged to be in a fixed position with respect to the Optical Sensor or can be configured to be movable in some manner with respect to the Optical Sensor. Additionally, at this level of abstraction, one or both of the Optical Sensor and Lensless Optical Structure(s) themselves can be variable in their electrical, physical, optical, mechanical, and other characteristics. For example, one or both of the Optical Sensor and Lensless Optical Structure(s) themselves can be any one or more of flat, curved, bendable, elastic, elastically-deformable, plastically-deformable, etc.

The Inverse Model can be derived from analytical optical models, empirical measurements, or combinations of these. In some embodiments the Inverse Model can be parametrized using interpolation.

Interpolation-based parameterization can be particularly useful if the Inverse Model is based on a collection of selected empirical measurements, or if the analytical optical model involves complex numerical computations.

FIG. **59** depicts an example polynomial fitting function interpolation method for interpolating the numerical model, its inverse/pseudo-inverse, and/or other functions for separation distances values lying between k empirically-trained separation distances. As described elsewhere, the source image need not be on a parallel plane and can be distributed arbitrarily in the observable space. In general the polynomial fitting function can be expected to include terms with negative exponential powers expected due to the overall "1/r²" enveloping attention as the serration distance "r" increases.

FIG. **60** depicts an example polynomial fitting function interpolation method for interpolating the numerical model, its inverse/pseudo-inverse, and/or other functions for separation distances values lying between k separation distances used by a predictive-model. As described elsewhere, the source image need not be on a parallel plane and can be distributed arbitrarily in the observable space. Hereto in general the polynomial fitting function can be expected to include terms with negative exponential powers expected due to the overall " $1/r^2$ " enveloping attention as the serration distance "r" increases.

FIG. **61** depicts an example of very poor curve-fit interpolation of the matrix elements of the numerical model between measure data distances resulting from not having sufficient terms in a model polynomial expansion and/or inclusion of terms with negative exponential powers expected due to the overall "1/r²" enveloping attention as the serration distance "r" increases.

FIG. **62** depicts an example piecewise-linear interpolation of the matrix elements of the numerical model between k empirically-trained separation distances. (Measurement data and piecewise-linear plot made by Michael Hörlng.)

Using an empirically-trained numerical model for representing the linear transformation invoked by the optical arrangement, it is clearly possible to train the system to focus on an arbitrarily-shaped surface, including one that is curved, bend, or irregularly-shaped; the inversion math "does not care" as long as the resulting numerical model matrix is non-singular, and the recovered image will be obtained in the same manner as if the focus-surface was a parallel plane. Accordingly, in principle a predictive analytical model can be used to generate the numerical model matrix, and by either means (empirically-trained or predictively-modeled) the system and methods can be arranged to focus on an arbitrarily-shaped surface, including one that is curved, bend, or irregularly-shaped.

FIG. **63***a* depicts how with very small separation distances and certain non-alignment of source-pixel locations and sensor pixel locations some sensor pixel locations cannot receive light from proximate source-pixel locations, while FIG. **63***b* depicts how at slightly greater separation 5 distances this condition does not occur; such processes can give rise to the rising and falling of selected curves in the example empirical training data shown in the example of FIG. **61**. (This analysis performed by Michael Hörlng.)

FIG. **64** depicts an example piecewise-linear interpolation 10 method for interpolating the numerical model, its inverse/pseudo-inverse, and/or other functions for separation distances values lying between k empirically-trained separation distances. As described elsewhere, the source image need not be on a parallel plane and can be distributed arbitrarily 15 in the observable space.

FIG. **65** depicts an example piecewise-linear interpolation method for interpolating the numerical model, its inverse/pseudo-inverse, and/or other functions for separation distances values lying between k separation distances used by 20 a predictive-model. As described elsewhere, the source image need not be on a parallel plane and can be distributed arbitrarily in the observable space.

FIG. **66** depicts an abstract representation of the mathematical recovery of image from measured image array data. 25

FIG. 67 depicts a variation on the representation of the mathematical recovery of image from measured image array data shown in FIG. 66 wherein more measurements are made than needed, resulting in an over-specified collection of measurements that can be expected to lead to inconsistent 30 calculation outcomes when different subgroups of measurements are used to solve for the recovered image. As provided for by the invention, a Moore-Penrose pseudo-inverse operation gives a least-squares fit to the expected inconsistent outcomes; this is depicted in the bottom portion of the 35 figure.

FIG. **68***a* through **68***d* depict example numerical model outcomes responsive to a single-illuminated pixel as generated for various separation distances by an example predictive analytical geometric model. The particular example 40 predictive analytical geometric model used only accounts for vignette occultation as calculated by simple ray-trancing and does not include the effects of vignette-internal reflections, vignette-internal scattering, vignette-aperture diffraction, surface plasmoid propagation, etc.

FIG. **69***a* depicts three example interactive quantization-effect modeling outcomes wherein controllable quantization is artificially imposed on measurement data so as to predictively model and characterize the effects of quantizing nonlinearities imposed by electronic digital-to-analog converter processes on empirical training, predictive-model generated, and real-time measurements as they influence the quality of image recovery.

FIG. **69***b* depicts three example interactive offset-effect modeling outcomes wherein controllable measurement offset is artificially imposed on measurement data so as to predictively model and characterize the effects of measurement offsets imposed by electronic digital-to-analog converter processes on empirical training, predictive-model generated, and real-time measurements as they influence the 60 quality of image recovery.

There are many noise processes inherent to light sensing and associated electronics and various resulting performance limitations and tradeoffs; see for example [P44], [B2]. A very general performance perspective is provided in 65 the book by Janesick [B2]. In the limit, highest performance will be obtained by single-electron sensors and amplifies; as

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to steps towards array sensors of this type see the paper by Richardson [P33]. The invention provides for inclusion of these considerations. FIG. **69**c depicts an example interactive noise-modeling control used to introduce syntheticallygenerated noise and noise processes so as to predictively model and characterize its effects. The selection shown controls additive Gaussian noise, but other noise processes associated with photodiodes (1/f noise, dark-current shot (Poissonian) noise, photon shot (Poissonian) noise, Johnson and other circuit noise, dark-current thermal noise, spectral noise, detector amplifier noise, etc.) can similarly be introduced.

FIGS. **70***a* through **70***d* depict example interactive modeling outcomes showing the effect of noise, offset, and both these for a 32-step (5-bit) quantized ("DN" [B2]) measurement dynamic range.

FIGS. 71a through 71d depict example interactive modeling outcomes showing the effect of noise, offset, and both these for a 64-step (6-bit) quantized ("DN") measurement dynamic range.

FIGS. 72a through 72d depict example interactive modeling outcomes showing the effect of noise, offset, and both these for a 128-step (7-bit) quantized ("DN") measurement dynamic range.

FIGS. 73a through 73d depict example interactive modeling outcomes showing the effect of noise, offset, and both these for a 140-step (slightly more than 7-bit) quantized ("DN") measurement dynamic range.

FIGS. 74a through 74d depict example interactive modeling outcomes showing the effect of noise, offset, and both these for a 150-step (yet more than 7-bit) quantized ("DN") measurement dynamic range.

FIG. 75a, adapted from [B7] Figure C2.5.16(a), depicts a first example pixel-cell multiplexed-addressing circuit for an individual OLED within an OLED array that includes a dedicated light-coupled monitoring photodiode for use in regulating the light output of the individual OLED so as to prevent user-observed fading or other brightness-variation processes. The adjacent photodiodes used for pixel-by-pixel closed-loop feedback of OLED brightness.

FIG. 75b, adapted from [B7] Figure C2.5.16(b), depicts a second example pixel-cell multiplexed-addressing circuit for an individual OLED within an OLED array that includes a dedicated light-coupled monitoring photodiode for use in regulating the light output of the individual OLED so as to prevent user-observed fading or other brightness-variation processes. There are many other subsequent developments since the publishing of this books tentatively-toned remarks; for example recently-announced OLED phones are said to be using this technique.

FIG. **76***a*, adapted from [B18], depicts an example pixelcell multiplexed-addressing circuit for an individual OLED within an OLED array with a monitoring feature.

FIG. **76***b*, also adapted from [B18], depicts an example pixel-cell multiplexed-addressing circuit for an isolated high-performance photodiode or phototransistor within a high-performance photodiode or phototransistor array with a forced-measurement provision.

Additional Functional Architectures

As descried earlier, FIG. 1 depicts an example conceptual view of the underlying principles of the invention, facilitating a wide range of implementation methods and architectures. In this depiction, an Optical Scene creates a Light-Field that is directed to an Optical Sensor which is preceded by one or more Lensless Optical Structure(s) that in some manner alters the light field in a predictable spatial manner. The Optical Sensor produces (typically time-varying) elec-

trical signals and/or computational data responsive (instantly and/or within some time-delay) to light incident to the surface or other substructure(s) within the Optical Sensor at any given moment. The depicted Inverse Model can be configured to, in some appropriate manner, undo the effects 5 of the incoming light's optical travel first within the Light-Field preceding the optical structure(s) and then through the Lensless Optical Structure(s) to where it reaches the Optical Sensor, resulting in a computationally-produced image which, for example, can be arranged to be useful for human 10 or machine use. The Inverse Model can, for example, be implemented as a matrix, a 4-tensor, or other mathematical and/or data and/or logical operation. The Inverse Model can be fixed or adjustable, can be implemented in a lumped or distributed manner, and can be unique or variationally- 15 replicated in various manners. The optical structure can be fixed or reconfigurable, and can be arranged to be in a fixed position with respect to the Optical Sensor or can be configured to be movable in some manner with respect to the Optical Sensor. Additionally, at this level of abstraction, one 20 or both of the Optical Sensor and Lensless Optical Structure(s) themselves can be variable in their electrical, physical, optical, mechanical, and other characteristics. For example, one or both of the Optical Sensor and Lensless Optical Structure(s) themselves can be any one or more of 25 flat, curved, bendable, elastic, elastically-deformable, plastically-deformable, etc.

FIG. 77 depicts a simplified view of FIG. 1 showing only the signal and computational portion of FIG. 1 as will be useful in a subsequent discussion. It is understood that in 30 FIG. 77 and related figures that the Optical Scene, Light-Field, and Lensless Optical Structure(s) can have the arrangements with respect to the Optical Sensor like that, similar to, extensible from, or in appropriate manners alternative to that depicted in FIG. 1.

FIG. 78 depicts a variation of the arrangement represented in FIG. 77 wherein the Inverse Model is rendered as a parameterized Inverse Model which can be altered responsive to one or more provided parameters. For example, the parameters provided to the parameterized Inverse Model 40 could control a surrogate viewpoint, specify one or more "focus planes" (or more generally "focus surfaces"), etc. rating to what the Inverse Model "undoes." Accordingly, this arrangement allows a plurality of imaging capabilities and functions to be selectably and/or adjustably be supported by 45 the more general arrangement of FIG. 77.

FIG. 79 depicts a variation of the arrangement represented in FIG. 78 wherein the electrical signals and/or computational data produced by the Optical Sensor are in parallel provided in whole or selected (or selectable) part to a 50 plurality of Inverse Models, each producing one or more computationally-produced images responsive to the sensor data. Although the Inverse Models shown in FIG. 79 are depicted as parameterized Inverse Models, the invention provides for some or all of the plurality of Inverse Models 55 to be non-parameterized Inverse Models.

FIG. **80** depicts a variation of the arrangement represented in FIG. **78** wherein the electrical signals and/or computational data produced by the Optical Sensor is handled by a computer or computational element (such as a microprocessor, GPU, DSP chip, ALU, FPLA, combination of two or more these, pluralities of these, etc.) in some fashion that at least permits the electrical signals and/or computational data produced by the Optical Sensor to be stored as a file.

FIG. **81** depicts a variation of the arrangement represented 65 in FIG. **78** wherein the aforementioned handling by a computer or computational element is controlled in some

manner by a control parameter. The control parameter for example can specify an aspect of the name of the Stored File, specify an aspect of the format of the Stored File, specify a selection of specific portions of the electrical signals and/or computational data produced by the Optical Sensor, specify or control data operations on the electrical signals and/or computational data produced by the Optical Sensor, specify or mathematical operations on the electrical signals and/or computational data produced by the Optical Sensor, specify or control logical operations on the electrical signals and/or computational data produced by the Optical Sensor, etc.

FIG. 82a depicts a variation of the arrangement represented in FIG. 81 wherein a plurality of stored files is created, for example with different parameter values associated with each stored file. Although a separate computer function is depicted for each of the stored file, the invention provides for these computer functions to be implemented with or executed on any of a single computer or computational element (such as a microprocessor, GPU, DSP chip, ALU, FPLA, combination of two or more these, pluralities of these, etc.), a plurality of computers or computational elements, an individually-dedicated computer or computational element, etc. The parameter values used in creating each Stored File can be either externally associated with each stored file, or can be stored as part of the stored file in a direct or encoded form.

FIG. **82***b* depicts an example arrangement wherein a stored file is used by a fixed Inverse Model to create a computationally-produced image.

FIG. **82**c depicts an example arrangement wherein a stored file is used by a parameterized Inverse Model to create a computationally-produced image, and further wherein parameter value(s) associated the parameterized Inverse Model are externally associated with each stored file.

FIG. 82d depicts an example arrangement wherein a stored file is used by a parameterized Inverse Model to create a computationally-produced image, and further wherein parameter value(s) associated the parameterized Inverse Model are derived from or obtained from the stored file

FIG. 83 depicts four example conformations of a particular bendable, flexible, and/or or pliable optical-sensor/optical-structure sheet, each conformation giving rise to an associated model for how a light field is sensed in the context of reconstructing an image, and each model giving rise to its own associated inverse model. It is noted that, as dependent on the properties and limitations of the optical-structure, there can be small blind spots in regions of sufficiently-high curvature.

FIG. **84***a* through FIG. **84***d* depict how various conformations can be used to render a computationally derived image

FIG. **85***a* depicts an example arrangement for an optical-sensor/optical-structure of fixed conformation.

FIG. **85***b* depicts an example arrangement for an optical-sensor/optical-structure of variable conformation, for example should the surface bend, deform, hinge, expand, contract, etc.

FIG. **85**c depicts a variation of FIG. **85**b wherein the model and the Inverse Model are parameterized.

FIG. **86***a* depicts an arrangement useful for using optical training to sense the present conformation of an optical-sensor/optical-structure of variable conformation, for example should the surface bend, deform, hinge, expand, contract, etc.

FIG. 86b depicts an arrangement useful for using internal sensing means to sense the present conformation of an optical-sensor/optical-structure of variable conformation, for example should the surface bend, deform, hinge, expand, contract, etc. It is noted that a prototype for a commercial (panoramic camera) product employing a flexible OLED display, (c) conformation deformation sensing has been presented and is described in [P36].

FIG. 86c depicts an arrangement useful for using information about a movable or changing support structure or contact arrangement to identify the present conformation of an optical-sensor/optical-structure of variable conformation, for example should the surface bend, deform, hinge, expand, contract, etc.

FIG. **86**d depicts an arrangement useful for using external observation mean, for example such as one or more observing video camera(s) means to sense the present conformation of an optical-sensor/optical-structure of variable conformation, for example should the surface bend, deform, 20 hinge, expand, contract, etc.

FIG. 87a depicts an optical-sensor/optical-structure of variable conformation, for example should the surface bend, deform, hinge, expand, contract, etc. producing an output signal and/or output data.

FIG. 87b depicts a controllable variable-conformation material whose shape/conformation can be controlled by externally-provide control stimulus.

FIG. 87c depicts an optical-sensor/optical-structure of variable conformation, for example should the surface bend, deform, hinge, expand, contract, etc. producing an output signal and/or output data fabricated on, with, or co-integrated with controllable variable-conformation material whose shape/conformation can be controlled by externallyprovide control stimulus.

FIG. 88a depicts use of conformational sensing information to derive or compute parameter values for a parameterized Inverse Model.

FIG. **88***b* depicts use of conformational control parameter 40 J-dimensional column vector y is given by information to derive or compute parameter values for a parameterized Inverse Model.

FIG. 88c depicts use of both conformational sensing information and conformational control parameter information to derive or compute parameter values for a parameter- 45 ized Inverse Model.

Imaging Algorithms

The development to follow is broad enough to cover a wide variety of sensor types and imaging frameworks, and can be expanded further. Although the development to 50 follow readily supports the advanced features made possible by curved, flexible/bendable, transparent, light-emitting, and other types of advanced sensors taught in the present patent application and earlier inventor patent families, many of the techniques can be readily applied to appreciate optical 55 arrangements, devices, and situations employing traditional image sensors such as CMOS, CCD, vidicon, etc. Accordingly, the present invention provides for the use of a wide range of image sensor types including CMOS, CCD, vidicon, flat, curved, flexible/bendable, transparent, light-emitting, and other types of advanced sensors taught in the present patent application and earlier inventor patent families, as well as other know and future types of image sensors. Traditional Notation Conventions for Vectors, Matrices, and Matrix-Vector (Left) Multiplication

Let x be an M-dimensional column vector (i.e., an array of dimension 1×M) comprising elements $\{x_m\}$ 1≤m≤M

$$x = \begin{bmatrix} x_1 \\ \vdots \\ x_M \end{bmatrix}$$

and y be a J-dimensional column vector (i.e., an array of dimension $1\times M$) comprising elements $\{y_i\}1\le j\le J$

$$y = \begin{bmatrix} y_1 \\ \vdots \\ y_J \end{bmatrix}$$

Let A be a J×M matrix (an array of dimension J×M) comprising elements $\{a_{jm}\}$, $1 \le j \le J$, $1 \le m \le M$:

$$A = \begin{bmatrix} a_{11} & \dots & a_{1K} \\ \vdots & \ddots & \vdots \\ a_{J1} & \dots & a_{JK} \end{bmatrix}$$

The "matrix product" of a J×M matrix A with an M-dimensional column vector x can produce a J-dimensional column vector y; by "left multiplication" convention this is denoted as

$$y=$$

where each element y, of resulting a J-dimensional column vector y is calculated as

$$y_j = \sum_{m=1}^{M} a_{jm} x_m$$

for each j an integer such that 1≤j≤J. Then the entire a

$$y = \begin{bmatrix} y_1 \\ \vdots \\ y_J \end{bmatrix} = \begin{bmatrix} \sum_{m=1}^{M} a_{1m} x_m \\ \vdots \\ \sum_{m=1}^{M} a_{Jm} x_m \end{bmatrix}$$

Use to Represent Spatial Line-Array (1-Dimensional) Imaging (as Used in Fax and Spectrometry Sensors)

In the above, one is using the matrix A as a transformational mapping from column vector x to column vector y

$$x \stackrel{A}{\rightarrow} y$$

60 analogous 4-Tensor Representation of Spatial Grid-Array (2-dimensional) Imaging.

For example, if column vector x represents a line-array of data (such as light source values directed to a line-array light-measurement sensor used in a fax scanner or optical spectrometer), the matrix A can represent a composite chain of linear optical processes, electro-optical processes, and interface electronics (transconductance, transimpedance,

amplification, etc.) processes that result in measured data represented by a column vector y. Here the indices of the vectors and matrix signify unique well-defined discrete (step-wise) spatial positions in an underlying 1-dimensional spatial structure.

A visual image as humans experience it through vision and conventional photography, as well as other analogous phenomena, has an underlying 2-dimensional spatial structure. In digital imaging, unique well-defined discrete (stepwise) spatial positions within an underlying 2-dimensional spatial structure are identified and/or employed—in the context of this discussion these may be called "pixels."

Mathematically, a 2-dimensional array of mathematically-valued elements, such as a matrix, can provide a mathematical representation of an image wherein the indices of an element identify an individual pixel's spatial location and the value of that mathematical element represents the "brightness" of that pixel. For example, an J×K array of measured 2-dimensional image data arranged as row and 20 columns can be represented as a matrix of "brightness" values:

$$Q = \begin{bmatrix} q_{11} & \dots & q_{1K} \\ \vdots & & \vdots \\ q_{J1} & \dots & q_{JK} \end{bmatrix}$$

A convenient shorthand for this can be denoted as

$$Q = \{q_{ik}\}$$

where it is understood each of the two indices span a range of consecutive non-zero integer values

$$1 \le j \le J$$
, $1 \le k \le K$.

Similarly, a source image (2-dimensional array) can be represented as a matrix:

$$S = \begin{bmatrix} s_{11} & \dots & s_{1N} \\ \vdots & & \vdots \\ s_{M1} & \dots & s_{MN} \end{bmatrix}$$

A similar convenient shorthand for this is denoted

$$S = \{s_{mn}\}$$

where it is understood each of the two indices span a range 50 of consecutive non-zero integer values

$$1 \le m \le M$$
, $1 \le n \le N$.

A source image S can be transformed by linear optical 55 would be: processes, linear sensor processes, and linear electronics processes into a measured image Q. This can be represented mathematically as a linear matrix-to-matrix transformation \mathbb{T} mapping the matrix S to the matrix Q

$$S \xrightarrow{\mathbb{T}} Q$$

akin to employing the earlier matrix A as a linear vector- 65 to-vector transformational (for example, mapping column vector x to column vector y):

 $x \stackrel{A}{\rightarrow} y$

Most generally this linear transformation \mathbb{T} can be represented by a 4-dimensional array 4-tensor:

$$\mathbb{T=}\{t_{jkmn}\}$$

 $1 \le j \le J$

 $1 \le k \le K$

 $1 \le m \le M$

 $1 \le n \le N$

 15 with the understanding that the following multiplication rule is represented by the tensor \mathbb{T} "multiplying" the matrix S, namely each element q_{ik} of resulting matrix Q is given by

$$q_{jk} = \sum_{m=1}^{M} \sum_{n=1}^{N} t_{jkmn} s_{mn}$$

25 Note this convention corresponds in form to the matrix case presented earlier:

$$y_j = \sum_{k=1}^K a_{jk} x_k$$

 $1 \le k \le K$

The corresponding "multiplicative" product of the 4-tensor T with matrix S to give matrix Q can be represented as $O = \mathbb{T}_S$

which compares analogously to the "multiplicative" product 40 of the matrix A with the vector x to give the vector y

$$y=Ax$$

With its four tensor-element indices and tensor-matrix product organized in this way, the 4-tensor T with elements t_{jkmn} can be readily and conveniently represented as a matrix-of-matrices where interior matrix blocks are indexed by row j and column k and the elements with each of the interior matrices are indexed by row m and column n. More specifically, the 4-tensor element t_{ikmn} resides in an inner matrix residing in row m and column n of an inner matrix that resides in row j and column k of the outer matrix. The resulting matrix-of-a-matrices representation for the 4-tensor $\mathbb{T} = \{t_{jkmn}\}$ with

$$1 \le j \le J$$
, $1 \le k \le K$, $1 \le m \le M$, $1 \le n \le N$

60

$$\mathbf{T} = \begin{bmatrix} \begin{bmatrix} t_{1111} & \dots & t_{111N} \\ \vdots & \ddots & \vdots \\ t_{11M1} & \dots & t_{11MN} \end{bmatrix} & \dots & \begin{bmatrix} t_{1K11} & \dots & t_{1K1N} \\ \vdots & \ddots & \vdots \\ t_{1KM1} & \dots & t_{1KMN} \end{bmatrix} \\ & \vdots & & \vdots \\ \begin{bmatrix} t_{J111} & \dots & t_{J11N} \\ \vdots & \ddots & \vdots \\ t_{J1M1} & \dots & t_{J1MN} \end{bmatrix} & \dots & \begin{bmatrix} t_{JK11} & \dots & t_{JK1N} \\ \vdots & \ddots & \vdots \\ t_{JKM1} & \dots & t_{JKMN} \end{bmatrix} \end{bmatrix}$$

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This matrix-of-a-matrices structure where the mapping

$$S \xrightarrow{\mathbb{T}} O$$

is defined by

$$q_{jk} = \sum_{m=1}^{M} \sum_{n=1}^{N} t_{jkmn} \, s_{mn}$$

$$1 \leq j \leq J, \, 1 \leq k \leq K.$$

provides several important opportune outcomes, among these being:

Property:

The individual entries t_{jkmn} of each interior matrix having block-position index $\{j, k\}$ scale the contribution of 20 each element s_{mn} , which sum together to the quantity q_{jk} comprised within the matrix Q; this can be seen directly by just considering fixed values for $\{j, k\}$ in the defining relation

$$q_{jk} = \sum_{m=1}^{M} \sum_{n=1}^{N} t_{jkmn} \, s_{mn}$$

Utility:

this is also the way MatrixForm[*] displays the 4-array $\mathbb T$ in Mathematica.TM

Remark 1: It is noted that the 4-tensor \mathbb{T} as defined thus $_{35}$ far is represented in this "matrix of matrices" structure, the interior matrices are organized so that each interior matrix having block-position index {j,k} is associated with the corresponding outcome quantity q_{jk} . An attractive property of this representation, as called out above, is that the value 40 of the output quantity q_{jk} is the sum of all the pointwise products of values of source image pixels s_{mn} scaled by the corresponding elements in the interior matrix that has blockposition index $\{i, k\}$. Thus, in an optical imaging context, the values of elements in the interior matrix that has blockposition index {j, k} graphically show the multiplicative "gain" (or "sensitivity") attributed to each of the samepositioned source image pixels s_{mn} in the image source matrix S. In more pedestrian but intuitively useful terms, the values of elements in the interior matrix that has blockposition index {j,k} display the "heat map" of responsiveness of an observed or measured sensor pixel q_{jk} in the observed or measured image matrix Q to source image pixels s_{mn} in the image source matrix S.

Remark 2: From this it is further noted that other kinds of 4-tensors could be reorganized in other ways that have other attractive merits. For example, a 4-tensor Ψ comprising elements ψ_{mnjk} can be defined by the simple index reordering

$$\psi_{mnjk} = t_{jkmn}$$
;

each interior matrix in the "matrix of matrices" structure for the 4-tensor Ψ having block-position index $\{m,\,n\}$ represents a discrete "point-spread function" for a source pixel at $_{65}$ position $\{m,\,n\}$ into individual outcome pixels at position $\{j,\,k\}$ as can be seen from the resulting relation

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$$q_{jk} = \sum_{m=1}^{M} \sum_{n=1}^{N} \psi_{mnjk} \, s_{mn}$$

Although "point-spread function" representation imposed by the "matrix of matrices" structure for 4-tensor Ψ has obvious customary attraction, the discourse will continue in terms of the 4-tensor $\mathbb T$ comprising elements $\mathbf t_{jkmn}$ as defined by

$$q_{jk} = \sum_{m=1}^{M} \sum_{n=1}^{N} t_{jkmn} s_{mn}$$

because of its organizational similarity with the conventional matrix definition

$$y_j = \sum_{k=1}^K a_{jk} x_k$$

and with the understanding that all the subsequent development can be transformed from the definitions used for 4-tensor $\mathbb T$ to the "point-spread" oriented for 4-tensor Ψ by the index re-mapping

$$\psi_{mnjk}=t_{jkmn}$$
.

Remark 3: It is noted that for a (variables-separable) "separable" two-dimensional transform, such as the two-dimensional DFT, DCT, DST, etc., commonly used in traditional spectral image processing affairs of the j and m indices are handled entirely separate from affairs of the k and n indices, so q_{ik} takes the restricted "variables-separable" form, for example when J=M and K=N

$$q_{ik} = \sum_{m=1}^{M} \sum_{n=1}^{N} d_{jm} d_{kn} s_{mn}$$

in which case

$$t_{jkmn} = d_{jm}d_{kn}$$

For example, for the normalized DFT matrices operating on an image of M rows and N columns, these \mathbf{d}_{jm} and \mathbf{d}_{kn} element are:

$$d_{jm} = \frac{e^{-2\pi i(j-1)(m-1)}}{\sqrt{M}}$$
 and

$$d_{kn} = \frac{e^{-2NI(k-1)(n-1)}}{\sqrt{N}}$$

where $i=\sqrt{-1}$.

60

As another example of other kinds of 4-tensors be reorganized in other ways with attractive merits, a "variables-separable" 4-tensor Φ comprising elements ϕ_{mnjk} can be defined by the simple index reordering

 $\phi_{jmkn} = t_{jkmn}$

which separately associates rows (indexed by j) in matrix Q with rows (indexed by m) in matrix S and separately associates columns (indexed by k) in matrix Q with columns (indexed by n) in matrix S.

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Remark 4: To further illustrate details and develop intuition of the "matrix of matrices" structure, or at least the aforedescribed organization of indices and multiplication rule, one could employ the dimension signifier $(J\times J)\times (M\times N)$. As some examples:

$$\mathbb{T}_{(3\times3)\times(3\times3)} = \begin{bmatrix} I_{1111} & I_{1112} & I_{1113} \\ I_{1121} & I_{1122} & I_{1123} \\ I_{1131} & I_{1132} & I_{1133} \end{bmatrix} \begin{bmatrix} I_{1211} & I_{1212} & I_{1213} \\ I_{1221} & I_{1222} & I_{1223} \\ I_{1231} & I_{1332} & I_{1333} \end{bmatrix} \begin{bmatrix} I_{1311} & I_{1312} & I_{1313} \\ I_{1321} & I_{1322} & I_{1323} \\ I_{1331} & I_{1332} & I_{1333} \end{bmatrix}$$

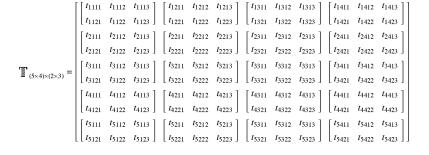
$$\mathbb{T}_{(3\times3)\times(3\times3)} = \begin{bmatrix} I_{2111} & I_{2112} & I_{2113} \\ I_{2121} & I_{2122} & I_{2123} \\ I_{2131} & I_{2132} & I_{2133} \end{bmatrix} \begin{bmatrix} I_{2211} & I_{2212} & I_{2223} \\ I_{2231} & I_{2222} & I_{2223} \\ I_{2231} & I_{2232} & I_{2233} \end{bmatrix} \begin{bmatrix} I_{2311} & I_{2312} & I_{2313} \\ I_{2331} & I_{2332} & I_{2333} \\ I_{2311} & I_{2312} & I_{2313} \\ I_{2312} & I_{2322} & I_{2223} \\ I_{2313} & I_{2322} & I_{2323} \\ I_{2313} & I_{2332} & I_{2333} \end{bmatrix} \begin{bmatrix} I_{2311} & I_{2312} & I_{2313} \\ I_{2321} & I_{2322} & I_{2223} \\ I_{2331} & I_{2332} & I_{2333} \\ I_{233$$

$$T_{(5\times 4)\times (3\times 2)} = \begin{bmatrix} t_{1111} & t_{1112} \\ t_{1121} & t_{1122} \\ t_{1131} & t_{1132} \\ t_{1131} & t_{1132} \end{bmatrix} \begin{bmatrix} t_{1211} & t_{1212} \\ t_{1221} & t_{1222} \\ t_{1231} & t_{1332} \end{bmatrix} \begin{bmatrix} t_{1311} & t_{1312} \\ t_{1321} & t_{1332} \\ t_{1331} & t_{1332} \end{bmatrix} \begin{bmatrix} t_{1411} & t_{1412} \\ t_{1421} & t_{2422} \\ t_{1231} & t_{2132} \end{bmatrix} \begin{bmatrix} t_{2211} & t_{2212} \\ t_{2221} & t_{2222} \\ t_{2231} & t_{2232} \end{bmatrix} \begin{bmatrix} t_{2311} & t_{2312} \\ t_{2331} & t_{2332} \end{bmatrix} \begin{bmatrix} t_{2411} & t_{2412} \\ t_{2421} & t_{2422} \\ t_{2431} & t_{2432} \end{bmatrix}$$

$$T_{(5\times 4)\times (3\times 2)} = \begin{bmatrix} t_{3111} & t_{3112} \\ t_{3121} & t_{3122} \\ t_{3131} & t_{3132} \end{bmatrix} \begin{bmatrix} t_{3211} & t_{3212} \\ t_{3221} & t_{3222} \\ t_{3231} & t_{3332} \end{bmatrix} \begin{bmatrix} t_{3411} & t_{3412} \\ t_{3421} & t_{3422} \\ t_{3331} & t_{3332} \end{bmatrix} \begin{bmatrix} t_{3411} & t_{3412} \\ t_{3421} & t_{3422} \\ t_{3431} & t_{3432} \end{bmatrix}$$

$$\begin{bmatrix} t_{4111} & t_{4112} \\ t_{4122} & t_{4122} \\ t_{4131} & t_{4132} \end{bmatrix} \begin{bmatrix} t_{4211} & t_{4212} \\ t_{4221} & t_{4222} \\ t_{4331} & t_{4332} \end{bmatrix} \begin{bmatrix} t_{4411} & t_{4412} \\ t_{4422} & t_{4422} \\ t_{4431} & t_{4432} \end{bmatrix} \begin{bmatrix} t_{4411} & t_{4412} \\ t_{4422} & t_{4422} \\ t_{4331} & t_{4332} \end{bmatrix} \begin{bmatrix} t_{5411} & t_{5412} \\ t_{5421} & t_{5422} \\ t_{5321} & t_{5322} \end{bmatrix} \begin{bmatrix} t_{5311} & t_{5312} \\ t_{5321} & t_{5322} \end{bmatrix} \begin{bmatrix} t_{5411} & t_{5422} \\ t_{5421} & t_{5422} \\ t_{5321} & t_{5322} \end{bmatrix} \begin{bmatrix} t_{5312} & t_{5322} \\ t_{5331} & t_{5332} \end{bmatrix} \begin{bmatrix} t_{5411} & t_{5422} \\ t_{5421} & t_{5422} \\ t_{5431} & t_{5432} \end{bmatrix} \begin{bmatrix} t_{5411} & t_{5422} \\ t_{5421} & t_{5422} \\ t_{5321} & t_{5322} \end{bmatrix} \begin{bmatrix} t_{5311} & t_{5332} \\ t_{5331} & t_{5332} \end{bmatrix} \begin{bmatrix} t_{5411} & t_{5422} \\ t_{5421} & t_{5422} \\ t_{5431} & t_{5432} \end{bmatrix}$$

| $T_{(2\times3)\times(5\times4)} =$ | $\begin{bmatrix} t_{1121} \\ t_{1131} \\ t_{1141} \\ t_{1151} \\ \end{bmatrix}$ | t_{1122} t_{1132} t_{1142} t_{1152} t_{2112} t_{2122} t_{2132} | t_{1123} t_{1133} t_{1143} t_{1153} t_{2113} t_{2123} t_{2133} | t1114 t1124 t1134 t1144 t1154 t2114 t2124 t2134 t214 | $\begin{bmatrix} t_{1221} \\ t_{1231} \\ t_{1241} \\ t_{1251} \end{bmatrix}$ $\begin{bmatrix} t_{2211} \\ t_{2221} \\ t_{2231} \end{bmatrix}$ | t_{1222} t_{1232} t_{1242} t_{1252} t_{2212} t_{2222} t_{2232} | t_{1223} t_{1233} t_{1243} t_{1253} t_{2213} t_{2223} t_{2233} | t ₁₂₂₄ t ₁₂₃₄ t ₁₂₄₄ t ₁₂₅₄ t ₁₂₅₄ t ₂₂₁₄ t ₂₂₂₄ | $\begin{bmatrix} t_{1321} \\ t_{1331} \\ t_{1341} \\ t_{1351} \end{bmatrix}$ $\begin{bmatrix} t_{2311} \\ t_{2321} \\ t_{2331} \end{bmatrix}$ | t_{1322} t_{1332} t_{1342} t_{1352} t_{2312} t_{2322} t_{2332} | t_{1323} t_{1333} t_{1343} t_{1353} t_{2313} t_{2323} t_{2333} | t ₁₃₂₄ t ₁₃₃₄ t ₁₃₃₄ t ₁₃₄₄ t ₁₃₅₄ t ₂₃₁₄ t ₂₃₂₄ t ₂₃₃₄ |
|------------------------------------|---|--|--|--|---|--|--|---|---|--|--|---|
| | t ₂₁₄₁ | | | | | | | | t ₂₃₄₁ | t_{2342} | t_{2343} | t ₂₃₄₄ |
| | [<i>t</i> ₂₁₅₁ | t_{2152} | t_{2153} | t ₂₁₅₄ | t ₂₂₅₁ | t_{2252} | t_{2253} | t ₂₂₅₄ | t ₂₃₅₁ | t_{2352} | t_{2353} | t_{2354}] |



Examples of Transpose Operations for 4-Tensors

Various types of "Transpose" operations involving self-inverting index-exchange operations for one or two pairs of indices can be defined from $(4\cdot3\cdot2\cdot1)-1=23$ index re-organizations overall.

Perhaps some of the most useful of these would include: "2134-Transpose": Exchanging rows and columns within the outer matrix structure (i.e., exchanging order of first two indices) $v_{kjmn} = t_{jkmn}$; $t_{kjmn} = v_{jkmn}$;

"1243-Transpose": Exchanging rows and columns within the inner matrix structure (i.e., exchanging order of last two indices) $v_{jknm} = t_{jkmn}$; $t_{jknm} = v_{jknn}$;

"2143-Transpose": Exchanging rows and columns within the outer matrix structure (exchanging order of first two indices) and exchanging rows and columns within the inner matrix structure (exchanging order of last two indices) together $\mathbf{v}_{kjnm} = \mathbf{t}_{jkmn}$; $\mathbf{t}_{kjnm} = \mathbf{v}_{jkmn}$;

"3412-Transpose": Exchanging row-column pair of outer matrix structure (first two indices) with the row-column pair of inner matrix structure (last two indices)

ν_{mnjk}=t_{mnjk}; t_{mnjk}=ν_{jkmn};
"1324-Transpose": Grouping the row indices of both the inner and outer matrix structures (first and third indices) followed by grouping the column indices of both the inner and outer matrix structures (second and fourth indices) ν_{jmkn}=t_{jkmn}; t_{mkn}=ν_{jkmn}.

indices) $v_{jmkn} = t_{jkmn}$; $t_{jmkn} = v_{jkmn}$. Incidentally it is noted, for example that:

$$T$$
 $\xrightarrow{3412\text{-Transpose}} \Psi$

("matrix analogy" to "point spread function" re-organization from above)

$$\Psi \xrightarrow{3412\text{-Transpose}} \mathbb{T}$$

("point spread function" to "matrix analogy" re-organization)

("matrix analogy" to "variables-separable" re-organization from above)

$$\Phi \xrightarrow{1324 \text{ Transpose}} \mathbb{T}$$

("variables-separable" to "matrix analogy" re-organization)

The "Identity" 4-Tensor

As with an N×N "Identity" matrix employing the mapping

$$y_j = \sum_{n=1}^{N} a_{mn} x_n$$

to map an N-dimensional vector to a copy of itself, using $a = \delta$

where δ_{Pq} is the "Kronecker delta"

$$\delta_{pq} = \begin{cases} 0 & \text{if } p \neq q \\ 1 & \text{if } p = q \end{cases}$$

10 an "Identity" 4-tensor (for example J=M and K=N) mapping a M×N matrix to an M×N copy of itself results from employing the mapping:

$$q_{ik} = \sum_{m=1}^{M} \sum_{n=1}^{N} t_{jkmn} s_{mn}$$

with

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35

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 $t_{jkmn=\delta} \int_{im} \delta_{km}$

Note that with this (variables-separable) structure gives $q_{jk}=s_{jk}$ for each $1 \le j \le M$, $1 \le k \le N$.

Using the "matrix-of-matrices" representation, a $(3\times3)\times(3\times3)$ Identity 4-tensor $\mathbb{I}_{(3\times3)\times(3\times3)}$ would have the form:

$$\prod_{(3\times3)\times(3\times3)} = \begin{bmatrix} \begin{bmatrix} 1 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix} \begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix} \begin{bmatrix} 0 & 0 & 1 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix} \begin{bmatrix} 0 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 0 \end{bmatrix} \begin{bmatrix} 0 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 0 \end{bmatrix} \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix} \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix} \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix}$$

Such a $(3\times3)\times(3\times3)$ Identity 4-tensor would map a 3×3 pixel source image S to a 3×3 pixel result image Q with O=S.

More generally Identity 4-Tensors map an M×N matrix to an M×N matrix, but the matrices need not individually (row-column) "symmetric"—that is one does not require M=N.

For example, using the "matrix-of-matrices" representation, a $(3\times2)\times(3\times2)$ Identify 4-Tensor $\mathbb{I}_{(3\times2)\times(3\times2)}$ that maps a 3×2 matrix to a 3×2 matrix would have the form:

$$\prod_{(3\times 2)\times (3\times 2)} = \begin{bmatrix} \begin{bmatrix} 1 & 0 \\ 0 & 0 \\ 0 & 0 \end{bmatrix} & \begin{bmatrix} 0 & 1 \\ 0 & 0 \\ 0 & 0 \end{bmatrix} & \begin{bmatrix} 0 & 0 \\ 0 & 1 \\ 0 & 0 \end{bmatrix} & \begin{bmatrix} 0 & 0 \\ 0 & 1 \\ 0 & 0 \end{bmatrix} & \begin{bmatrix} 0 & 0 \\ 0 & 0 \\ 1 & 0 \end{bmatrix} & \begin{bmatrix} 0 & 0 \\ 0 & 0 \\ 1 & 0 \end{bmatrix} & \begin{bmatrix} 0 & 0 \\ 0 & 0 \\ 1 & 0 \end{bmatrix} & \begin{bmatrix} 0 & 0 \\ 0 & 0 \\ 0 & 1 \end{bmatrix} & \begin{bmatrix} 0 & 0 \\ 0 & 0 \\ 0 & 1 \end{bmatrix} & \begin{bmatrix} 0 & 0 \\ 0 & 1 \\ 0 & 1 \end{bmatrix}$$

Such a $(3\times2)\times(3\times2)$ Identity 4-tensor would map a 3×2 pixel source image S to a 3×2 pixel result image Q with O=S.

For each of these Identity 4-tensor examples, regarding Remark 1 above (as to interpreting the values of elements in the interior matrix with block-position index $\{j, k\}$ in an

(m×N)×(M×N) "matrix of matrices" as representing a "heat map" of responsiveness of an observed or measured sensor pixel q_{ik} in the observed or measured image matrix Q to source image pixels s_{mn} in the image source matrix S), the structure of an M×N×M×N Identity 4-tensor is crystal clear 5 as to it rendering $q_{jk}=s_{jk}$ for each $1 \le j \le M$, $1 \le k \le N$.

Re-Indexing and Reorganization a 4-Tensor-Operator Matrix-to-Matrix (Image-to-Image) Equation as a Matrix-Operator Vector-to-Vector Equation

two-dimensional neighboring arrangement of pixels, and other such two-dimensional indexing details are essential, some linear transformations act entirely independently of the two-dimensional index structure. An example, are situations where one can regard the relationships defined by a tensor 15 mapping between matrices such as

$$Q = \mathbb{T}S$$

as simply representing a set of simultaneous equations

$$q_{jk} = \sum_{m=1}^{M} \sum_{n=1}^{N} t_{jkmn} s_{mn}$$
$$1 \le j \le J, 1 \le k \le K.$$

In such circumstances one could without consequence uniquely re-index the variables with an indexing scheme that serializes the index sequence in an invertible way. For example, one can define two serializing indices p and q to 30 serialize a J×K×M×N dimensional 4-tensor T comprising elements t_{jkmn} into a JK×MN dimensional matrix T comprising elements t_{pq} using the index-mapping relations

$$p = (j-1)K + k$$

r = (m-1)N + n

those relations can be inverted via

$$j=\operatorname{Mod}(p-1,K)+1$$

k=Floor(p^{-1}/K)+1=Ceiling[p/K]

 $m = \operatorname{Mod}(r-1, N) + 1$

$$n=Floor(r^{-1}/N)+1=Ceiling[r/N]$$

Using these, one can define the serialized-index vectors q, comprising elements

$$q_p \ 1 \le p \le JK$$

and s, comprising elements

 $s_r. 1 \le r \le MN$,

which are simply "scanned" or "flattened" versions of matrix Q, comprising elements

$$q_{jk} \ 1 \le j \le J, \ \le k \le K$$

and matrix S, comprising elements

 $s_{mn} \ 1 \le m \le M, \ 1 \le n \le N$

An example "scanning" or "flattening" index correspondence is

$$q_{(j-1)K+k} \leftrightarrow q_{jk} \ 1 \le j \le J, \ 1 \le k \le K$$

$$s_{(m-1)N+n} {\leftrightarrow} s_{mn} \ 1{\leq} m{\leq} M, \ 1{\leq} n{\leq} N$$

and its corresponding inverse correspondence is

$$s_r {\leftrightarrow} s_{Mod(r-1,N)+1,Ceiling(r/N)}, \ 1 {\leq} r {\leq} MN.$$

The last pair of these index correspondences can be used to formally define index-serializing mappings

$$q_p {=} q_{Mod(p-1,N)+1,Ceiling(p/K)}, \ 1 {\leq} p {\leq} JK$$

$$s_r = s_{Mod(r-1,N)+1,Ceiling(r/N)}, \ 1 \leq r \leq MN$$

Although in an image the row and column ordering, 10 that provide a flattening reorganization of the elements q_{jk} comprised by the J×K-dimensional matrix Q into a vector q comprising elements q_p , and a flattening reorganization of the elements s_{mn} comprised the M×N-dimensional matrix S into a vector s comprising elements s_r. These result in flattening transformations $Q \rightarrow q$ and $\rightarrow s$.

> The first pair of the index correspondences can be used to formally define index-vectorizing mappings

$$q_{jk} = q_{(j-1)K+k} \ 1 \le j \le J, \ 1 \le k \le K$$

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$$s_{mn} = s_{(m-1)N+n} \ 1 \le m \le M, \ 1 \le n \le N$$

that provide a partitioning reorganization of the elements q_p of vector q into the elements q_{jk} comprised by the J×Kdimensional matrix Q, and a partitioning reorganization of the elements s_r of vector q into the elements s_{mn} comprised the M×N-dimensional matrix S. These result in partitioning transformations q→Q and s→S which reconstruct the matrices Q and S from the serialized vectors q and s.

In a corresponding way, one can use these same serialized-indices to correspondingly re-label and reorganize the values of the $(J\times K)\times (M\times N)$ -dimensional tensor \mathbb{T} to the JK×MN-dimensional matrix T. The mapping $\mathbb{T} \to T$ is given

$$t_{(j-1)K+k,(m-1)N+n} = t_{jkmn}$$

 $1 \le j \le J$, $1 \le k \le K$, $1 \le m \le M$, $1 \le n \le N$

and the reverse mapping $T \rightarrow T$ is given by

$$t_{Mod(p-1,K)+1,Ceiling(p/K),Mod(r-1,K)+1,Ceiling(r/N)} = t_{pr}$$
4()

Thus. because of the transformational equivalence between

$$q_{jk} = \sum_{m=1}^{M} \sum_{n=1}^{N} t_{jkmn} s_{mn}$$
 (Matrix-Tensor equation)

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$$q_p = \sum_{r=1}^{M+N} t_{pr} s_r$$
 (Vector-Matrix equation)

55 for the same (but re-indexed) variables, this allows one to exactly represent the matrix-tensor equation

$$Q = \mathbb{T}_S$$

as an equivalent vector-matrix equation

$$q = Ts$$

More generally, the index serialization functions can be arbitrary as long as they are one-to-one and onto over the full range and domain of the respective indices, and invertably 65 map pairs of integers to single integers. For example they could be organized as a scan in other ways, or even follow fixed randomly-assigned mapping. In general one can write:

$$q_{jk} = \sum_{m=1}^{M} \sum_{n=1}^{N} I_{jkmn} s_{mn} \stackrel{\stackrel{=}{=}}{\rightarrow} q_p = \sum_{p=1}^{M*N} I_{pr} s_r$$

and
$$q_p = \sum_{p=1}^{M*N} t_{pr} s_r \overset{\equiv}{\to} q_{jk} = \sum_{m=1}^{M} \sum_{n=1}^{N} t_{jkmn} s_{mn}$$

or more compactly

$$Q = \mathbb{T} S \xrightarrow{index \ serialization} q = Ts$$

$$q = Ts \xrightarrow{index \ vectorization} O = \mathbb{T} S$$

or more abstractly

$$Q = \mathbb{T} S \xrightarrow{Array \ Flatten} q = Ts$$

$$q = Ts \xrightarrow{Array \ Partition} Q = \mathbb{T} S.$$

This is extremely valuable as it allows for matrix methods to solve inverse problems or implement transformations on images in terms of matrices. Of course matrix methods have been used in variables-separable image processing for decades employing various ad hoc constructions. Those ad 30 hoc constructions could be formalized with the aforedescribed 4-tensor representation should one be interested in the exercises, but more importantly the computation of the aforedescribed 4-tensor representation and the formal isomorphic equivalence between 4-tensor linear transformations mapping matrices (representing images) to matrices (representing images) and matrix transformations mapping vectors to vectors allows clarity and methodology to complicated non-variables-separable linear imaging transformations, inverses, pseudo-inverses, etc. Also importantly the aforedescribed 4-tensor representation readily extends to mappings among tensors as may be useful in color, multiplewavelength, tomographic, spatial-data, and many other settings and applications.

Additionally, as an aside: the aforedescribed 4-tensor representation naturally defines eigenvalue/eigenmatrix and 45 eigenvalue/eigentensor problems; for example the eigenvalue/eigenmatrix problem $\mathbb{T}_{Z_i=\lambda_i Z_i \ 1 \leq i \leq JK}$

$$T_{Z_i = \lambda_i Z_i \ 1 \le i \le JK}$$

for $\mathbb T\,$ a J×K×J×K 4-tensor, the collection of indexed scalars $\{\lambda_i\}$ 1 \leq i \leq JK the scalar eigenvalues, and the collection of indexed matrices $\{Z_i\}$ $1 \le i \le JK$ the eigenmatrices is equivalent to the eigenvalue/eigenvector problem

$$Tz_i=\lambda_i z_i\ 1\le i\le JK$$
 via
$$\mathbb{T}\xrightarrow{Array\ Flatten}\ T;\ Z_i\xrightarrow{Array\ Flatten}\ z_i$$

for calculation and analysis and transformed back via

$$T \xrightarrow{Array Partition} T$$
; $z_i \xrightarrow{Array Partition} Z_i$

These general process can be order-extended and further generalized to similarly transform eigenvalue/eigentensor problems into equivalent eigenvalue/eigenvector problems, and extended further in various ways to replace the eigenvalue scalars with an "eigenvalue array."

As and additional aside, these same and similar approaches employing

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$$T \xrightarrow{Array \ Partition} \quad T ; \ z_i \xrightarrow{Array \ Partition} \quad Z_i$$

$$T \xrightarrow{Array \ Flatten} \quad T ; \ z_i \xrightarrow{Array \ Flatten} \quad z_i$$

15 and other combined or more generalized reorganization methods

can be order-extended and further generalized to similarly transform the vast understanding, rules, bases, transformations, vector spaces, spaces of matrices, properties of matrices, and matrix-vector equations into a wide range of tensor understandings, tensor rules, tensor bases, tensor transformations, and properties of tensors, spaces of tensors, and tensor-matrix and tensor-tensor equations.

Attention is next directed to inversion and then to image formation, and then after first developing and using extensions of the aforedescribed 4-tensor representation to mappings among tensors) expanding these to color/multiplewavelength imaging applications.

35 Inverse of a 4-Tensor

Accordingly, for

$$Q = \mathbb{T} S$$
 with $M = J, N = K$,

if all the represented individual equations are linearly independent and of full rank, then the matrix T defined by

$$T$$
 $\xrightarrow{Array\ Flatten}$ T : T $\xrightarrow{Array\ Partition}$ T

is invertible and the pixel values of the source image S can be obtained from the pixel values of the measurement Q by simply inverting the matrix T:

$$S=T^{-1}q$$

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where the corresponding "flattening" and "partitioning" index transformations are employed among the matrices and vectors

$$S \xrightarrow{Array \ Flatten} \quad s; \quad s \xrightarrow{Array \ Partition} \quad S$$

$$Q \xrightarrow{Array \ Flatten} \quad q; \quad q \xrightarrow{Array \ Partition} \quad Q.$$

Further, the pixel values of the source image S can be obtained from the pixel values of the measurement Q by simply inverting the matrix T to obtain T^{-1} , multiplying the flattened measurement data q with T⁻¹ to obtain the vector s, and partitioning the result into the source (image) matrix S:

$$Q \xrightarrow{Array\ Flatten} q \xrightarrow{T^{-1}q} s \xrightarrow{Array\ Parition} S$$

It is noted that effectively the column vectors of the matrix T serve as the natural linearly-independent spanning basis of the composite sensor and optical arrangement corresponding to a particular positioning situation. The natural linearly-independent spanning basis is not necessarily orthogonal, although it can of course be orthogonalized if useful using Gram-Schmitt of other methods. Additionally, the natural linearly-independent spanning basis can be transformed into other coordinate systems defined by other basis functions should that be useful. Such transformations can include the effects of discrete Fourier transforms, wavelet transforms, Walsh/Hadamard transforms, geometric rotations and scaling transforms, etc.

The simple approach employing T⁻¹ reconstructs the image by simply reproducing individual columns of an 20 identity matrix, more precisely a diagonal matrix whose non-zero diagonal elements represent the light amplitude at a particular pixel. The invention provides for the replacement of this simple approach with other methods fitting into the same structure or delivering the same effect; for example projection techniques, matched filters, generalized inverses, SVD operations, sparse matrix operations, etc. These can be formatted in Tensor or matrix paradigms in view of the formal transformational tensor/matrix isomorphism established above. An example of this, namely the pseudo inverse case of a generalized inverse operation.

It is noted that the matrix T can become quite large, making inversion and subsequent operations described above numerically and computationally challenging. The invention provides for separating matrix T operations into smaller blocks (for example JPEG and MPEG regularly employ 8×8 and 16×16 blocks). The invention provides for these blocks to be non-overlapping, to overlap, and to be interleaved. The invention further provides for blocked 40 inversion results involving overlapping blocks or interleaving blocks to be combined by linear or other operations to suppress block-boundary artifacts.

Pseudo-Inverse of a 4-Tensor

Further, because in image capture a system usually spatially quantizes natural source image without a pixel structure, it is additional possible to measure a larger number of pixels than will be used in the final delivered image, that is M<J and N<K.

In traditional image processing such an excess-measurement scheme can be used in various "oversampling" methods, or could be decimated via resampling. Instead of these, the excess measurements can be used to create an overspecified system of equations that provides other opportunities. For example, the resulting over-specified matrix T can be used to generate a generalized inverse T⁺.

For example, if the 4-tensor T represents a transformation of a 2-dimensional (monochromatic) "source image" represented as an M×N matrix of "brightness" values:

$$S = \begin{bmatrix} s_{11} & \dots & s_{1N} \\ \vdots & & \vdots \\ s_{M1} & \dots & s_{MN} \end{bmatrix}$$

to a J×K array of measured 2-dimensional (monochromatic) image data represented as a J×K matrix of "brightness" values:

$$Q = \begin{bmatrix} q_{11} & \cdots & q_{1K} \\ \vdots & & \vdots \\ q_{J1} & \cdots & q_{JK} \end{bmatrix}$$
with $M < J$, $N < K$, via
$$q_{jk} = \sum_{m=1}^{M} \sum_{n=1}^{N} t_{jkmn} s_{mn}$$

$$1 \le j \le J$$
, $1 \le k \le K$.

represented as

$$Q = \mathbb{T}_S$$

then a pseudo-inverse tensor \mathbb{T}^+ can be defined via:

$$T \xrightarrow{Array Flatten} T \xrightarrow{Pseudo-Inverse Formulation} T^+ \xrightarrow{Array Partition} T$$

and represented as

$$S = \mathbb{T} + Q$$

Further, the pixel values of the source image S can be obtained from the pixel values of the measurement Q by forming the pseudo-inverse of the matrix T, multiplying the flattened measurement data q with T⁺ to obtain the vector s, and partitioning the result into the source (image) matrix S:

$$Q \xrightarrow{Array\ Flatten} q \xrightarrow{T^+ q} s \xrightarrow{Array\ Partition} S$$

There are a number of pseudo-inverses and related singular-value decomposition operators, but of these it can be advantageous for the optical imaging methods to be described for the generalized inverse T^+ to be specifically the "Moore-Penrose" generalized (left) inverse defined (when a matrix T has all linearly-independent columns) using the matrix transpose T^T or conjugate transpose T^\dagger of T and matrix inverse operations as:

$$T^+=(T^T T)^{-1}T^T$$
 for real-valued T

$$T^+=(T^{\dagger}T)^{-1}$$
 T^{\dagger} for complex-valued T

(There is also Moore-Penrose generalized "right" inverse defined when a matrix T has all linearly-independent rows.) The Moore-Penrose generalized inverse inherently provides a "Least-Squares" statistical fit where solvable subsets of the larger number of equations give different inconsistent solutions. This "Least-Squares" statistical fit can provide robustness to the imaging system, for example in the case where one or more sensor elements degrade, are damaged, are occulted by dirt, are occulted by objects, are altered by transparent or translucent droplets or deposits, etc.

Using the Moore-Penrose generalized inverse for real-valued pixel quantities, the pixel values of the source image S can be obtained from the pixel values of the measurement Q by forming the pseudo-inverse of the matrix T, multiplying the flattened measurement data q with T⁺ to obtain the vector s, and partitioning the result into the source (image) matrix S:

$$Q \xrightarrow{Array Flatten} q \xrightarrow{(T^T T)^{-1} T^T q} s \xrightarrow{Array Partition} S$$

Configurations for Applications

Drawing on the functionality described above and taught in the Inventor's related lensless imaging patent filings listed at the beginning of this application, a wide range of additional provisions and configurations can be provided so as to support of vast number of valuable and perhaps slightly revolutionary imaging applications.

In an example generalizing assessment, the invention provides for a rigid or flexible surface to be configured to implement a lensless light-field sensor, producing electrical 15 signals that can be used in real time, or stored and later retrieved, and provided to a computational inverse model algorithm executing on computational hardware comprising one or more computing elements so as to implement a lensless light-field camera.

In another aspect of the invention, a rigid surface is configured to additionally function as a housing and thus operate as a "seeing housing".

In another aspect of the invention, a rigid surface is configured to additionally function as a protective plate and 25 surface performs imaging. thus operate as a "seeing armor".

In another aspect of the invention, a rigid surface is configured to additionally function as an attachable tile and thus operate as a "seeing tile".

In another aspect of the invention, a rigid surface is configured to additionally function as an attachable film and thus operate as a "seeing film".

In another aspect of the invention, a flexible surface is configured to additionally function as an attachable film and 35 material. thus operate as a "seeing film".

In another aspect of the invention, a flexible surface is configured to additionally function as a garment and thus operate as a "seeing garment".

In another aspect of the invention, a flexible surface is 40 configured to additionally function as a shroud and thus operate as a "seeing shroud".

In another aspect of the invention, a flexible surface is configured to additionally function as an enveloping skin and thus operate as a "seeing skin".

In another aspect of the invention, the rigid or flexible surface is small in size.

In another aspect of the invention, the rigid or flexible surface is large in size.

surface is flat.

In another aspect of the invention, the rigid or flexible surface is curved.

In another aspect of the invention, the rigid or flexible surface is rendered as a polytope.

In another aspect of the invention, the rigid or flexible surface is rendered as a dome.

In another aspect of the invention, the rigid or flexible surface is rendered as a part of a sphere.

In another aspect of the invention, the rigid or flexible 60 surface is rendered as a part of a spheroid.

In another aspect of the invention, the rigid or flexible surface is rendered as a sphere.

In another aspect of the invention, the rigid or flexible surface is rendered as a spheroid.

In another aspect of the invention, the rigid or flexible surface is transparent.

In another aspect of the invention, the rigid or flexible surface is translucent.

In another aspect of the invention, the rigid or flexible surface is opaque.

In another aspect of the invention, the rigid or flexible surface performs contact sensing.

In another aspect of the invention, the rigid or flexible surface is configured to perform contact image sensing with near-zero separation distance.

In another aspect of the invention, the rigid or flexible surface is configured to perform contact image sensing with zero separation distance.

In another aspect of the invention, the rigid or flexible surface performs distributed optical imaging.

In another aspect of the invention, the rigid or flexible surface performs distributed optical sensing.

In another aspect of the invention, the rigid or flexible surface performs image sensing of ultraviolet light.

In another aspect of the invention, the rigid or flexible 20 surface performs image sensing of infrared light.

In another aspect of the invention, the rigid or flexible surface performs image sensing of selected ranges of visible color light.

In another aspect of the invention, the rigid or flexible

In another aspect of the invention, the rigid or flexible surface performs distributed chemical sensing employing optical chemical sensing properties of at least one material.

In another aspect of the invention, the rigid or flexible surface performs distributed radiation sensing employing optical radiation sensing properties of at least one material.

In another aspect of the invention, the rigid or flexible surface performs distributed magnetic field sensing employing optical magnetic field sensing properties of at least one

In another aspect of the invention, the rigid or flexible surface is configured to emit light.

In another aspect of the invention, the rigid or flexible surface is configured to operate as a light-emitting display.

In another aspect of the invention, the rigid or flexible surface is configured to operate as a selectively self-illuminating contact imaging sensor.

In another aspect of the invention, the computational inverse model algorithm is configured to provide variable 45 focusing.

In another aspect of the invention, the computational inverse model algorithm is configured to mixed depth-offield focusing.

In another aspect of the invention, the computational In another aspect of the invention, the rigid or flexible 50 inverse model algorithm is configured to implement a viewpoint with a controllable location.

In another aspect of the invention, the computational inverse model algorithm is configured to implement a plurality of viewpoints, each viewpoint having a separately 55 controllable location.

In another aspect of the invention, the computational inverse model algorithm is configured to provide pairs of outputs so as to function as a stereoscopic camera.

In another aspect of the invention, the computational inverse model algorithm is configured to capture a panoramic view.

In another aspect of the invention, the computational inverse model algorithm is configured to capture a 360degree view.

In another aspect of the invention, the computational inverse model algorithm is configured to capture a partial spherical view.

In another aspect of the invention, the computational inverse model algorithm is configured to capture a full spherical view.

In another aspect of the invention, the rigid or flexible surface is configured to perform enveloping image sensing 5 with near-zero separation distance.

In another aspect of the invention, the rigid or flexible surface is configured to perform contact enveloping sensing with zero separation distance.

In another aspect of the invention, the rigid or flexible 10 surface is configured to operate as a selectively self-illuminating enveloping imaging sensor.

In another aspect of the invention, the computational inverse model algorithm is configured to operate at slowframe video rates.

In another aspect of the invention, the computational inverse model algorithm is configured to operate at conventional video rates.

In another aspect of the invention, the computational inverse model algorithm and computational hardware is 20 [B3] A. J. Devaney, Mathematical Foundations of Imaging, configured to operate at high-speed video rates.

CLOSING

The terms "certain embodiments", "an embodiment", 25 [B5] O. Scherzer, M. Grasmair, H. Grossauer, M. Haltmeier, "embodiment", "embodiments", "the embodiment", "the embodiments", "one or more embodiments", "some embodiments", and "one embodiment" mean one or more (but not all) embodiments unless expressly specified otherwise. The terms "including", "comprising", "having" and 30 variations thereof mean "including but not limited to", unless expressly specified otherwise. The enumerated listing of items does not imply that any or all of the items are mutually exclusive, unless expressly specified otherwise. The terms "a", "an" and "the" mean "one or more", unless 35 expressly specified otherwise.

The foregoing description, for purpose of explanation, has been described with reference to specific embodiments. However, the illustrative discussions above are not intended to be exhaustive or to limit the invention to the precise forms 40 disclosed. Many modifications and variations are possible in view of the above teachings. The embodiments were chosen and described in order to best explain the principles of the invention and its practical applications, to thereby enable others skilled in the art to best utilize the invention and 45 various embodiments with various modifications as are suited to the particular use contemplated.

While the invention has been described in detail with reference to disclosed embodiments, various modifications within the scope of the invention will be apparent to those 50 of ordinary skill in this technological field. It is to be appreciated that features described with respect to one embodiment typically can be applied to other embodiments.

The invention can be embodied in other specific forms without departing from the spirit or essential characteristics 55 [B15] A. Albert, Regression and the Moore-Penrose Pseudothereof. The present embodiments are therefore to be considered in all respects as illustrative and not restrictive, the scope of the invention being indicated by the appended claims rather than by the foregoing description, and all changes which come within the meaning and range of 60 equivalency of the claims are therefore intended to be embraced therein.

Although exemplary embodiments have been provided in detail, various changes, substitutions and alternations could be made thereto without departing from spirit and scope of 65 the disclosed subject matter as defined by the appended claims. Variations described for the embodiments may be

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realized in any combination desirable for each particular application. Thus particular limitations and embodiment enhancements described herein, which may have particular advantages to a particular application, need not be used for all applications. Also, not all limitations need be implemented in methods, systems, and apparatuses including one or more concepts described with relation to the provided embodiments. Therefore, the invention properly is to be construed with reference to the claims.

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What is claimed is:

- 1. A lensless light-field imaging system, comprising:
- an array of light sensing elements, each light-sensing element comprising a light-sensing area and each light-sensing element configured to generate an electrical photocurrent responsive to an amplitude of incoming light striking a light-sensing surface, each light-sensing surface arranged to experience angularly-varying sensitivity responsive to a direction of each path of the incoming light striking the light-sensing surface;
- electronics configured to interface the array of light sensing elements and further configured to provide a plurality of electronically-represented digital numbers, each digital number responsive to light received by at least one light-sensing element in the array of light sensing elements, producing a result comprising a plurality of electronically-represented digital numbers;
- an algorithm configured to execute on a computational processor, the algorithm for computing a two-dimensional image representation from the plurality of electronically-represented digital numbers, the two-dimensional image representation corresponding to portion of a focused image at a separation distance value measured perpendicular to the light-sensing surface of the one of the light sensing elements in the array of light sensing elements, there being a plurality of separation distance values,
- wherein each of the electronically-represented digital numbers are responsive to the amplitude of incoming light striking the light-sensing surface of an associated light sensing element in the array of light sensing elements and a plurality of focused image portions, and wherein the plurality of separation distance values are not a substantially same numeric value.
- 2. The lensless light-field imaging system of claim 1, wherein the light sensing elements of the array of light sensing elements are oriented in space to form a curved surface.
- 3. The lensless light-field imaging system of claim 1, wherein spatial positions of the plurality of focused image portions form a planar surface.
- **4.** The lensless light-field imaging system of claim **1**, wherein the light sensing elements of the array of light sensing elements are oriented in space to form a planar surface.
- **5**. The lensless light-field imaging system of claim **1**, wherein spatial positions of the plurality of focused image portions form a curved surface.
- **6.** The lensless light-field imaging system of claim **1**, wherein the light sensing elements of the array of light sensing elements are oriented in space to form a first curved surface and spatial positions of the plurality of focused image portions form a second curved surface.
- 7. The lensless light-field imaging system of claim 1, wherein the algorithm is controlled by at least one separation distance parameter.
- **8**. The lensless light-field imaging system of claim **1**, wherein the light sensing elements comprise organic semiconductors.

- 9. The lensless light-field imaging system of claim 1, wherein the light sensing elements comprise semiconductors that are co-optimized for both light emission and light sensing.
- 10. The lensless light-field imaging system of claim 1, wherein the light sensing elements are arranged to emit light for an interval of time.
- 11. The lensless light-field imaging system of claim 1, wherein the angularly-varying sensitivity of the light sensing elements results at least in part from a structure of the light sensing elements.
- 12. The lensless light-field imaging system of claim 1, wherein the angularly-varying sensitivity of the light sensing elements results at least in part from a structure attached to the array of light sensing elements.
- 13. The lensless light-field imaging system of claim 12, wherein the structure attached to the array of light sensing elements comprises segregated optical paths.
- 14. The lensless light-field imaging system of claim 13, $_{20}$ wherein the segregated optical paths are created by separating surfaces.
- 15. The lensless light-field imaging system of claim 13, wherein the separating surfaces are at least partially-reflective.

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- 16. The lensless light-field imaging system of claim 13, wherein at least one of the light sensing elements is color selective.
- 17. The lensless light-field imaging system of claim 13, wherein a color selective property results from a band gap property of a semiconductor device element comprised by the at least one of the light sensing elements.
- 18. The lensless light-field imaging system of claim 1, wherein the algorithm comprises array multiplication of numerical values obtained from calculation of a generalized inverse matrix.
- 19. The lensless light-field imaging system of claim 1, wherein the algorithm comprises array multiplication of numerical values obtained from an interpolation.
- 20. The lensless light-field imaging system of claim 1, wherein the algorithm comprises array multiplication of numerical values obtained from a predictive analytical model.
- 21. The lensless light-field imaging system of claim 1, wherein the algorithm comprises array multiplication of numerical values derived from a predictive analytical model.
- 22. The lensless light-field imaging system of claim 1, wherein the algorithm comprises array multiplication of numerical values derived from empirical measurements.

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